

Orifice Plate Coefficient of Expansion for High dP Compressible Fluid Flow - refer Cunningham "Orifice Meters with Supercritical Compressible Flow - Transactions of the ASME - July 1951"

Air k 1.4
Experimental (Cunningham)

Beta Nom	Beta Act	K Calc	KY Exp			Y Exp			Y Fig 7		
1	0.63	0	1	0.63	0	1	0.63	0	1	0.63	0
0.15	0.1503	0.608212	0.5993			1	0.8916	0.671	1	0.8916	0.671
0.2	0.2035	0.608712	0.616	0.548	0.407	1.011973	0.900262	0.668625	1	0.89	0.664
0.3	0.3027	0.611484	0.616	0.548	0.407	1.007385	0.89618	0.665594	1	0.89	0.664
0.4	0.4047	0.619132	0.616	0.548	0.407	0.994941	0.88511	0.657372	1	0.89	0.664
0.5	0.5037	0.634714	0.634	0.562	0.413	0.998875	0.885438	0.650687	1	0.886	0.653
0.6	0.6119	0.666179	0.665	0.585	0.423	0.998229	0.878142	0.634964	1	0.88	0.638
0.7	0.7049	0.710461	0.719	0.624	0.445	1.012019	0.878303	0.626354	1	0.87	0.62
0.8	0.8071	0.784099	0.82	0.703	0.452	1.045786	0.88657	0.576458	1	0.86	0.56

using $K = 0.608 + 0.415 \times B^4$

Formula (Cunningham)

Beta Nom	Beta Act	Y			1	0.63	0	Y		
1	0.1503	$Y = 1.0 - (0.41 + 0.35 \times B^4) \times (1 - r) / k$			1	0.891596	0.671033	$Y = Y_{0.63} - 0.3501 \times (0.63 - r)$		
0.2	0.2				1	0.891495	0.661545	$Y = Y_{0.63} - 0.3650 \times (0.63 - r)$		
0.3	0.3				1	0.890894	0.660944	$Y = Y_{0.63} - 0.3650 \times (0.63 - r)$		
0.4	0.4				1	0.889275	0.659325	$Y = Y_{0.63} - 0.3650 \times (0.63 - r)$		

k 1.4
Calculated (D Kirk)

Beta Nom	Beta Act	1	0.63	0	1	0.63	0
0.1	0.1503	1	0.891596	0.670992	1	0.891596	0.670994
0.2	0.2035	1	0.891484	0.670637	1	0.891495	0.670671
0.3	0.3027	1	0.890866	0.668666	1	0.890894	0.668753
0.4	0.4047	1	0.889162	0.66323	1	0.889275	0.663591
0.5	0.5037	1	0.885689	0.652154	1	0.885862	0.652705
0.6	0.6119	1	0.878675	0.629786	1	0.879655	0.632911
0.7	0.7049	1	0.868805	0.598309	1	0.869434	0.600313
0.8	0.8071	1	0.852392	0.545964	1	0.853755	0.550311

Comparison of calculated and experimental values for Y

Total	0.999995	0.999989	0.999996	0.999999	0.999996	0.999999
	0.99025	1.003099	0.990262	1.003059	1.00168	1.010046
	0.99407	1.004616	0.994101	1.004747	1.001004	1.007159
	1.004578	1.008911	1.004706	1.009461	0.999185	0.999384
	1.000283	1.002254	1.000478	1.003102	0.999844	0.999549
	1.000607	0.991846	1.001723	0.996767	0.999608	0.992023
	0.989186	0.956225	0.989902	0.958425	0.999349	0.968247
	0.950725	0.947101	0.952245	0.954642	0.992738	0.982698
Average	99.12%	98.91%	99.17%	99.13%	99.92%	99.49%

Steam k 1.3
Experimental (Cunningham)

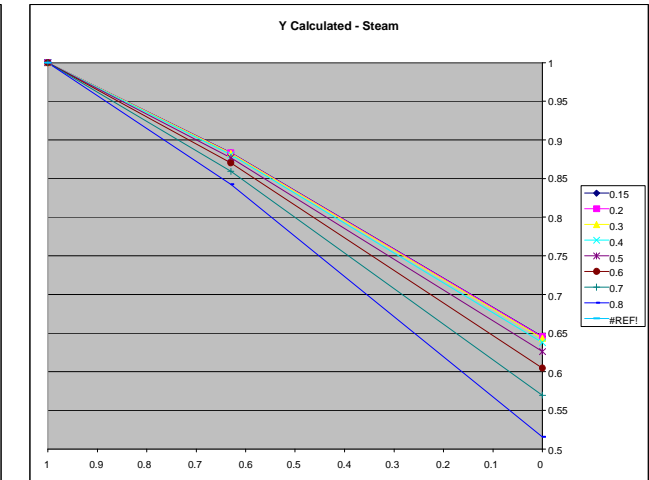
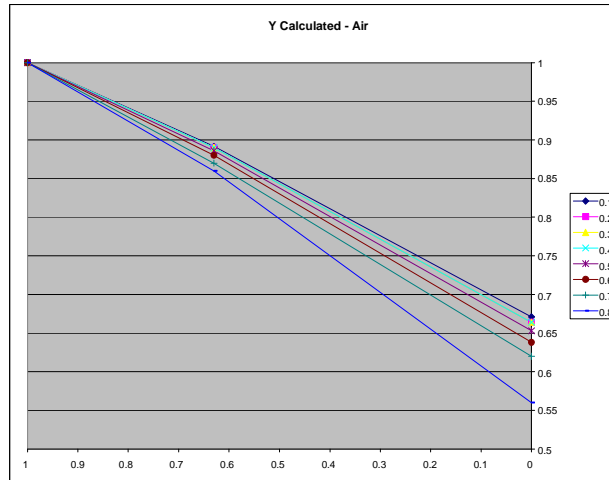
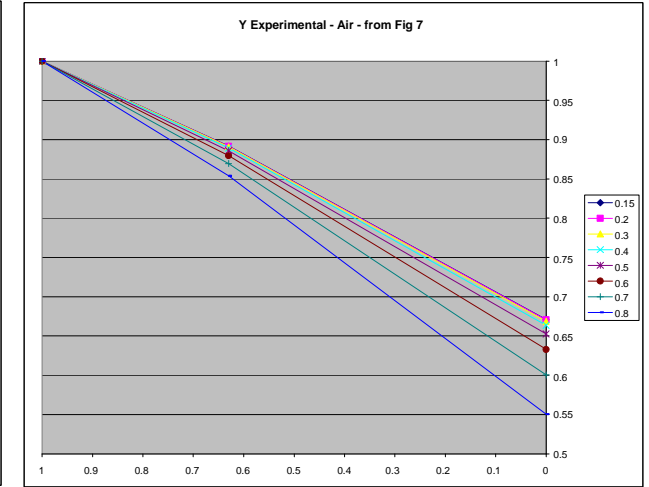
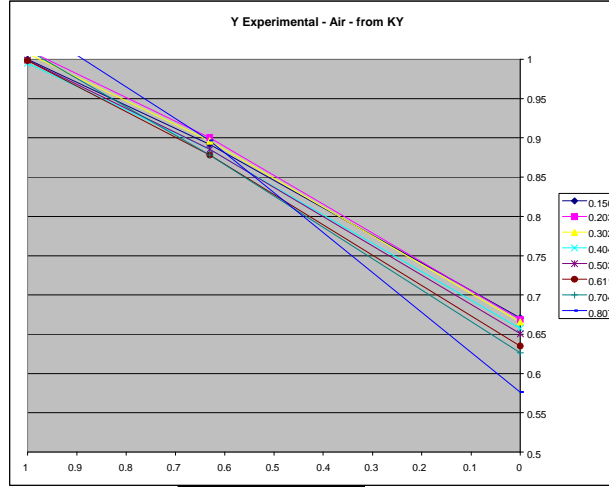
Beta Nom	Beta Act	1	0.63	0	Y Fig 4
1	0.1514	1	0.884	0.664	

Formula (Cunningham)

Beta Nom	Beta Act	1	0.63	0	Y
1	0.1514	1	0.891594	0.672354	$Y = Y_{0.63} - 0.3480 \times (0.63 - r)$

k 1.3
Calculated (D Kirk)

Beta Nom	Beta Act	1	0.63	0	1	0.63	0
0.15	0.1514	1	0.883255	0.645679	1	0.883257	0.645685
0.2	0.2035	1	0.883137	0.645301	1	0.883148	0.645338
0.3	0.3027	1	0.882471	0.643179	1	0.882501	0.643273
0.4	0.4047	1	0.880636	0.637324	1	0.880758	0.637713
0.5	0.5037	1	0.876895	0.625396	1	0.877082	0.62599
0.6	0.6119	1	0.869342	0.601308	1	0.870398	0.604673
0.7	0.7049	1	0.858713	0.56741	1	0.85939	0.569568
0.8	0.8071	1	0.841037	0.511038	1	0.842505	0.515719



$$Y = 1 - \left(0.41 + 0.35 \cdot \beta^4\right) \cdot \frac{\left(1 - \frac{P_2}{P_1}\right)}{k}$$

for $\frac{P_2}{P_1} > 0.63$

$$Y = Y_{0.63} - \left(0.49 + 0.45 \cdot \beta^4\right) \cdot \frac{\left(0.63 - \frac{P_2}{P_1}\right)}{k}$$

for $0.63 > \frac{P_2}{P_1} > 0$

- the ASME Formula is valid down to $P_2/P_1 = 0.63$

- $Y_{0.63}$ is Y from the ASME formula at $P_2/P_1 = 0.63$

- use this formula for $P_2/P_1 < 0.63$

