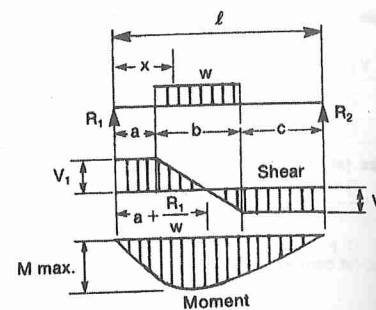


Table 1.14: (Continued)

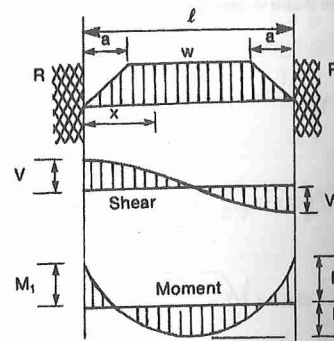
## Simple Beam — uniform load partially distributed

$$\begin{aligned}
 R_1 = V_1 \text{ (max. when } a < c) &= \frac{wb}{2l}(2c+b) \\
 R_2 = V_2 \text{ (max. when } a > c) &= \frac{wb}{2l}(2a+b) \\
 V_x \text{ (when } x > a \text{ and } < (a+b)) &= R_1 - w(x-a) \\
 M \text{ max. (at } x = a + \frac{R_1}{w}) &= R_1 \left( a + \frac{R_1}{2w} \right) \\
 M_x \text{ (when } x < a) &= R_1 x \\
 M_x \text{ (when } x > a \text{ and } < (a+b)) &= R_1 x - \frac{w}{2}(x-a)^2 \\
 M_x \text{ (when } x > (a+b)) &= R_2(l-x)
 \end{aligned}$$



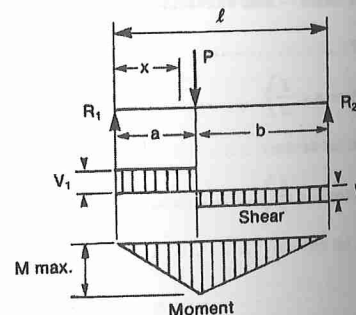
## Beam fixed at both ends — symmetrical trapezoidal load

$$\begin{aligned}
 R = V &= \frac{wl}{2} \left( 1 - \frac{a}{l} \right) \\
 M_1 &= -\frac{wl^2}{12} \left( 1 - 2\frac{a^2}{l^2} + \frac{a^3}{l^3} \right) \\
 M_2 &= \frac{wl^2}{24} \left( 1 - 2\frac{a^3}{l^3} \right) \\
 M_x \text{ (when } x < a) &= M_1 + R_1 x - \frac{wx^3}{6a} \\
 M_x \text{ (when } a < x < l-a) &= M_1 + R_1 x - \frac{wa}{2} \left( x - \frac{2}{3}a \right) - \frac{w}{2}(x-a)^2
 \end{aligned}$$

Note: When  $a = l/2$  loading is triangular

## Simple Beam — concentrated load at any point

$$\begin{aligned}
 R_1 = V_1 \text{ (max. when } a < b) &= \frac{Pb}{l} \\
 R_2 = V_2 \text{ (max. when } a > b) &= \frac{Pa}{l} \\
 M \text{ max. (at point of load)} &= \frac{Pab}{l} \\
 M_x \text{ (when } x < a) &= \frac{Pbx}{l} \\
 \Delta \text{ max. (at } x = \sqrt{\frac{a(a+2b)}{3}} \text{ when } a > b) &= \frac{Pab(a+2b)\sqrt{3a(a+2b)}}{27EI} \\
 \Delta a \text{ (at point of load)} &= \frac{Pa^2b^2}{3EI} \\
 \Delta_x \text{ (when } x < a) &= \frac{Pbx}{6EI} (l^2 - b^2 - x^2)
 \end{aligned}$$



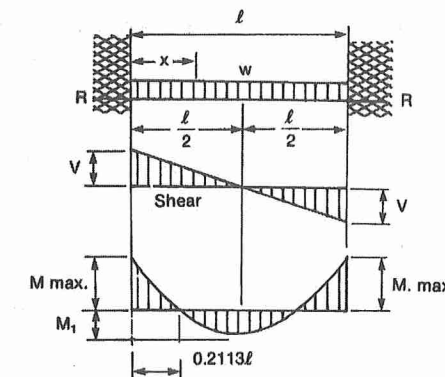
Note:

w: Distributed load per unit length. In the case of triangular distribution, w represents the maximum intensity of load per unit length.  
P: Concentrated load.

Table 1.14: (Continued)

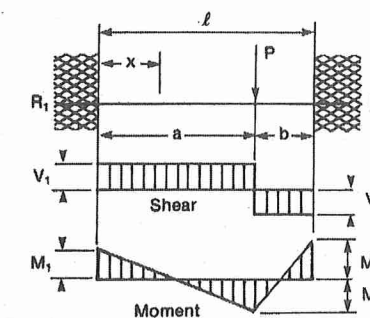
## Beam fixed at both ends — uniformly distributed loads

$$\begin{aligned}
 R = V &= \frac{wl}{2} \\
 V_x &= w \left( \frac{l}{2} - x \right) \\
 M \text{ max. (at ends)} &= -\frac{wl^2}{12} \\
 M_1 \text{ (at centre)} &= \frac{wl^2}{24} \\
 M_x &= \frac{w}{12} (6lx - l^2 - 6x^2) \\
 \Delta \text{ max. (at centre)} &= \frac{wl^4}{384EI} \\
 \Delta_x &= \frac{wx^2}{24EI} (l-x)^2
 \end{aligned}$$



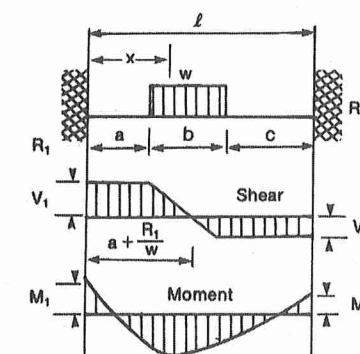
## Beam fixed at both ends — concentrated load at any point

$$\begin{aligned}
 R_1 = V_1 \text{ (max. when } a < b) &= \frac{Pb^2}{l^3} (3a+b) \\
 R_2 = V_2 \text{ (max. when } a > b) &= \frac{Pa^2}{l^3} (a+3b) \\
 M_1 \text{ (max. when } a < b) &= -\frac{Pab^2}{l^2} \\
 M_2 \text{ (max. when } a > b) &= -\frac{Pa^2b}{l^2} \\
 M_x \text{ (at point of load)} &= \frac{2Pa^2b^2}{l^3} \\
 M_x \text{ (when } x < a) &= R_1 x - \frac{Pab^2}{l^2} \\
 \Delta \text{ max. (when } a > b \text{ at } x = \frac{2al}{3a+b}) &= \frac{2Pa^3b^2}{3EI(3a+b)^2} \\
 \Delta_x \text{ (at point of load)} &= \frac{Pa^3b^3}{3EI} \\
 \Delta_x \text{ (when } x < a) &= \frac{Pb^2x^2}{6EI} (3al - 3ax - bx)
 \end{aligned}$$



## Beam fixed at both ends — uniform load partially distributed

$$\begin{aligned}
 M_1 &= -\frac{w}{12l^2} [(l-a)^3(l+3a) - c^3(4l-3c)] \\
 M_2 &= \frac{w}{12l^2} [(l-c)^3(l+3c) - a^3(4l-3a)] \\
 R_1 = V_1 &= \frac{1}{l} [M_1 - M_2 + wb \left( c + \frac{b}{2} \right)] \\
 R_2 = V_2 &= \frac{1}{l} [M_2 - M_1 + wb \left( a + \frac{b}{2} \right)] \\
 M_x \text{ (when } x < a) &= R_1 x - M_1 \\
 M_x \text{ (when } a < x < (a+c)) &= R_1 x - M_1 - \frac{w}{2}(x-a)^2 \\
 M_x \text{ (when } x > (a+c)) &= R_2(l-x) - M_2
 \end{aligned}$$



Note:

w: Distributed load per unit length. In the case of triangular distribution, w represents the maximum intensity of load per unit length.  
P: Concentrated load.