

Mechanical equivalents of electricity

$$\text{mass} := \text{kg}$$

$$\text{velocity} := \frac{\text{m}}{\text{sec}}$$

$$E := \text{mass} \cdot \text{velocity}^2 \quad \text{Einstein's definition of energy (E=mc}^2\text{)}$$

$$E = 1 \text{ J} \quad \text{kg} \cdot \left(\frac{\text{m}}{\text{sec}} \right)^2 = 1 \text{ J}$$

$$\frac{E}{\text{sec}} = 1 \text{ W} \quad \text{Time rate of change of energy is power}$$

$$\frac{\text{kg}}{\text{sec}} \cdot \left(\frac{\text{m}}{\text{sec}} \right)^2 = 1 \text{ W} \quad \text{Equivalent power calculations, thus}$$

$$\text{ohm amp}^2 = 1 \text{ W}$$

$$\frac{\text{kg} \cdot \text{m}^2}{\text{sec}^3} = 1 \text{ W}$$

Mechanical to
Electrical
Conversion factors

$$R := \frac{\text{kg}}{\text{sec}}$$

mechanical equivalent of resistance

$$K_R := \text{ohm} \cdot \frac{\text{sec}}{\text{kg}}$$

$$I := \frac{\text{m}}{\text{sec}}$$

velocity is the mechanical equivalent of current

$$K_I := \text{amp} \cdot \frac{\text{sec}}{\text{m}}$$

$$I^2 \cdot R = 1 \text{ W}$$

$$V := \sqrt{I^2 \cdot R \cdot R} \quad \text{the power equation can be manipulated to get voltage}$$

$$V = 1 \text{ N}$$

$$V := \frac{\text{kg} \cdot \text{m}}{\text{sec}^2}$$

thus force is equivalent to voltage

$$K_V := \text{volt} \cdot \frac{\text{sec}^2}{\text{kg} \cdot \text{m}}$$

$$C := \frac{I}{\left(\frac{V}{\text{sec}} \right)}$$

$$C = 1 \frac{\text{s}^2}{\text{kg}}$$

Use $i = Cdv/dt$ to calculate the mechanical equivalent of capacitance

$$K_C := \text{farad} \cdot \frac{\text{kg}}{\text{s}^2}$$

$$L := \frac{V}{\left(\frac{I}{\text{sec}} \right)}$$

$$L = 1 \text{ kg}$$

Use $V = Ldi/dt$ to calculate the mechanical equivalent of inductance.

$$K_L := \frac{\text{henry}}{\text{kg}}$$

$$\sqrt{L \cdot C} = 1 \text{ s}$$

sanity check. Good!

$$\sqrt{\frac{L}{C}} \cdot K_R = 1 \Omega$$

Characteristic impedance sanity check. Good!

"Interesting" conversions

Magnetic flux

$$\text{weber} = 1 \text{ Wb}$$

$$\text{volt} \cdot \text{sec} = 1 \text{ Wb}$$

$$\text{tesla} \cdot \text{m}^2 = 1 \text{ Wb}$$

$$\frac{\text{volt} \cdot \text{sec}}{\text{m}^2} = 1 \text{ T}$$

$$\text{coul} \cdot \text{ohm} = 1 \text{ Wb}$$

Magnetic field (B)

$$\text{tesla} = 1 \text{ T}$$

$$\frac{\text{newton}}{\text{amp} \cdot \text{m}} = 1 \text{ T}$$

$$\frac{\text{newton} \cdot \text{sec}}{\text{coul} \cdot \text{m}} = 1 \text{ T}$$

$$\text{tesla} = 1 \times 10^4 \text{ gauss}$$

Current (I)

$$\text{amp} = 1 \text{ A}$$

$$\frac{\text{coul}}{\text{sec}} = 1 \text{ A}$$

Inductance (H)

$$\text{volt} \cdot \frac{\text{sec}}{\text{amp}} = 1 \text{ H}$$

$$\frac{\text{Wb}}{\text{amp}} = 1 \text{ H}$$

Capacitance (F)

$$\text{amp} \cdot \frac{\text{sec}}{\text{volt}} = 1 \text{ F}$$

Voltage (V)

$$\text{volt} = 1 \text{ V}$$

$$\frac{\text{joule}}{\text{coul}} = 1 \text{ V}$$

$$\frac{\text{joule}}{\text{amp} \cdot \text{sec}} = 1 \text{ V}$$

$$\frac{\text{newton} \cdot \text{m}}{\text{amp} \cdot \text{sec}} = 1 \text{ V}$$

$$\text{tesla} \cdot \frac{1}{\text{sec}} \cdot \text{m}^2 = 1 \text{ V}$$

$$\text{tesla} \cdot \text{Hz} \cdot \text{m}^2 = 1 \text{ V}$$

Coulomb

$$\text{coul} = 1 \text{ C}$$

$$\text{amp} \cdot \text{sec} = 1 \text{ C}$$