

$$p1 := \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \quad p2 := \begin{bmatrix} 3 \\ 0 \\ 0 \end{bmatrix} \quad p3 := \begin{bmatrix} 0 \\ 0 \\ 3 \end{bmatrix} \quad pL := \begin{bmatrix} 3 \\ 0 \\ 3 \end{bmatrix}$$

$$F := \begin{bmatrix} 0 \\ 6 \\ 0 \end{bmatrix} \quad M := \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$pCG := \frac{p1 + p2 + p3}{3} \quad pCG = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$$

$$Mcg := M + (pL - pCG) \times F \quad Mcg = \begin{bmatrix} -12 \\ 0 \\ 12 \end{bmatrix}$$

$$\begin{aligned} FF1 &:= \frac{F}{3} & FF2 &:= \frac{F}{3} & FF3 &:= \frac{F}{3} \\ FF1 &= \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix} & FF2 &= \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix} & FF3 &= \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix} \end{aligned}$$

$$FM1\_x + FM2\_x + FM3\_x = 0$$

$$FM1\_y + FM2\_y + FM3\_y = 0$$

$$FM1\_z + FM2\_z + FM3\_z = 0$$

$$FM1\_z \cdot r1\_y - FM1\_y \cdot r1\_z + FM2\_z \cdot r2\_y - FM2\_y \cdot r2\_z + FM3\_z \cdot r3\_y - FM3\_y \cdot r3\_z = Mcg\_x$$

$$FM1\_x \cdot r1\_z - FM1\_z \cdot r1\_x + FM2\_x \cdot r2\_z - FM2\_z \cdot r2\_x + FM3\_x \cdot r3\_z - FM3\_z \cdot r3\_x = Mcg\_y$$

$$FM1\_y \cdot r1\_x - FM1\_x \cdot r1\_y + FM2\_y \cdot r2\_x - FM2\_x \cdot r2\_y + FM3\_y \cdot r3\_x - FM3\_x \cdot r3\_y = Mcg\_z$$

$$\begin{aligned} r1 &:= p1 - pCG & r2 &:= p2 - pCG & r3 &:= p3 - pCG & \text{sumsq} &:= (|r1|)^2 + (|r2|)^2 + (|r3|)^2 \\ r1 &= \begin{bmatrix} -1 \\ 0 \\ -1 \end{bmatrix} & r2 &= \begin{bmatrix} 2 \\ 0 \\ -1 \end{bmatrix} & r3 &= \begin{bmatrix} -1 \\ 0 \\ 2 \end{bmatrix} & \text{sumsq} &= 12 \end{aligned}$$

proportionality to the distance from point to CG in XZ plane

$$\text{sumsq\_xz} := r1\_x^2 + r1\_z^2 + r2\_x^2 + r2\_z^2 + r3\_x^2 + r3\_z^2 \quad \text{sumsq\_xz} = 12$$

$$FM1\_x\_xz := \frac{Mcg\_y \cdot r1\_z}{\text{sumsq\_xz}} \quad FM1\_x\_xz = 0 \quad FM1\_z\_xz := \frac{-Mcg\_y \cdot r1\_x}{\text{sumsq\_xz}} \quad FM1\_z\_xz = 0$$

$$FM2_{x_{xz}} := \frac{Mcg_{y_{r2\_z}}}{sumsq_{xz}} \quad FM2_{x_{xz}} = 0 \quad FM2_{z_{xz}} := \frac{-Mcg_{y_{r2\_x}}}{sumsq_{xz}} \quad FM2_{z_{xz}} = 0$$

$$FM3_{x_{xz}} := \frac{Mcg_{y_{r3\_z}}}{sumsq_{xz}} \quad FM3_{x_{xz}} = 0 \quad FM3_{z_{xz}} := \frac{-Mcg_{y_{r3\_x}}}{sumsq_{xz}} \quad FM3_{z_{xz}} = 0$$

proportionality to the distance from point to CG in XY plane

$$sumsq_{xy} := r1_{x^2} + r1_{y^2} + r2_{x^2} + r2_{y^2} + r3_{x^2} + r3_{y^2} \quad sumsq_{xy} = 6$$

$$FM1_{x_{xy}} := \frac{-Mcg_{z_{r1\_y}}}{sumsq_{xy}} \quad FM1_{x_{xy}} = 0 \quad FM1_{y_{xy}} := \frac{Mcg_{z_{r1\_x}}}{sumsq_{xy}} \quad FM1_{y_{xy}} = -2$$

$$FM2_{x_{xy}} := \frac{-Mcg_{z_{r2\_y}}}{sumsq_{xy}} \quad FM2_{x_{xy}} = 0 \quad FM2_{y_{xy}} := \frac{Mcg_{z_{r2\_x}}}{sumsq_{xy}} \quad FM2_{y_{xy}} = 4$$

$$FM3_{x_{xy}} := \frac{-Mcg_{z_{r3\_y}}}{sumsq_{xy}} \quad FM3_{x_{xy}} = 0 \quad FM3_{y_{xy}} := \frac{Mcg_{z_{r3\_x}}}{sumsq_{xy}} \quad FM3_{y_{xy}} = -2$$

proportionality to the distance from point to CG in YZ plane

$$sumsq_{yz} := r1_{y^2} + r1_{z^2} + r2_{y^2} + r2_{z^2} + r3_{y^2} + r3_{z^2} \quad sumsq_{yz} = 6$$

$$FM1_{y_{yz}} := \frac{-Mcg_{x_{r1\_z}}}{sumsq_{yz}} \quad FM1_{y_{yz}} = -2 \quad FM1_{z_{yz}} := \frac{Mcg_{x_{r1\_y}}}{sumsq_{yz}} \quad FM1_{z_{yz}} = 0$$

$$FM2_{y_{yz}} := \frac{-Mcg_{x_{r2\_z}}}{sumsq_{yz}} \quad FM2_{y_{yz}} = -2 \quad FM2_{z_{yz}} := \frac{Mcg_{x_{r2\_y}}}{sumsq_{yz}} \quad FM2_{z_{yz}} = 0$$

$$FM3_{y_{yz}} := \frac{-Mcg_{x_{r3\_z}}}{sumsq_{yz}} \quad FM3_{y_{yz}} = 4 \quad FM3_{z_{yz}} := \frac{Mcg_{x_{r3\_y}}}{sumsq_{yz}} \quad FM3_{z_{yz}} = 0$$

Adding it all up

$$FM1 := \begin{bmatrix} FM1_{x_{xz}} + FM1_{x_{xy}} \\ FM1_{y_{yz}} + FM1_{y_{xy}} \\ FM1_{z_{xz}} + FM1_{z_{yz}} \end{bmatrix} \quad FM2 := \begin{bmatrix} FM2_{x_{xz}} + FM2_{x_{xy}} \\ FM2_{y_{yz}} + FM2_{y_{xy}} \\ FM2_{z_{xz}} + FM2_{z_{yz}} \end{bmatrix} \quad FM3 := \begin{bmatrix} FM3_{x_{xz}} + FM3_{x_{xy}} \\ FM3_{y_{yz}} + FM3_{y_{xy}} \\ FM3_{z_{xz}} + FM3_{z_{yz}} \end{bmatrix}$$

$$FM1 = \begin{bmatrix} 0 \\ -4 \\ 0 \end{bmatrix} \quad FM2 = \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix} \quad FM3 = \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix}$$

$$FM1_{z_{r1\_y}} - FM1_{y_{r1\_z}} + FM2_{z_{r2\_y}} - FM2_{y_{r2\_z}} + FM3_{z_{r3\_y}} - FM3_{y_{r3\_z}} = -6$$

$$Mcg_x = -12$$

$$FM1_{x_{r1\_z}} - FM1_{z_{r1\_x}} + FM2_{x_{r2\_z}} - FM2_{z_{r2\_x}} + FM3_{x_{r3\_z}} - FM3_{z_{r3\_x}} = 0$$

$$Mcg_y = 0$$

$$FM1_{y_{r1\_x}} - FM1_{x_{r1\_y}} + FM2_{y_{r2\_x}} - FM2_{x_{r2\_y}} + FM3_{y_{r3\_x}} - FM3_{x_{r3\_y}} = 6$$

$$Mcg_z = 12$$