

N_m = Original RPM

P_m = Original HP

D_p = New diameter

D_m = Original diameter

Q_m = Original Flow

Q_p = New Flow

N_p = New RPM

P_p = New HP

1) Convert thrust into Q_m

$$F = m \times g$$

$$m = \dot{m} = (\rho_w \times Q_m)$$

$$Q = V = \frac{Q_m}{A}$$

$$A = \pi r^2$$

r = radius of Fin (Blade)

$$F = \frac{(\rho_w \times Q_m) \times Q_m}{\pi \times r^2}$$

$$\boxed{\begin{aligned} F &= \frac{\rho_w \times Q_m^2}{\pi \times r^2} \\ Q_m &= \sqrt{\frac{F(\pi \times r^2)}{\rho_w}} \end{aligned}}$$

2) Find Optimum speed associated with D_m & D_p

$$D_m = D_p$$

$$N_p = N_m \left(\frac{Q_p}{Q_m} \right) \left(\frac{D_m}{D_p} \right)^{3/4}$$

$$N_p = N_m \left(\frac{Q_p}{Q_m} \right)$$

Assume synchronous speed is less or equal to N_p
then

$$P_p = P_m \left(\frac{N_p}{N_m} \right)^3 \left(\frac{D_p}{D_m} \right)^5$$