

Theta6 = 100deg and Theta7 = 20deg
 Link 1 is 9m long, Link 2 is 5m long, Link 3 is 7m long, Link 4 is 9m long
 Lamda2 = 50deg
 lamda3 = 55deg
 lamda4 = 50deg
 lamda5 = -20 deg

Initialization, Constants, Procedures:

```

[ reset()

[ use(plot):
Warning: 'hull' already has a value, not exported. [use]
Warning: 'Integral' seems to be protected; not exported. [use]
Warning: 'Pyramid' seems to be protected; not exported. [use]

[ iexp:=proc(theta) begin exp(I*theta) end_proc:

[ arr:=proc(v1,v2) begin plot::Arrow2d([Re(v1),Im(v1)],
[Re(v2),Im(v2)],Color=mycolor,
LineWidth=mylinewidth)
end_proc:

[ lin:=proc(v1,v2) begin plot::Line2d([Re(v1),Im(v1)],
[Re(v2),Im(v2)],Color=mycolor,
LineWidth=mylinewidth)
end_proc:

[ dtr:=float(PI/180):
  
```

```
[ L1:=9: L2:=5: L3:=7: L4:=9:
[ lambda2 := 50*dtr:
[ lambda3 := 55*dtr:
[ lambda4 := 50*dtr:
[ lambda5 := -20*dtr:
[ theta6:=100*dtr:
[ theta7:=20*dtr:
[ T0:=3 // Value selected for plotting convenience (all vectors scale)
[ 3
```

Solve to find angles Phi1 and Phi2:

```
[ EqPhi:=L1*iexp(theta6)+L2*iexp(theta6+phi1)=
[ L4*iexp(theta7)+L3*iexp(theta7+phi2)
[ 5 ephi1 i+1.745329252 i - 1.562833599 + 8.863269777 i = 7 ephi2 i+0.3490658504 i + 8.457233587 + 3.07818129 i
[ assume (phi1 in R_)
[ assume(phi2 in R_)
[
[ EqPhi1:=Re(lhs(EqPhi))=Re(rhs(EqPhi))
[ 5.0 cos(phi1 + 1.745329252) - 1.562833599 = 7.0 cos(phi2 + 0.3490658504) + 8.457233587
[ EqPhi2:=Im(lhs(EqPhi))=Im(rhs(EqPhi))
[ 5.0 sin(phi1 + 1.745329252) + 8.863269777 = 7.0 sin(phi2 + 0.3490658504) + 3.07818129
[
[ PhiSoln:=numeric::solve({EqPhi1,EqPhi2},[phi1=2,phi2=2])
[ {[phi1 = 3.695379566, phi2 = 2.494772348]}
[ phi1:=phi1|PhiSoln
[ 3.695379566
[ phi2:=phi2|PhiSoln
[ 2.494772348
[ phi1/dtr
[ 211.7296528
[ phi2/dtr
[ 142.9399264
```

Solve to find tension T1 and T2 to balance forces applied at end of bar 1

```
[ Eq1:=T0*iexp(PI-lambda5)+T0*iexp(lambda4)+T1*iexp(theta6-PI)
[ +T2*iexp(theta6+phi1)=0
[ T1 (0.1736481777 - 0.984807753 i) + T2 (0.66561668 - 0.7462937996 i) - 0.8907150333 + 1.272072899 i :
[
[ Eq1r:=Re(lhs(Eq1))=0
```

$$\Re(T1 (0.1736481777 - 0.984807753 i)) + \Re(T2 (0.66561668 - 0.7462937996 i)) - 0.8907150333 = 0$$

$$\text{Eq1i} := \text{Im}(\text{lhs}(\text{Eq1})) = 0$$

$$0.1736481777 \Im(T1) + 0.66561668 \Im(T2) - 0.984807753 \Re(T1) - 0.7462937996 \Re(T2) + 1.272072899 = 0$$

$$\text{T12soln} := \text{solve}(\{\text{Eq1r}, \text{Eq1i}\}, \{T1, T2\})$$

$$\{[T1 = 0.3460234127, T2 = 1.247908478]\}$$

$$T1 := T1 | \text{T12soln}$$

$$0.3460234127$$

$$T2 := T2 | \text{T12soln}$$

$$1.247908478$$

Solve to find tension T3 and T4 to balance forces applied at end of bar 4

$$\text{Eq4} := T0 * i \exp(\pi/2 - \lambda_3) + T0 * i \exp(-\pi/2 + \lambda_2) + T4 * i \exp(\theta_7 - \pi) + T3 * i \exp(\theta_7 + \phi_2) = 0$$

$$T3 (-0.9559976837 + 0.2933742127 i) + T4 (-0.9396926208 - 0.3420201433 i) + \frac{3}{e^{\frac{\pi i}{2} - 0.872664626 i}} + 3 e^{\frac{\pi}{2}}$$

$$\text{Eq4r} := \Re(\text{lhs}(\text{Eq4})) = 0$$

$$\Re(T4 (-0.9396926208 - 0.3420201433 i)) + \Re(T3 (-0.9559976837 + 0.2933742127 i)) + 3.0 \cos(0.872664626)$$

$$\text{Eq4i} := \Im(\text{lhs}(\text{Eq4})) = 0$$

$$3.0 \sin\left(\frac{\pi}{2} - 0.9599310886\right) - 0.9559976837 \Im(T3) - 0.9396926208 \Im(T4) + 0.2933742127 \Re(T3) - 0.3420201433 \Re(T4) = 0$$

$$\text{T34soln} := \text{solve}(\{\text{Eq4r}, \text{Eq4i}\}, \{T3, T4\})$$

$$\{[T3 = 3.022671346, T4 = 1.985673416]\}$$

$$T3 := T3 | \text{T34soln}$$

$$3.022671346$$

$$T4 := T4 | \text{T34soln}$$

$$1.985673416$$

Solve to find Spring force vector for info

$$\text{EqS} := T2 * i \exp(\theta_6 + \phi_1 - \pi) + T3 * i \exp(\theta_7 + \phi_2 - \pi) + T_s * i \exp(\theta_s - \pi) = 0$$

$$2.059038107 - T_s e^{i \theta_s} + 0.04453253328 i = 0$$

$$\text{EqSr} := \Re(\text{lhs}(\text{EqS})) = 0$$

$$2.059038107 - \Re(T_s e^{i \theta_s}) = 0$$

$$\text{EqSi} := \Im(\text{lhs}(\text{EqS})) = 0$$

$$0.04453253328 - \Im(T_s e^{i \theta_s}) = 0$$

```

[ Tssoln:=solve({EqSr,EqSi},{Ts,thetaS})
[   {[Ts = 2.059519622, thetaS = 0.02162446218]}
First generate the bars: B1 thru B4
[ mylinewidth:=2:
[ mycolor:=RGB::Blue:

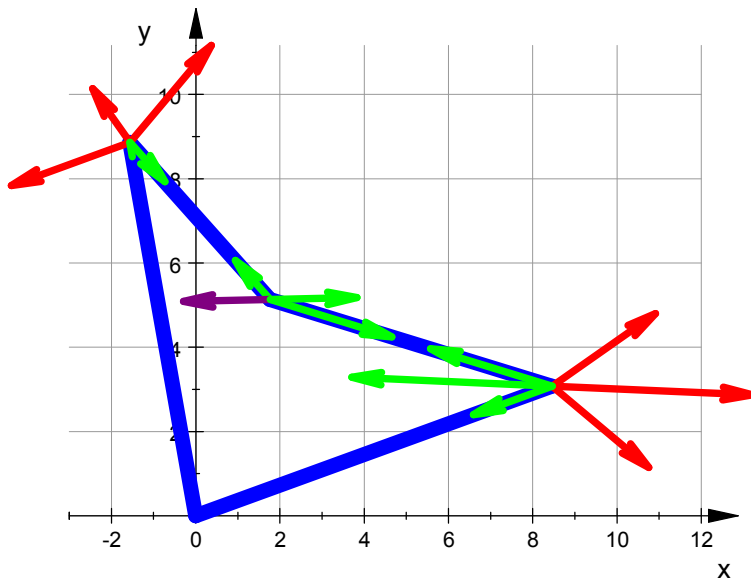
[ B1:=lin(0,L1*iexp(theta6)):
[ B4:=lin(0,L4*iexp(theta7)):
[ B2:=lin(L1*iexp(theta6),L1*iexp(theta6)+L2*iexp(theta6+phi1)):
[ B3:=lin(L4*iexp(theta7),L4*iexp(theta7)+L3*iexp(theta7+phi2)):
Now generate the applied forces of magnitude T0
[ mylinewidth:=1:
[ mycolor:=RGB::Red:
[ AT04:=arr(L1*iexp(theta6),L1*iexp(theta6)+T0*iexp(lambda4)):
[
[ AT05:=arr(L1*iexp(theta6),L1*iexp(theta6)+T0*iexp(PI-lambda5)):
[ AT0405:=arr(L1*iexp(theta6),L1*iexp(theta6)+T0*iexp(PI-lambda5)
[   +T0*iexp(lambda4)):
[ AT02:=arr(L4*iexp(theta7),L1*iexp(theta7)+T0*iexp(-PI/2+lambda2)):
[ AT03:=arr(L4*iexp(theta7),L1*iexp(theta7)+T0*iexp(PI/2-lambda3)):
[ AT0304:=arr(L4*iexp(theta7),L1*iexp(theta7)
[   +T0*iexp(PI/2-lambda3)+T0*iexp(-PI/2+lambda2)):
[
Now generate the vectors for tension in the bars
[ mycolor:=RGB::Green:
[
[ AT1:=lin(L1*iexp(theta6),L1*iexp(theta6)+T1*iexp(theta6-PI)):
[ AT2:=arr(L1*iexp(theta6),L1*iexp(theta6)+T2*iexp(theta6+phi1)):
[ AT3:=arr(L4*iexp(theta7),L4*iexp(theta7)+T3*iexp(theta7+phi2)):
[ AT4:=arr(L4*iexp(theta7),L4*iexp(theta7)+T4*iexp(theta7-PI)):
[ AT2A:=arr(L1*iexp(theta6)+L2*iexp(theta6+phi1),
[   L1*iexp(theta6)+L2*iexp(theta6+phi1)+T2*iexp(theta6+phi1-PI)):
[
[ AT3A:=arr(L4*iexp(theta7)+L3*iexp(theta7+phi2),
[   L4*iexp(theta7)+L3*iexp(theta7+phi2)+T3*iexp(theta7+phi2-PI)):
[ AT34:=arr(L4*iexp(theta7),L4*iexp(theta7)
[   +T3*iexp(theta7+phi2)+T4*iexp(theta7-PI)):
[ ATS:=arr(L1*iexp(theta6)+L2*iexp(theta6+phi1),
[   L1*iexp(theta6)+L2*iexp(theta6+phi1)-T2*iexp(theta6+phi1-PI)
[   -T3*iexp(theta7+phi2-PI)):
[ ATSOpp:=arr(L1*iexp(theta6)+L2*iexp(theta6+phi1),
[   L1*iexp(theta6)+L2*iexp(theta6+phi1)+T2*iexp(theta6+phi1-PI)

```

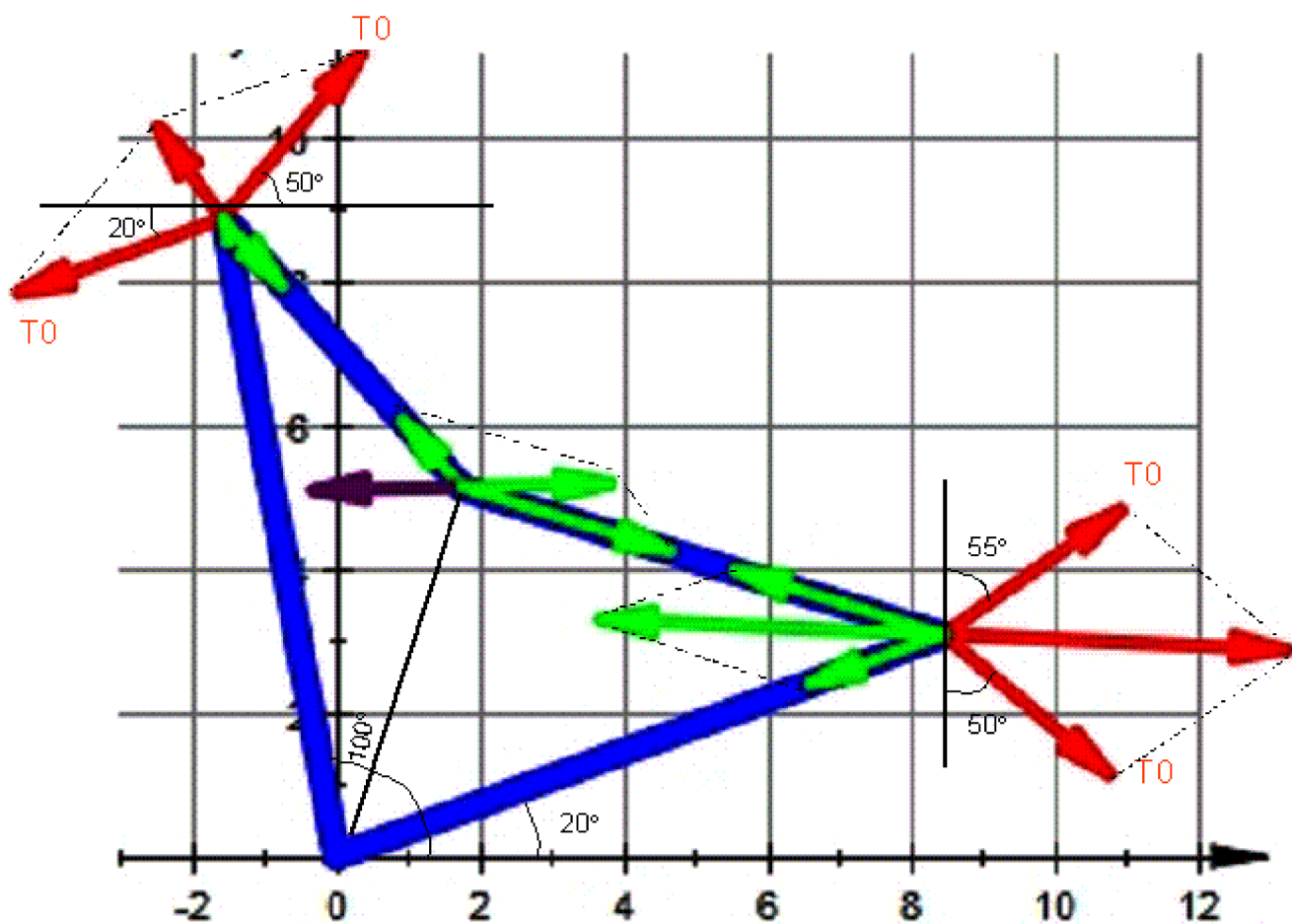
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+T3*iexp(theta7+phi2-PI)):
mycolor:=RGB::Violet:
ATS:=arr(L1*iexp(theta6)+L2*iexp(theta6+phi1),
L1*iexp(theta6)+L2*iexp(theta6+phi1)-T2*iexp(theta6+phi1-PI)
-T3*iexp(theta7+phi2-PI)):
plot([B1,B2,B3,B4,AT02,AT03,AT04,AT05,AT0304,AT0405,
AT1,AT2,AT3,AT4,AT34, AT2A,AT3A,ATS,ATSOpp],
Scaling=Constrained,ViewingBoxXRange =-3..12,
XGridVisible,YGridVisible)

```



Above result was transferred to powerpoint to add annotations,
and then cut/pasted below:



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[
[
[