

Table 2-9. Room Temperature Physical Properties, Annealed Condition

Type	Initial Modulus of Elasticity		Density		Thermal Conductivity at 68 F (20 C)		Specific Thermal Capacity at 68 F (20 C)	
	ksi	MPa	lb/ft ³	kg/m ³	BTU/(hr-ft- F)	W/(m-K)	BTU/(lb- F)	J/(kg-K)
S30400 S30403	28,000	193,000	490	7900	8.7	15	0.12	500
S31600 S31603	28,000	193,000	500	8000				
S32101 S32304 S32205	29,000	200,000	485	7800				
S17400	28,500	197,000	485	7800	9.2	16		

Note:

The data are taken from EN 10088, *Stainless Steels—Part 1: List of Stainless Steels* (CEN, 2005d) apart from the values for the initial modulus of elasticity which are taken from *Boiler and Pressure Vessel Code, Section II: Materials—Part D: Properties (Customary)* (ASME, 2010), with the value for the austenitic stainless steels rounded down to 28,000 ksi (193,000 MPa).

Poisson's ratio can be taken as 0.3 and the shear modulus of elasticity, *G*, as 0.385*E*.

LRFD	ASD
$\phi_c = 0.90$	$\Omega_c = 1.67$
$\phi_c P_n = 0.90(130 \text{ kips})$	$\frac{P_n}{\Omega_c} = \frac{130 \text{ kips}}{1.67}$
$= 117 \text{ kips}$	$= 77.8 \text{ kips}$

Example 3—W-Shape Subject to Compression and Bi-Axial Bending

Given:

Determine if a 9-ft-long **W6×16**, laser fused, Type S31600 stainless steel section in a symmetric braced frame has sufficient strength to support the following required strengths:

LRFD	ASD
$P_u = 7.00 \text{ kips}$	$P_a = 4.70 \text{ kips}$
$M_{ux} = 3.00 \text{ kip-ft}$	$M_{ax} = 2.00 \text{ kip-ft}$
$M_{uy} = 3.00 \text{ kip-ft}$	$M_{ay} = 2.00 \text{ kip-ft}$

Assume the column has adequate restraint to prevent lateral-torsional buckling.

Solution:

From Table 2-2 and Table 2-9, the material properties are as follows:

Type S31600 stainless steel

$F_y = 30 \text{ ksi}$

$E = 28,000 \text{ ksi}$

From AISC *Manual* Table 1-1 (AISC, 2010d), the geometric properties are as follows (assume these values are conservative for a laser-fused section):

W6×16

$A = 4.74 \text{ in.}^2$

$I_x = 32.1 \text{ in.}^4$

$I_y = 4.43 \text{ in.}^4$

$Z_x = 11.7 \text{ in.}^3$

$Z_y = 3.39 \text{ in.}^3$

$S_y = 2.20 \text{ in.}^3$

$r_x = 2.60 \text{ in.}$

$r_y = 0.967 \text{ in.}$

$b_f = 4.03 \text{ in.}$

$t_f = 0.405 \text{ in.}$

$t_w = 0.260 \text{ in.}$

$d = 6.28 \text{ in.}$

$h_o = 5.88 \text{ in.}$

$\frac{h}{t_w} = 19.1$

$\frac{b_f}{2t_f} = 4.98$

Check element slenderness

From Table 3-2, for a rolled I-shaped section subject to major or minor axis bending, an unstiffened compression element, such as the flanges, may be considered compact if:

$$\begin{aligned}\frac{b}{t} &\leq 0.33 \sqrt{\frac{E}{F_y}} \\ &\leq 0.33 \sqrt{\frac{28,000 \text{ ksi}}{30 \text{ ksi}}} \\ &\leq 10.1 \\ \frac{b}{t} = \frac{b_f}{2t_f} &= 4.98 \leq 10.1, \text{ therefore the flange is compact.}\end{aligned}$$

The web of a I-shaped section is considered compact if:

$$\begin{aligned}\frac{h}{t_w} &\leq 2.54 \sqrt{\frac{E}{F_y}} \\ &\leq 2.54 \sqrt{\frac{28,000 \text{ ksi}}{30 \text{ ksi}}} \\ &\leq 77.6 \\ \frac{h}{t_w} &= 19.1 \leq 77.6, \text{ therefore, the web is compact.}\end{aligned}$$

For a stiffened element, the more stringent limit of a stiffened element subject to a compression load (Table 3-1) governs over the limit of a stiffened element subject to flexure (Table 3-2):

$$\begin{aligned}\frac{h}{t_w} &\leq 1.24 \sqrt{\frac{E}{F_y}} \\ &\leq 1.24 \sqrt{\frac{28,000 \text{ ksi}}{30 \text{ ksi}}} \\ &\leq 37.9 \\ \frac{h}{t_w} &\leq 37.9 \text{ therefore the section is nonslender under axial compression}\end{aligned}$$

Determine the available compressive strength

From AISC *Specification* Commentary Table C-A-7.1, for a pinned-pinned condition, $K = 1.0$; therefore, the slenderness ratio is:

$$\begin{aligned}\frac{KL}{r} &= \frac{(1.0)(9.00 \text{ ft})(12 \text{ in./ft})}{0.967 \text{ in.}} \\ &= 112\end{aligned}$$

Determine the applicable equation for critical stress, F_{cr} , from Section 5.3 as follows:

$$\begin{aligned}3.77 \sqrt{\frac{E}{F_y}} &= 3.77 \sqrt{\frac{28,000 \text{ ksi}}{30 \text{ ksi}}} \\ &= 115 > 112, \text{ therefore modified AISC } Specification \text{ Equation E3-2 from Section 5.3 applies} \\ F_c &= \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2} \quad (\text{Spec. Eq. E3-4})\end{aligned}$$

$$= \frac{\pi^2 (28,000 \text{ ksi})}{(112)^2}$$

$$= 22.0 \text{ ksi}$$

$$F_{cr} = \left(0.50 \frac{F_e}{F_y} \right) F_y \quad (\text{modified Spec. Eq. E3-2})$$

$$= \left(0.50 \frac{30 \text{ ksi}}{22.0 \text{ ksi}} \right) (30 \text{ ksi})$$

$$= 11.7 \text{ ksi}$$

The nominal compressive strength is:

$$P_n = F_{cr} A_g \quad (\text{Spec. Eq. E3-1})$$

$$= 11.7 \text{ ksi} (4.74 \text{ in.}^2)$$

$$= 55.5 \text{ kips}$$

From Section 5.1, the available compressive strength is:

LRFD	ASD
$\phi_c P_n = 0.90(55.5 \text{ kips})$ $= 50.0 \text{ kips}$	$\frac{P_n}{\Omega_c} = \frac{55.5 \text{ kips}}{1.67}$ $= 33.2 \text{ kips}$

Determine the available flexural strength

For a compact section bent about the major axis, the limit states of yielding and lateral-torsional buckling apply. This member was said to have adequate restraint to prevent lateral-torsional buckling; therefore the limit state of yielding will control. As discussed in Section 6.2, the AISC *Specification* Section F2 applies to stainless steel, where the nominal flexural strength for yielding is defined as follows:

$$M_{ux} = M_p \quad (\text{Spec. Eq. F2-1})$$

$$= F_y Z_x$$

$$= (30 \text{ ksi})(11.7 \text{ in.}^3) / (12 \text{ in./ft})$$

$$= 29.3 \text{ kip-ft}$$

From Section 6.1, the available flexural strength about the major axis is:

LRFD	ASD
$\phi_b M_{ux} = 0.90(29.3 \text{ kip-ft})$ $= 26.4 \text{ kip-ft}$	$\frac{M_{ux}}{\Omega_b} = \frac{29.3 \text{ kip-ft}}{1.67}$ $= 17.5 \text{ kip-ft}$

As discussed in Section 6.2, the AISC *Specification* Section F6 applies to stainless steel I-shaped members bent about their minor axis and the limit states of yielding and flange local buckling apply; however, for sections with compact flanges the limit state of flange local buckling does not apply. The limit state of yielding will control:

$$\begin{aligned}
 M_{uy} &= F_y Z_y \leq 1.6 F_y S_y && \text{(Spec. Eq. F6-1)} \\
 &= (30 \text{ ksi})(3.39 \text{ in.}^3)/(12 \text{ in./ft}) \\
 &= 8.48 \text{ kip-ft} \\
 1.6 F_y S_y &= 1.6(30 \text{ ksi})(2.20 \text{ in.}^3)/(12 \text{ in./ft}) \\
 &= 8.80 \text{ kip-ft}
 \end{aligned}$$

Therefore, $M_{uy} = 8.48 \text{ kip-ft}$.

From Section 6.1, the available flexural strength about the minor axis is:

LRFD	ASD
$\phi_b M_{uy} = 0.90(8.48 \text{ kip-ft})$ $= 7.63 \text{ kip-ft}$	$\frac{M_{uy}}{\Omega_b} = \frac{8.48 \text{ kip-ft}}{1.67}$ $= 5.08 \text{ kip-ft}$

As discussed in Section 8.1.1, for doubly symmetric members subject to flexure and compression, the guidance in AISC *Specification* Section H1.1 applies. Determine whether AISC *Specification* Equation H1-1a or Equation H1-1b is applicable in this example:

LRFD	ASD
$\frac{P_r}{P_c} = \frac{P_u}{\phi_c P_n}$ $= \frac{7.00 \text{ kips}}{50.0 \text{ kips}}$ $= 0.140 < 0.2$	$\frac{P_r}{P_c} = \frac{P_u}{P_n / \Omega_c}$ $= \frac{4.70 \text{ kips}}{33.2 \text{ kips}}$ $= 0.142 < 0.2$

From AISC *Specification* Section H1, check the applicable interaction Equation H1-1b, as follows:

LRFD	ASD
$\frac{P_u}{2(\phi_c P_n)} + \left(\frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 1.0$ $\frac{7.00 \text{ kips}}{2(50.0 \text{ kips})} + \left(\frac{3.00 \text{ kip-ft}}{26.4 \text{ kip-ft}} + \frac{3.00 \text{ kip-ft}}{7.63 \text{ kip-ft}} \right) \leq 1.0$ $0.577 < 1.0 \quad \text{o.k.}$	$\frac{P_u}{2(P_n / \Omega_c)} + \left(\frac{M_{ux}}{M_{nx} / \Omega_b} + \frac{M_{uy}}{M_{ny} / \Omega_b} \right) \leq 1.0$ $\frac{4.70 \text{ kips}}{2(33.2 \text{ kips})} + \left(\frac{2.00 \text{ kip-ft}}{17.5 \text{ kip-ft}} + \frac{2.00 \text{ kip-ft}}{5.08 \text{ kip-ft}} \right) \leq 1.0$ $0.579 < 1.0 \quad \text{o.k.}$

Therefore, the W6×16 is adequate.

Example 4—Channel Subject to Strong-Axis Bending

Given:

Determine the available flexural and shear strength of a C12×30 Type S30400 stainless steel beam with a simple span of 30 ft. Also, determine the deflection at midspan due to an unfactored dead load of 5 kips applied at the midpoint. The beam is laterally restrained at its midpoint. The self-weight of the beam will be ignored for the purposes of this calculation.

Solution:

From Table 2-2 and Table 2-9, the material properties are as follows:

Type S31600 stainless steel