

Formulas according to Honma; information found on the internet:

Quote -----

In Mike 11, we are able to choose between different weir formulas to calculate their downstream discharge. We used the weir formula 2 (formula of Honma). This method uses different equations according to flow type, that is, if there is free overflow or submerged flow conditions.

$$\left. \begin{aligned} Q &= w C h_1 \sqrt{h_1} && \text{for } \frac{h_2}{h_1} \leq 2/3: \\ Q &= w \frac{3}{2} \sqrt{3} C h_2 \sqrt{h_1 - h_2} && \text{for } \frac{h_2}{h_1} > 2/3: \end{aligned} \right|$$

Where, w stands for the width of the weir, h_1 the depth of water above weir level upstream, h_2 is the depth of the water above weir level downstream and C is the weir coefficient, which accounts for its resistance to the flow.

Unquote-----

$$\begin{aligned} \text{Formula of Honma for } \frac{h_2}{h_1} \leq \frac{2}{3}: & \quad Q = w * C * h_1 * \sqrt{h_1} \\ \text{Formula of Honma for } \frac{h_2}{h_1} > \frac{2}{3}: & \quad Q = w * \frac{3}{2} * \sqrt{3} * C * h_2 * \sqrt{(h_1 - h_2)} \\ \text{or} & \quad Q = 2,598 * w * C * h_2 * \sqrt{(h_1 - h_2)} \end{aligned}$$

$$h_1 - h_2 = \left(\frac{Q}{2,598 * w * C * h_2} \right)^2$$

Q = total flow
 h_1 = upstream depth above weir lip
 h_2 = downstream depth above weir lip
 w = weir width
 C = weir coefficient

Formula according to RCooper:

$$Q = 0,61 * w * h_2 * \sqrt{2 * g * (h_1 - h_2)}$$

$$h_1 - h_2 = \left(\frac{Q}{0,61 * w * h_2} \right)^2 * \frac{1}{2g}$$

Q = total flow
 h₁ = upstream depth above weir lip
 h₂ = downstream depth above weir lip
 w = weir width
 g = gravity = ~ 10

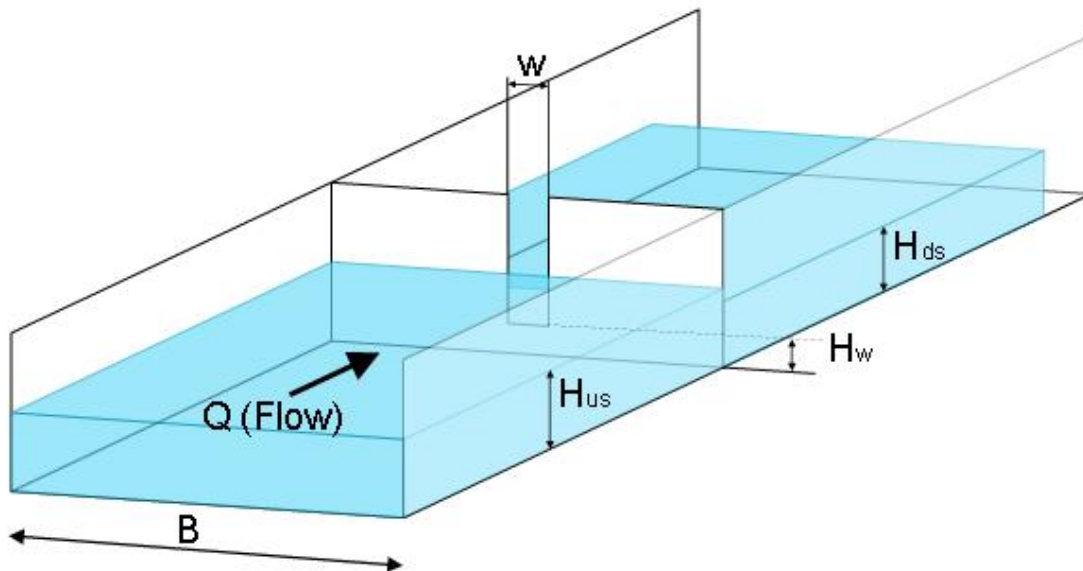
Formula sharp crested weir

$$Q = w * \frac{2}{3} * C * \sqrt{(2g * h^3)}$$

For a weir with the same width as the channel, C is approx 0,62. For a contracted weir (width of the weir less than width of the channel), C is approx 0,62 * (1 - 0,2 h/w).

This formula does not say anything about level H_{ds}.

Sample calculation



Q = 400 l/h = 0,4 m³/h = 0,000111 m³/sec
 B = channel width = 250 mm
 C = 0,6 (assumed, based on information found in literature)
 H_{us} = ???
 H_{ds} = 75 mm = 0,075 m
 H_w = 50 mm = 0,05 m

$$W = 50 \text{ mm} = 0,05 \text{ m}$$

$$h_1 = H_{us} - H_w$$

$$h_2 = H_{ds} - H_w = 25 \text{ mm} = 0,025 \text{ m}$$

Calculate with formula from Honma:

$$h_1 - h_2 = \left(\frac{Q}{2,598 * w * C * h_2} \right)^2$$

$$h_1 - h_2 = \left(\frac{0,000111}{2,598 * 0,05 * 0,6 * 0,025} \right)^2 = 0,0032678 \text{ m}$$

Calculate with formula from RCooper

$$h_1 - h_2 = \left(\frac{Q}{0,61 * w * h_2} \right)^2 * \frac{1}{2g}$$

$$h_1 - h_2 = \left(\frac{0,000111}{0,61 * 0,05 * 0,025} \right)^2 * \frac{1}{2 * 10} = 0,001059586 \text{ m}$$

So one formula gives approx. 3 mm, the other approx 1 mm. The latter seems to correspond better with what we observe in the model. You can barely see that there is a level drop.

RCooper bases his formula on the assumption that the dynamic head upstream and downstream of the weir are identical. As I see it, that means the velocity v is the same before and after the weir. But then, given that the width of the channel B and the flow Q are the same, H_{us} and H_{ds} should also be the same. That means no level drop.