

# Shear in Reinforced Concrete Slabs under Concentrated Loads close to Supports

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# Overview

- Introduction
- Overview of experiments
  - Beams vs. slabs
- Modified Bond Model
- Code extension proposal
- Application to practice
- Conclusions



# Motivation (1)

Bridges from 60s and 70s



The Hague in 1959

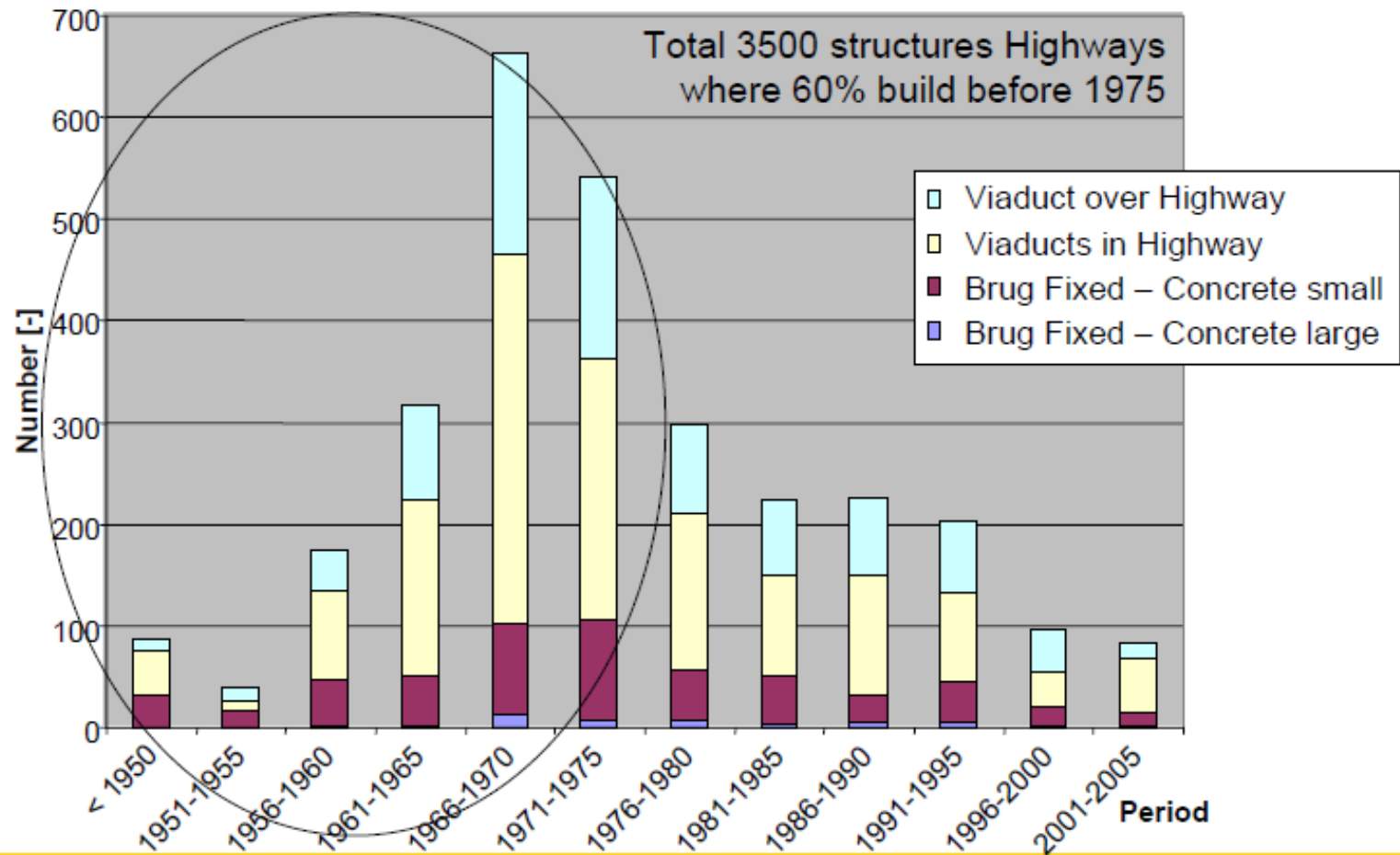
Increased live loads



heavy and long truck  
(600 kN > perm. max = 50ton)

End of service life + larger loads

## Motivation (2)



# Motivation (3)

- First checks since mid-2000s
  - 3715 structures to be studied
  - 600 slab bridges shear-critical
- But: checks according to design rules
- => Residual capacity???
- Hidden reserves of the bearing capacity



Highways in the Netherlands

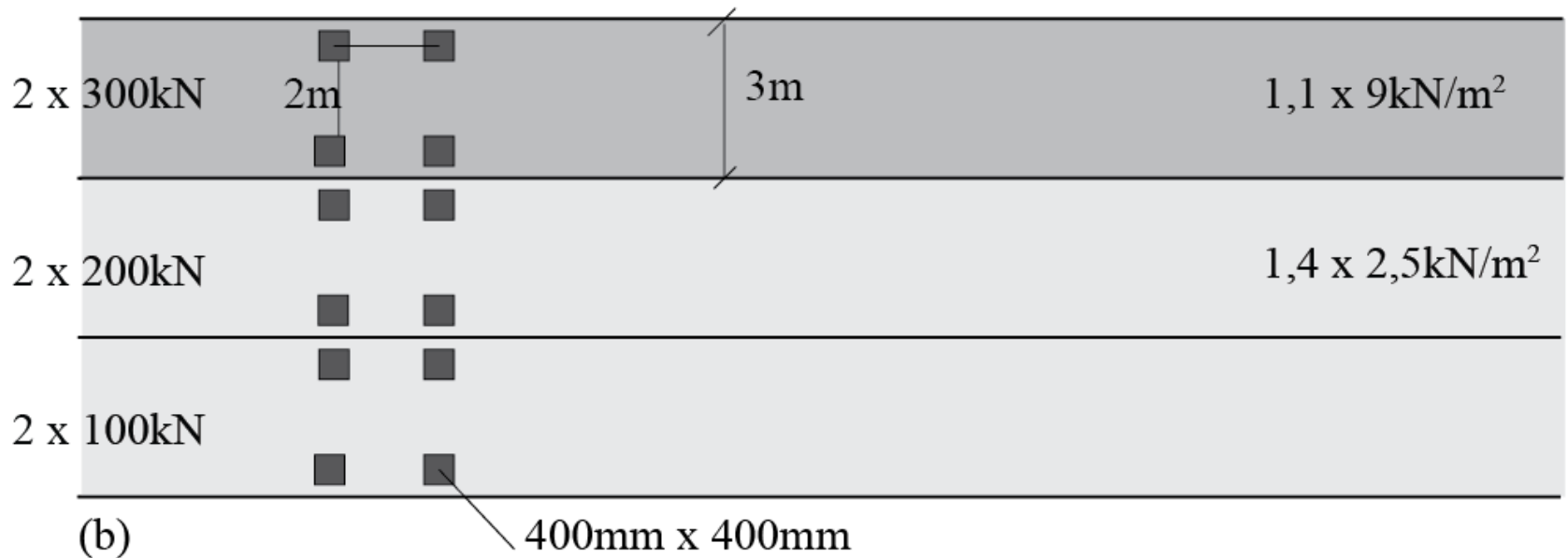
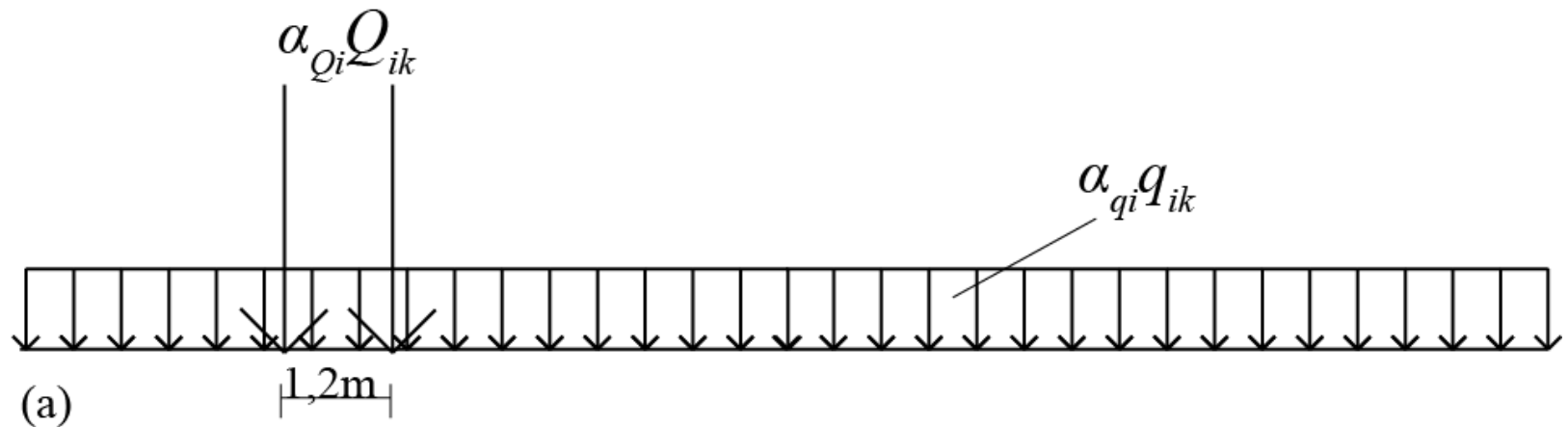
# Project description (1)

- Capacity of existing bridges
  - TU Delft
    - Concrete Structures
    - Structural Mechanics
  - TNO
  - RWS
- Concrete Structures
  - Long-term tensile strength
  - Beam shear – sustained loads
  - Continuous girders – shear
  - Prestressed slabs – punching
  - **Slab bridges - shear/punching**



Concrete bridges

# Live Loads in NEN-EN 1991-2:2003





# Shear Failure (1)



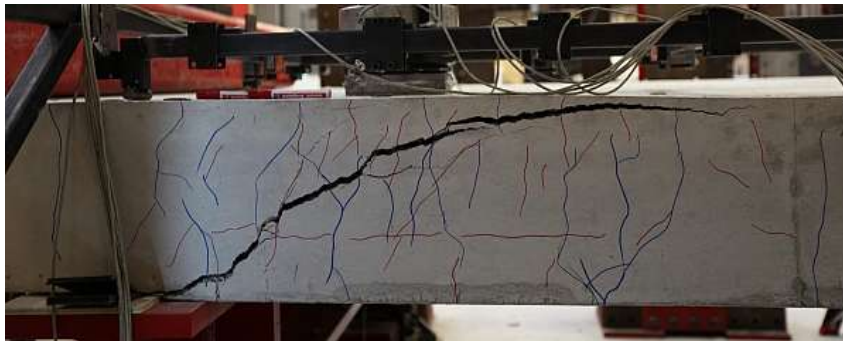
Shear failure of the de la Concorde bridge, Laval

Shear failures of bridges: rare but brittle failures



# Shear Failure (2)

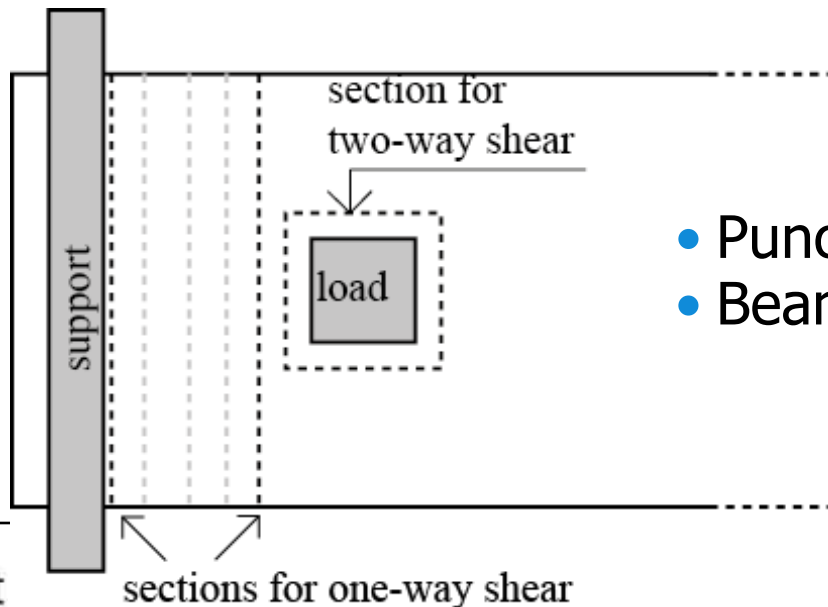
## Beam shear vs. Punching shear



Beam shear, one-way shear



Punching shear, two-way shear



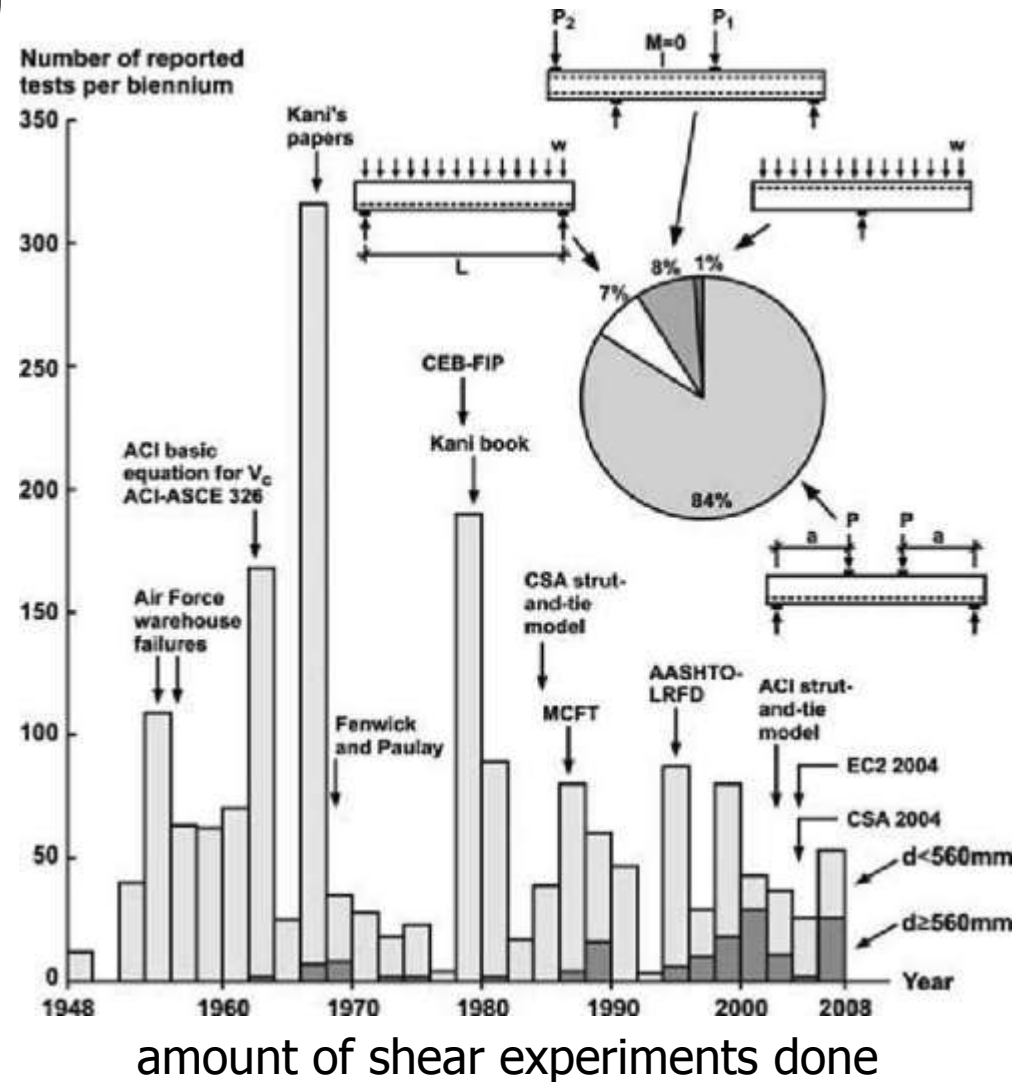
- Punching shear over perimeter
- Beam shear over (effective) width

concentrated loads close to supports

# Shear Failure (3)

## Beam shear

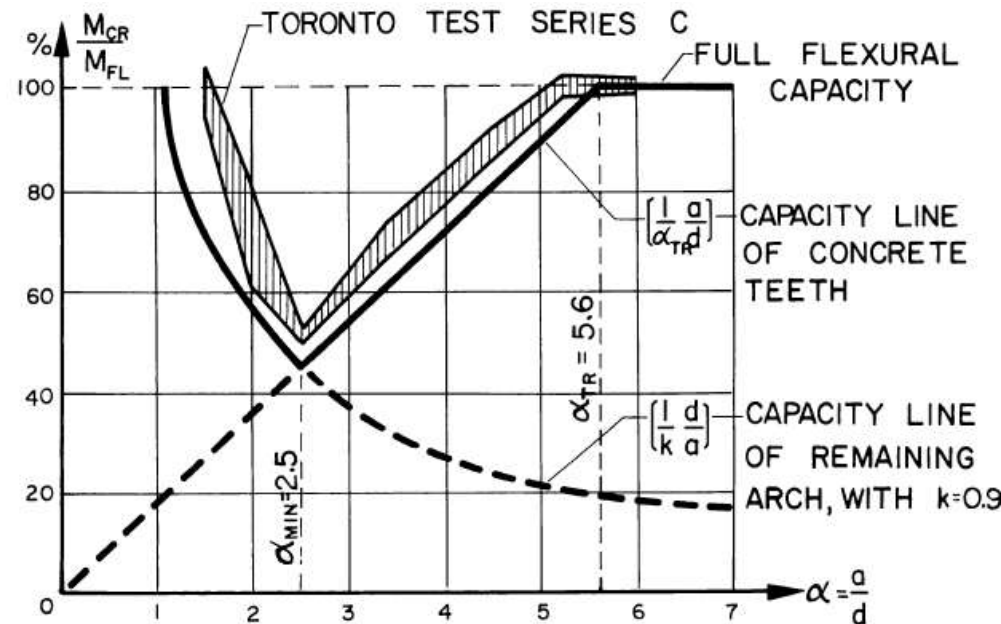
- Since 1899 (Ritter)
- 1955: collapse of warehouse
- Most experiments:
  - Beams
  - Heavily reinforced
  - Small size
  - Slender ( $a/d \geq 2,5$ )
- Basis for design codes



# Shear Failure (3)

## Beam shear

- Since 1899 (Ritter)
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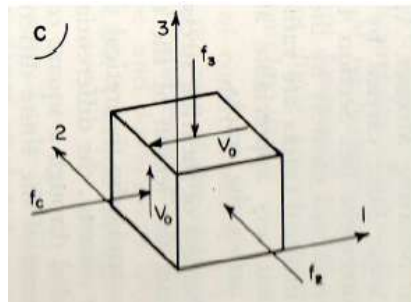


Influence of shear span

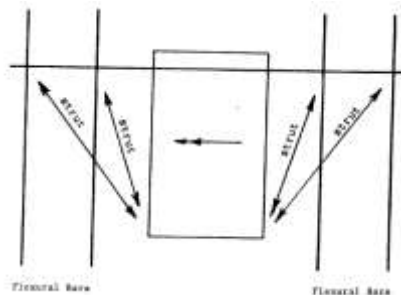
# Shear Failure (4)

## Punching shear

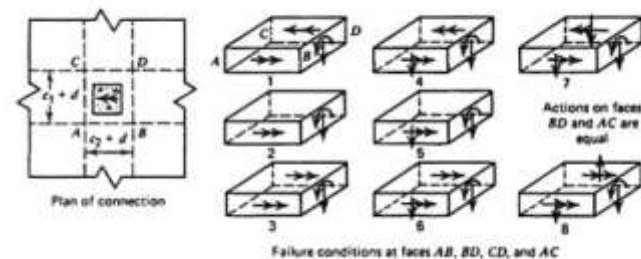
### Categories of methods for punching shear



Shear stress



Strut and tie



Beam analogy

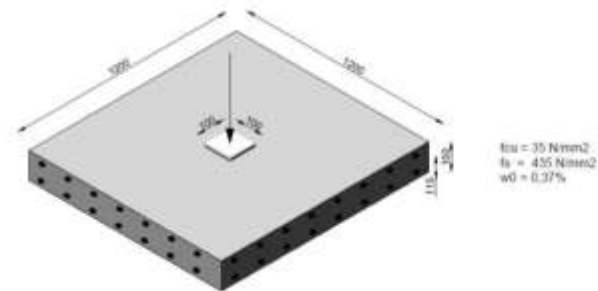


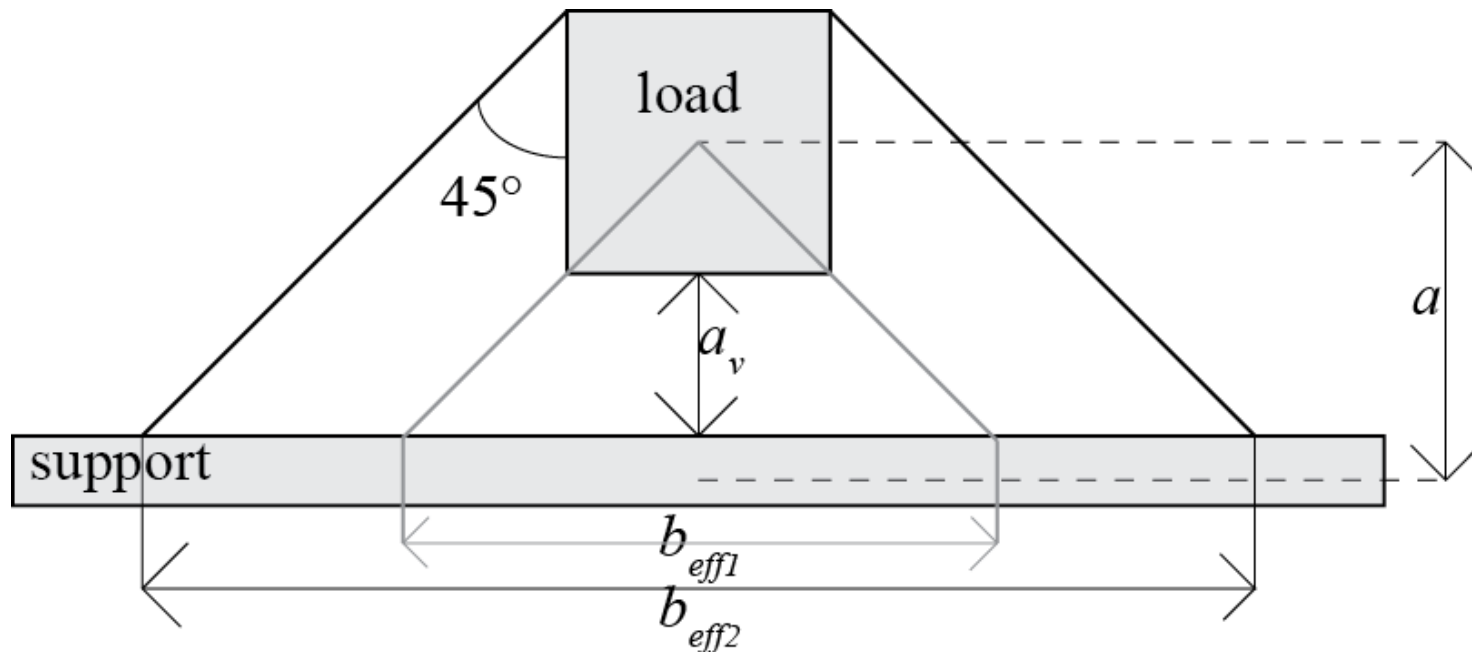
Plate theory / FEM

The nature of shear failure is still not fully understood!

- Transverse load redistribution
- Additional dimension in slabs
- Expected higher capacity than beams
- First experiments: Regan (1982)



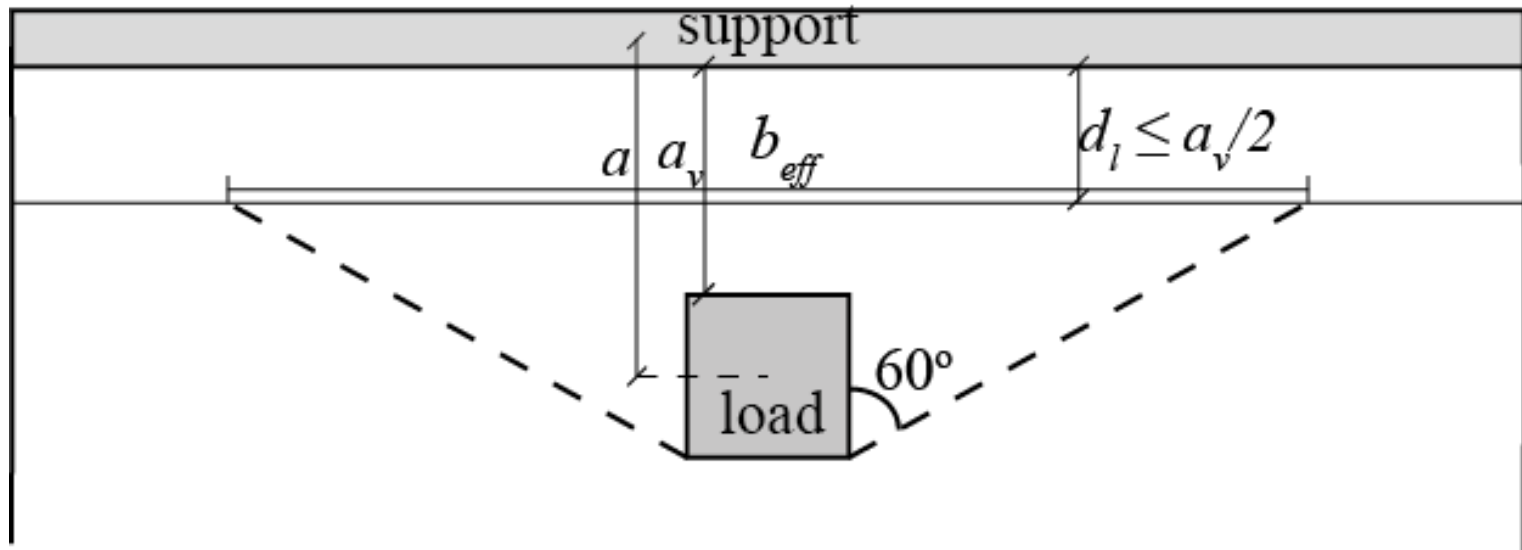
## Slabs under concentrated loads (2)



- Shear stress over effective width
- Fixed width, eg. 1 m
- Load spreading method



## Slabs under concentrated loads (2)



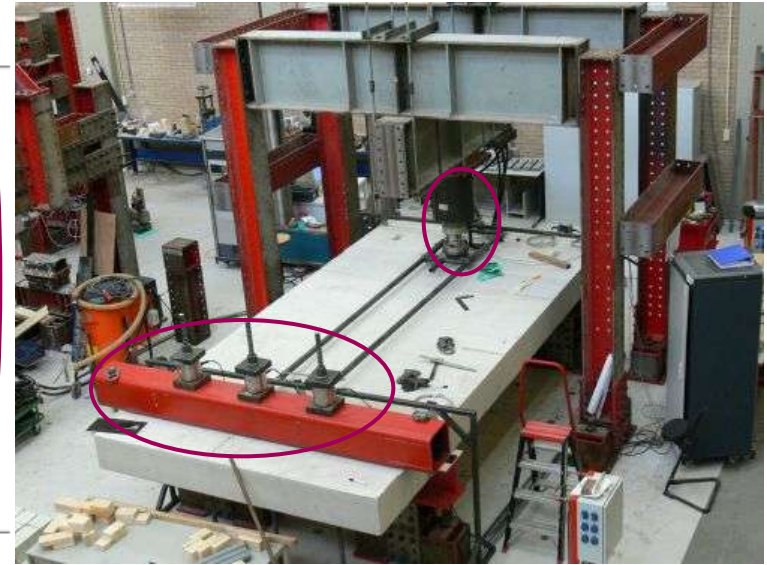
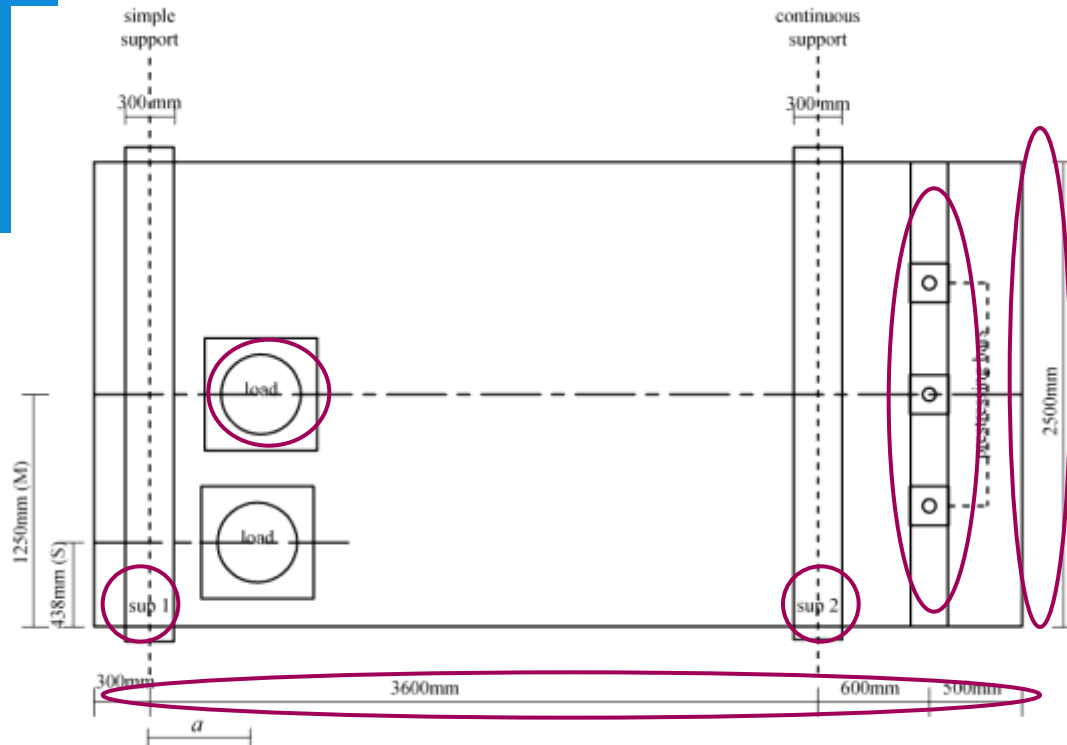
- Shear stress over effective width
- Fixed width, eg. 1 m
- Load spreading method

# Goals

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- *Assess shear capacity of slabs under concentrated loads*
  - *Determine effective width in shear*
-

# Experiments (1)



Size: 5m x 2,5m (variable) x 0,3m = scale 1:2

Continuous support, Line supports

Concentrated load: vary  $a/d$  and position along width

# Experiments (2)

- 2<sup>nd</sup> series experimental work:
  - Slabs under combined loading
  - Line load
    - Preloading
    - 50% of strength from slab strips
  - Concentrated load until failure
- Conclusions from 1<sup>st</sup> series valid when combining loads?
- 26 experiments, 8 slabs
- Overall: 156 experiments, 38 slabs



# Experiments (3)



(a)



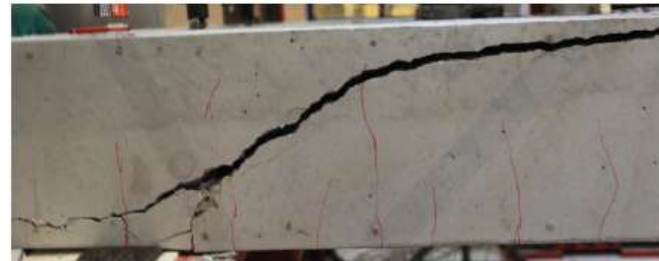
(b)



(c)



(d)

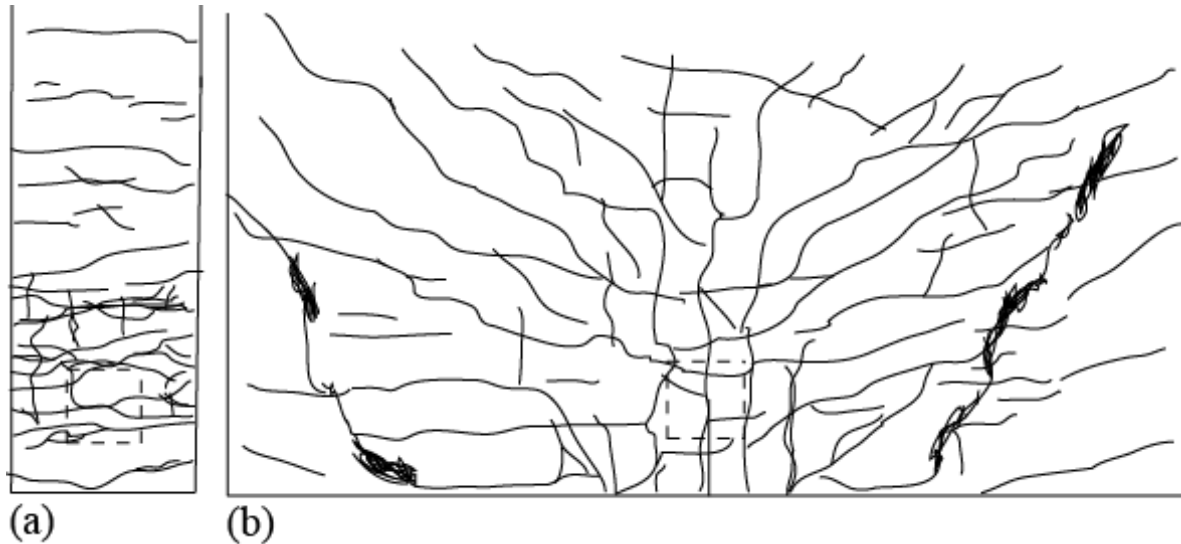


(e)



(f)

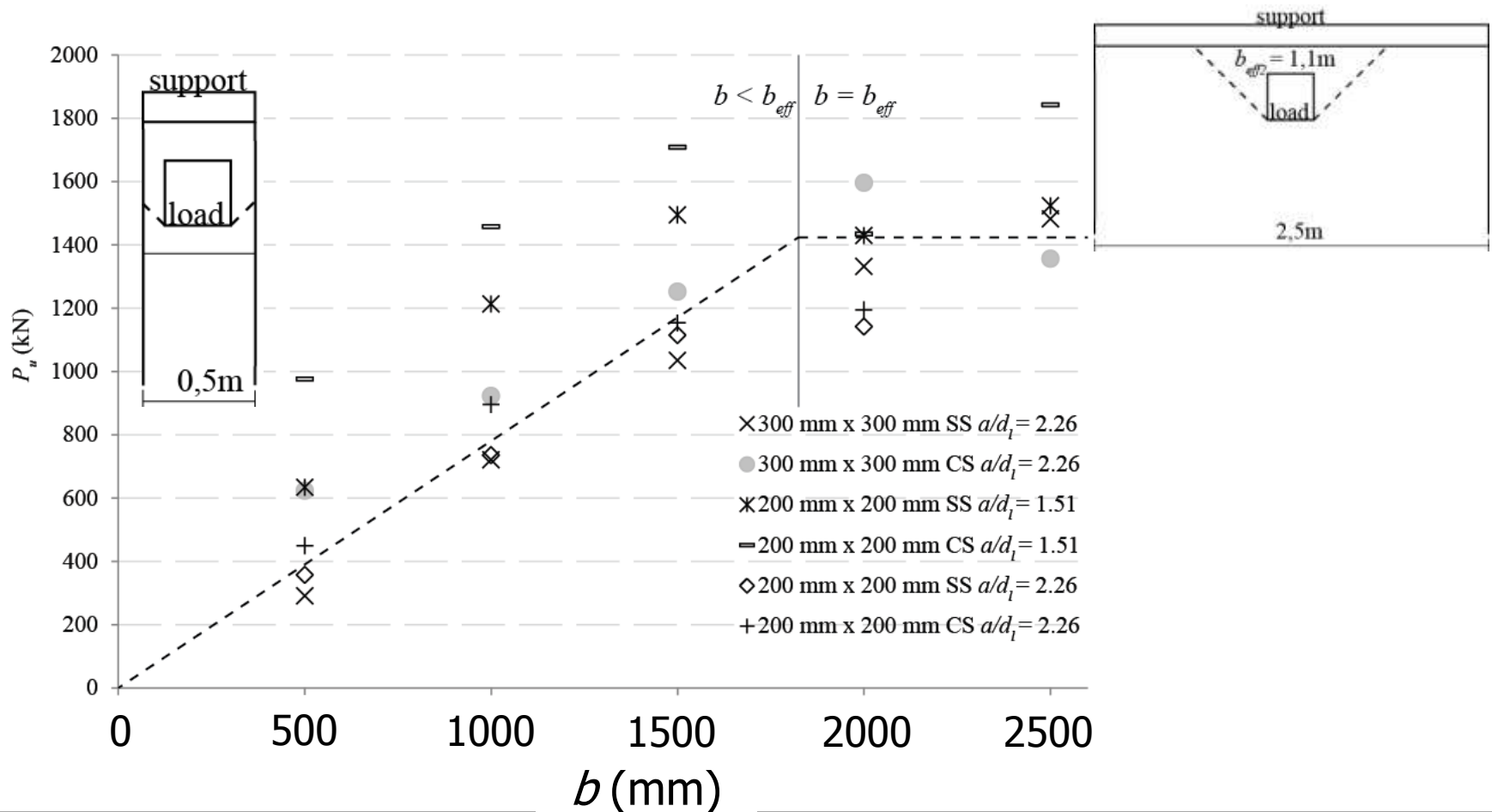
# Slabs vs. beams (1)



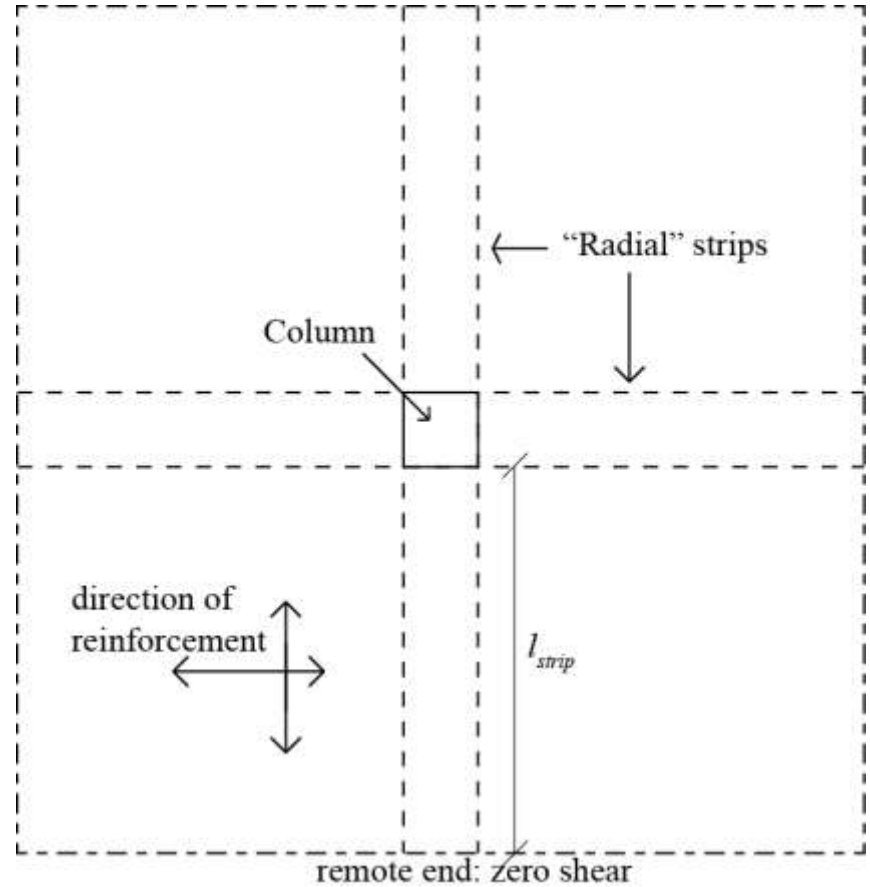
- Transverse load redistribution
- Geometry governing in slabs
- Location of load
  - result of different load-carrying paths
- Mid support vs end support
  - influence of transverse moment
- Wheel size
  - more 3D action



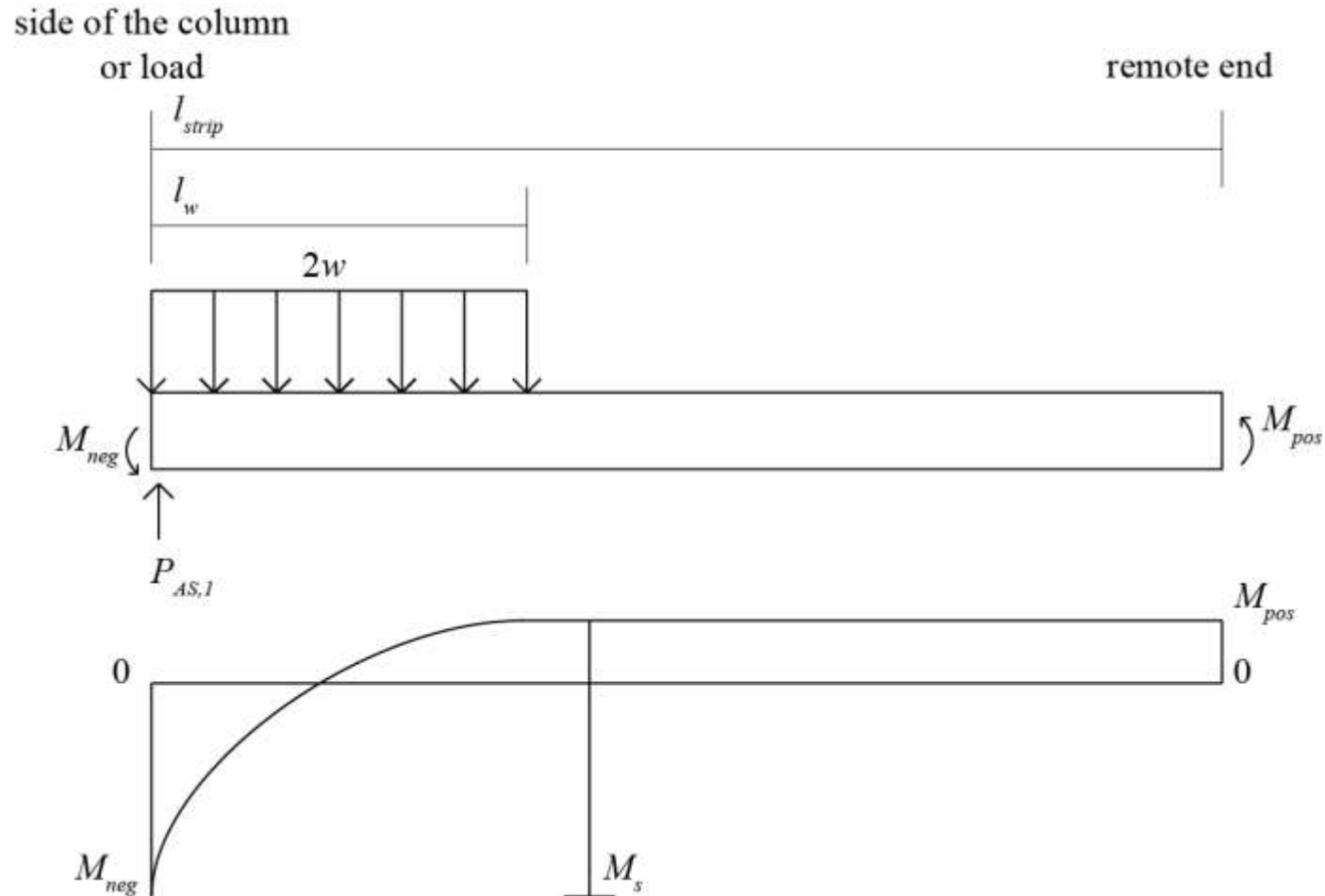
# Slabs vs. beams (2)



- Based on Bond Model (Alexander and Simmonds, 1990)
- For slabs with concentrated load in middle



# Modified Bond Model (2)

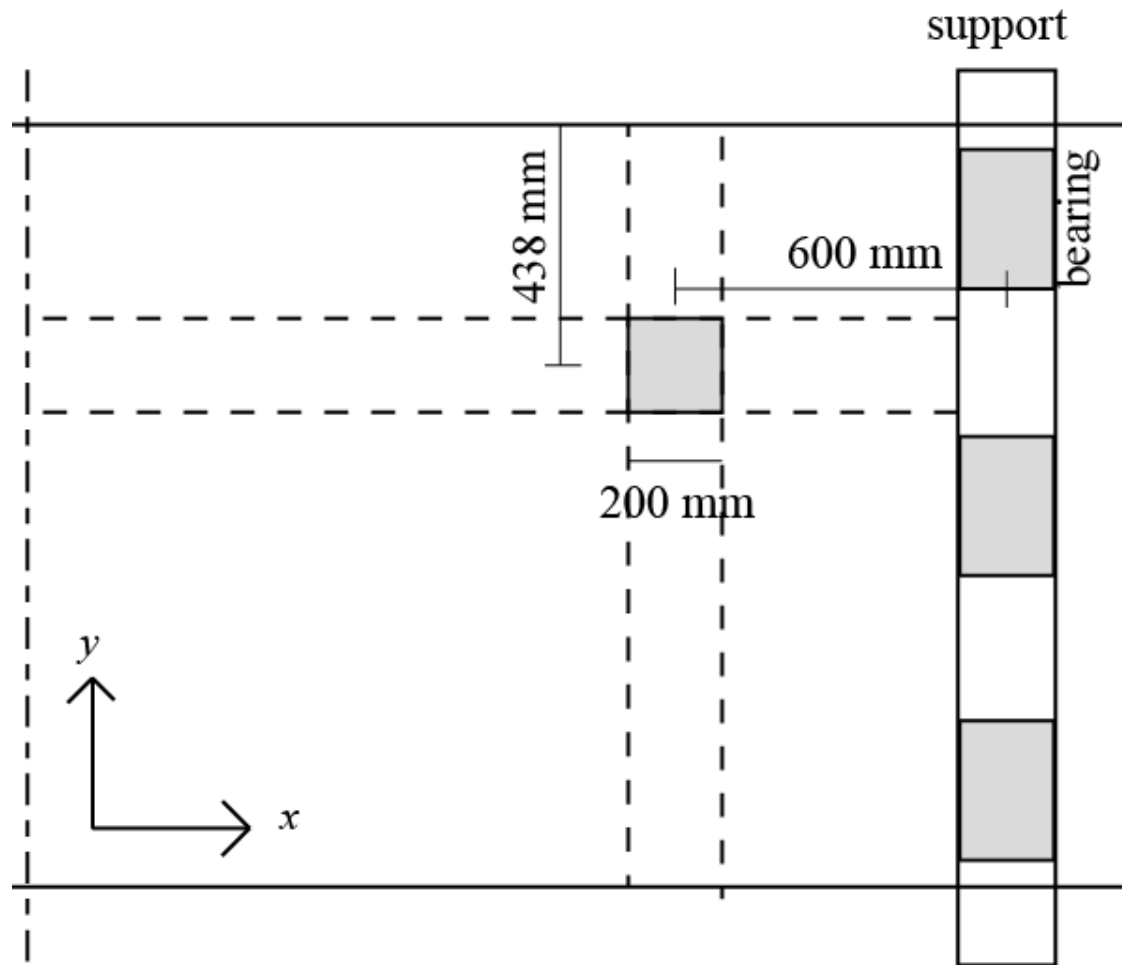


# Modified Bond Model (3)

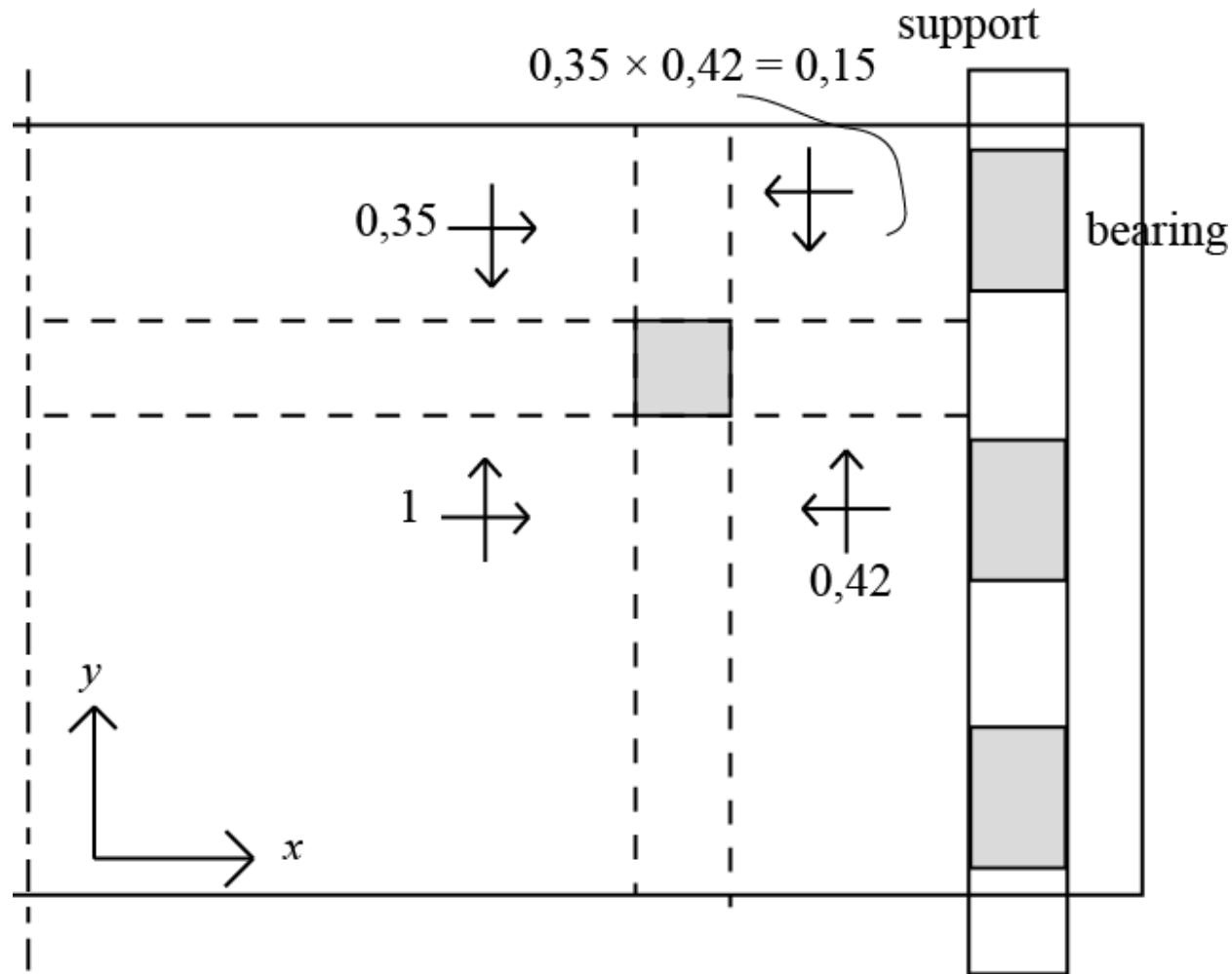
- Adapted for slabs with concentrated load close to support
- Geometry is governing as in experiments
- Determine factor that reduces capacity of “radial” strip
- Maximum load: based on sum capacity of 4 strips



# Modified Bond Model (4)

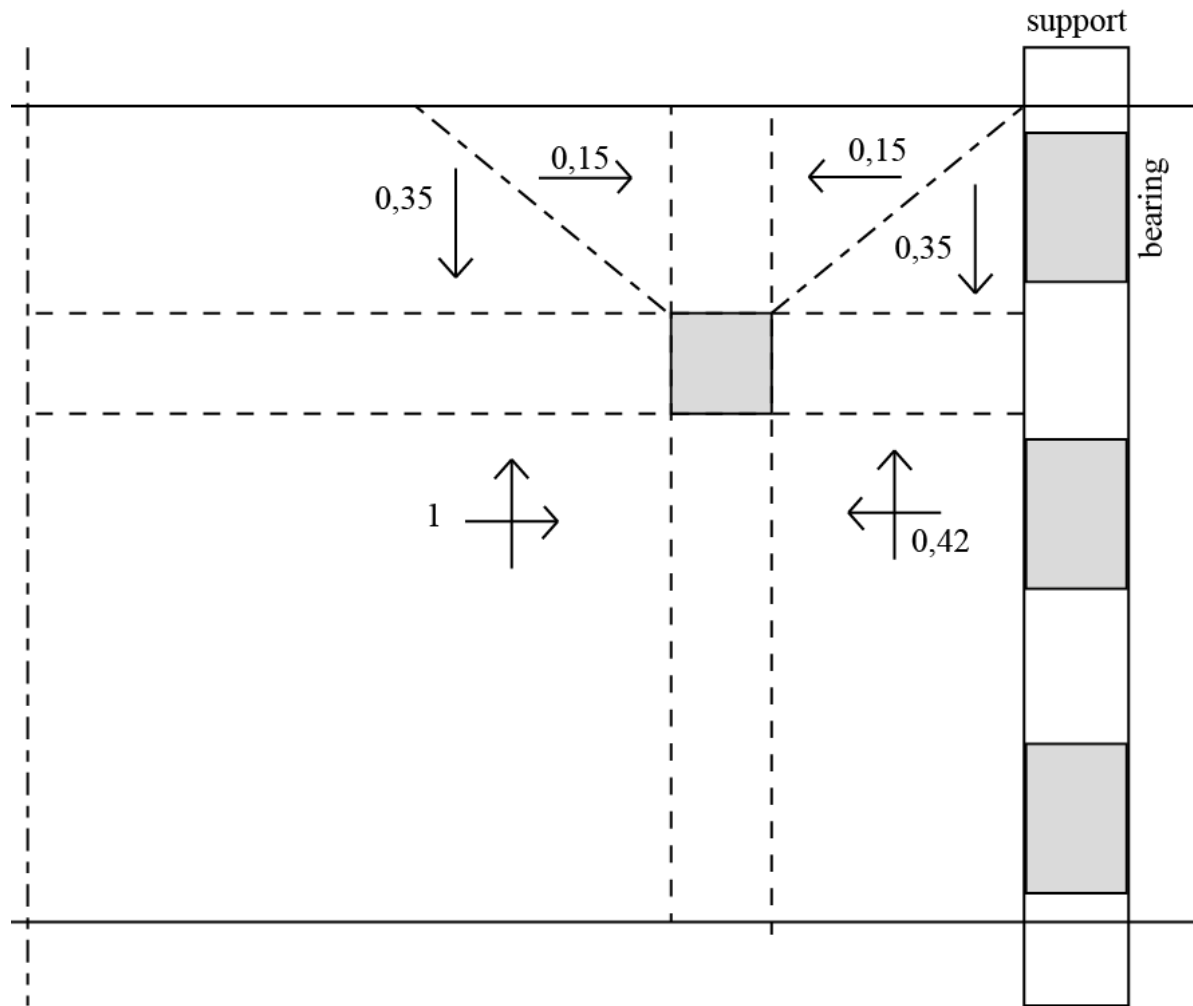


# Modified Bond Model (5)

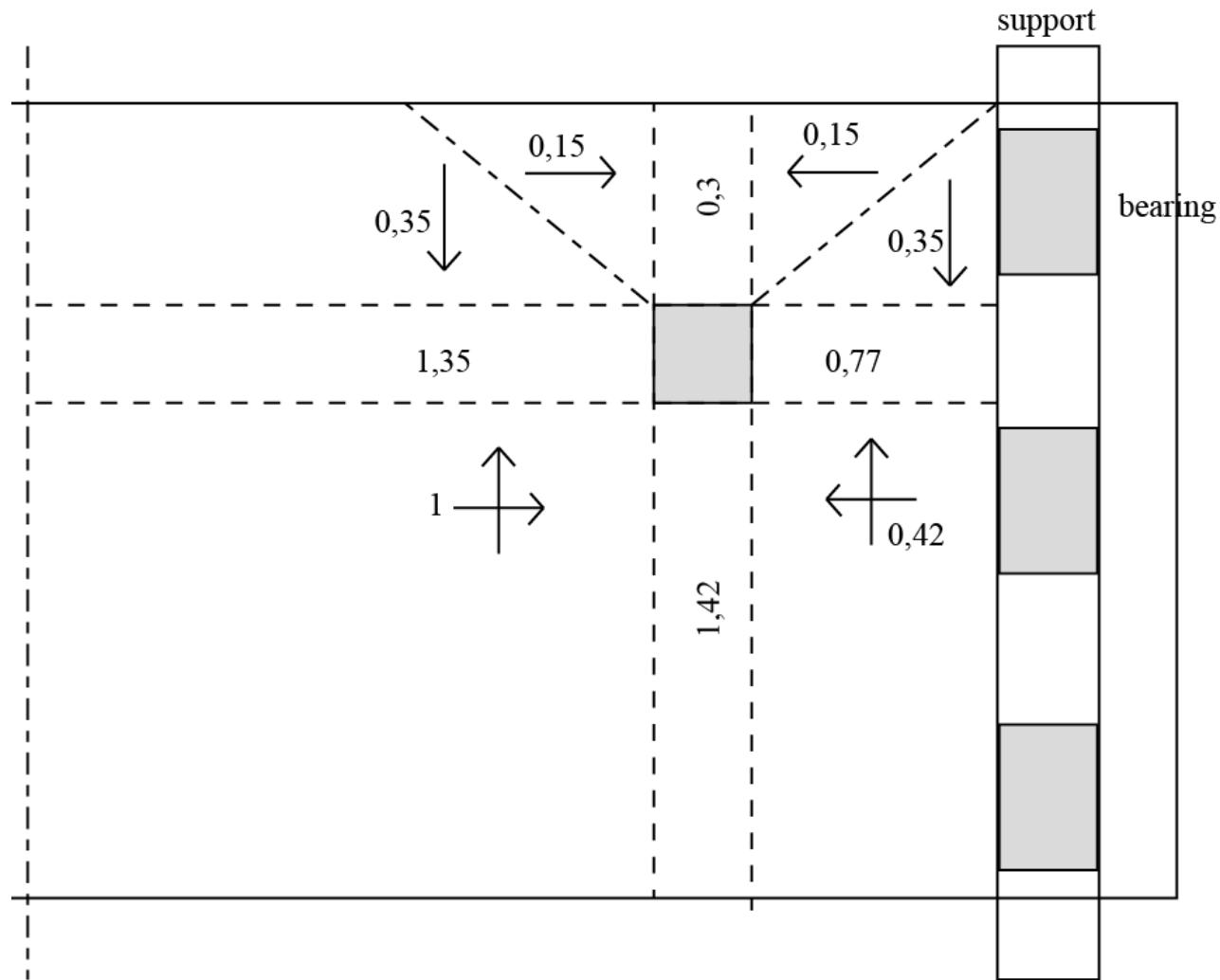




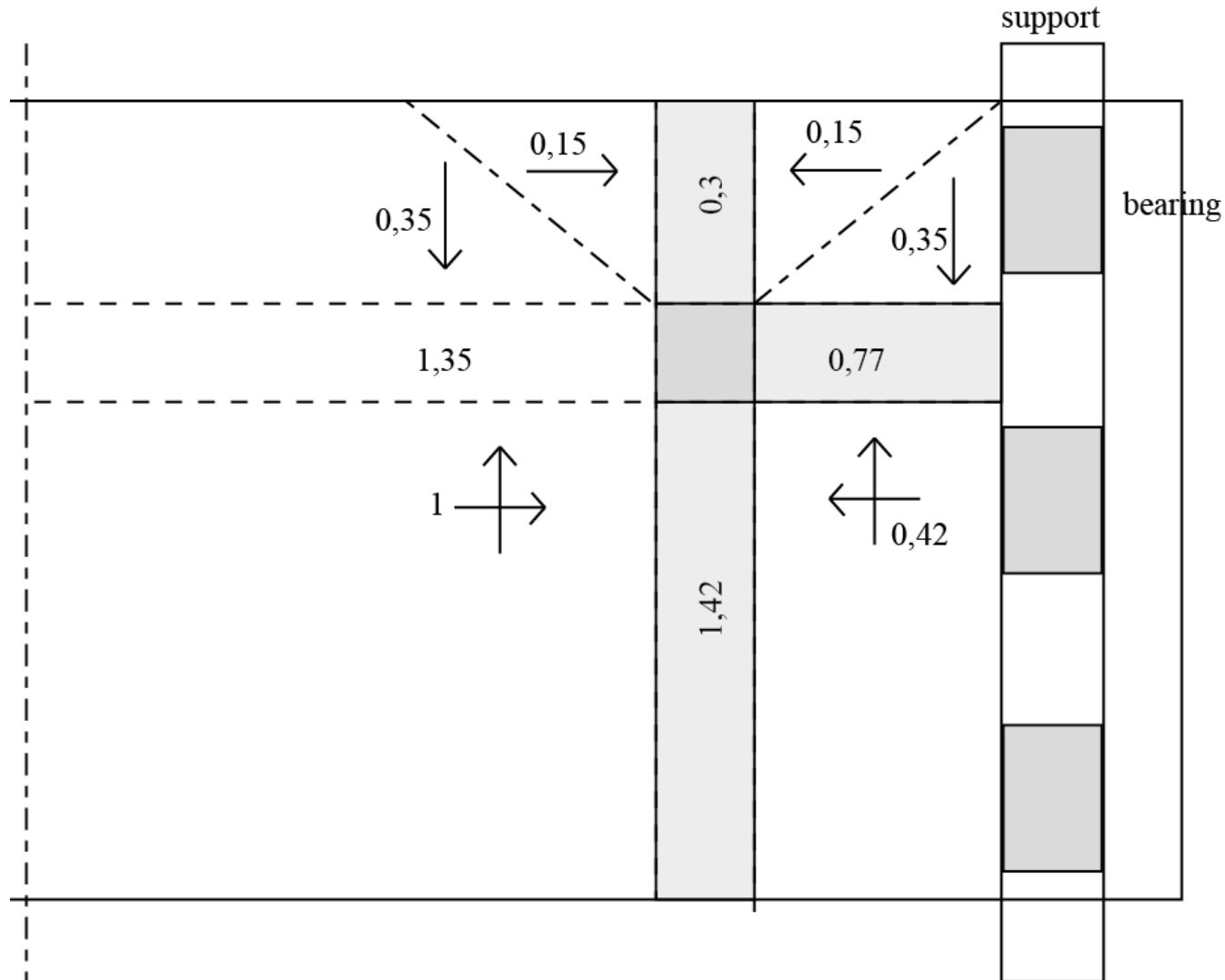
# Modified Bond Model (6)



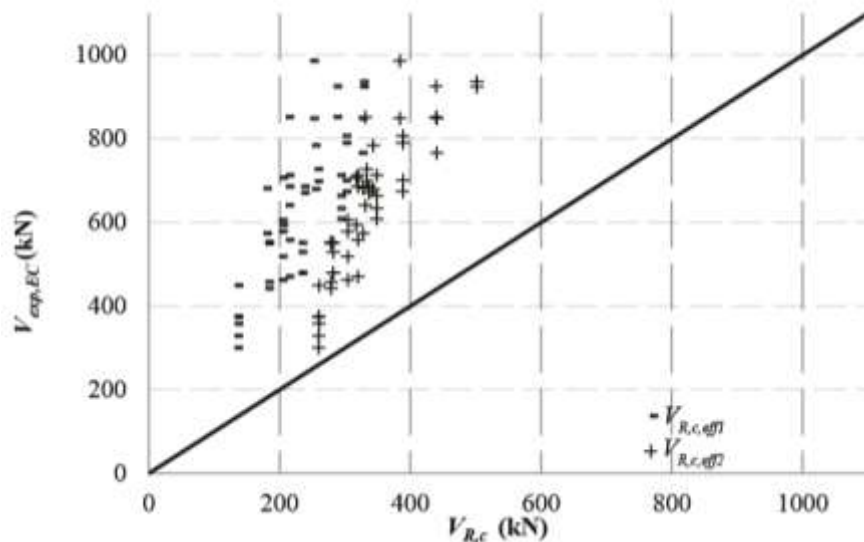
# Modified Bond Model (7)



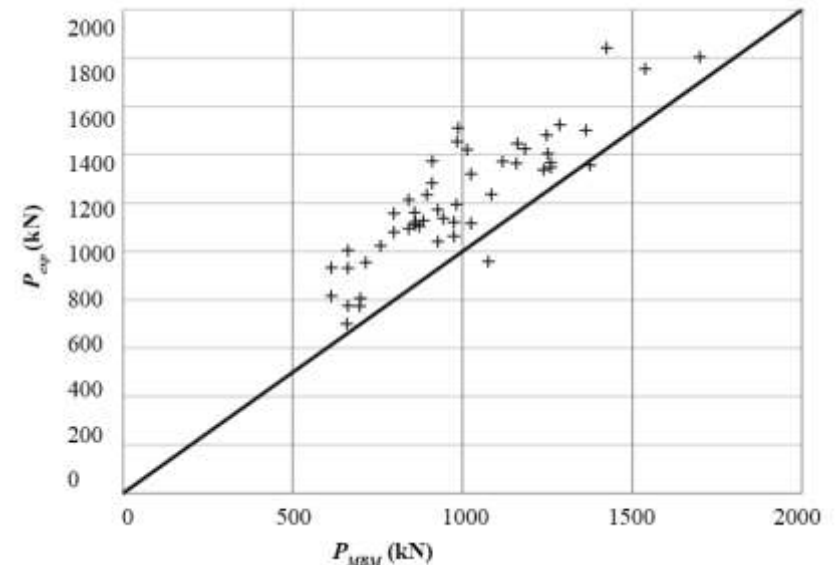
# Modified Bond Model (8)



# Modified Bond Model (9)



Experiments vs Eurocode shear



Experiments vs Modified Bond Model

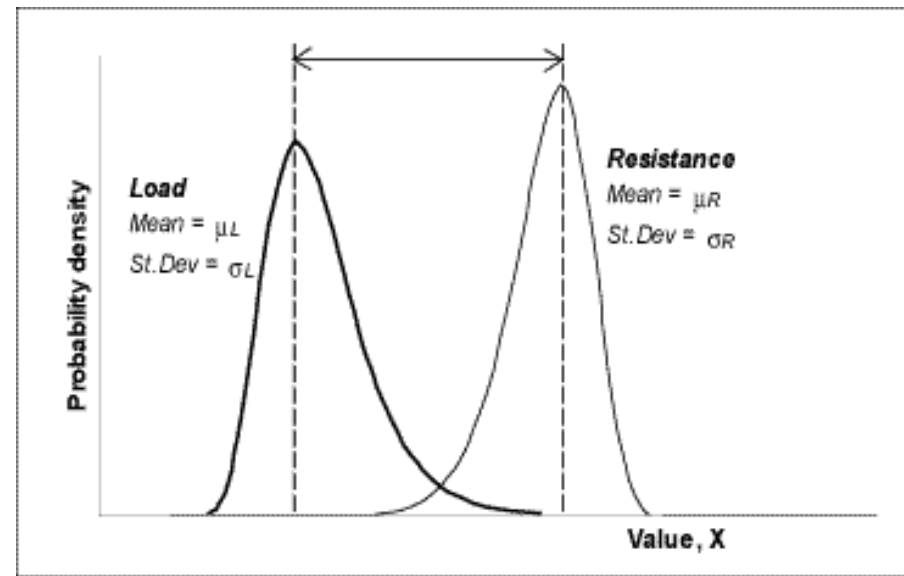
# Code extension proposal

## Limit State function

$$P_f = P \quad R < R_d$$

Experiment vs. Design value

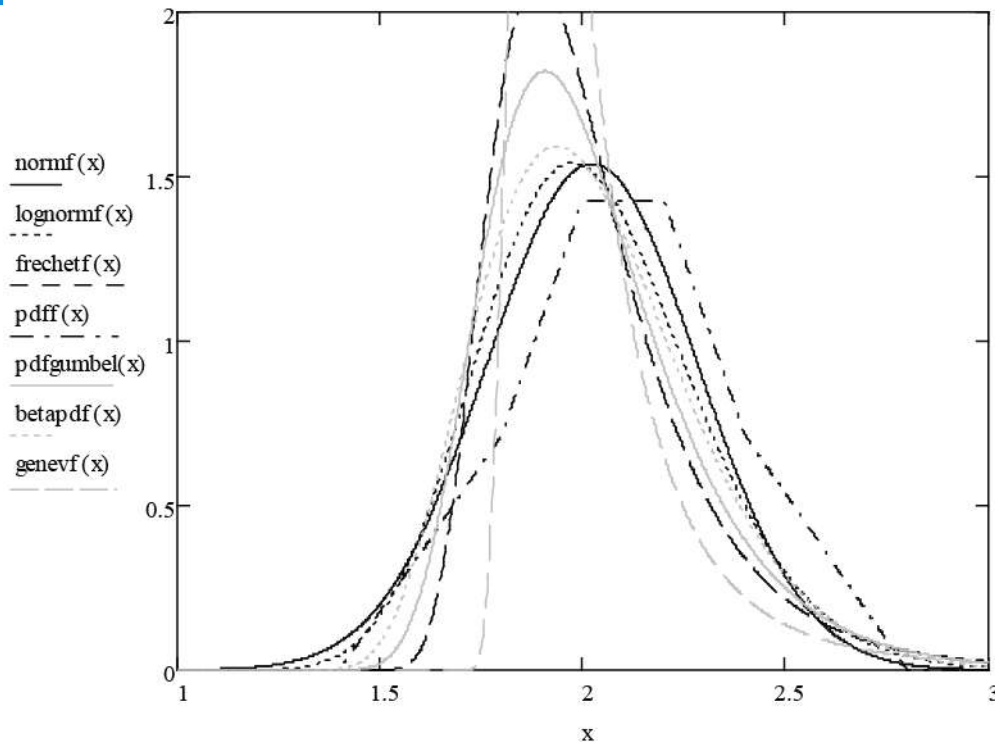
- Experiment
  - mean values
  - Test/Predicted ratio
- Design value
  - characteristic values



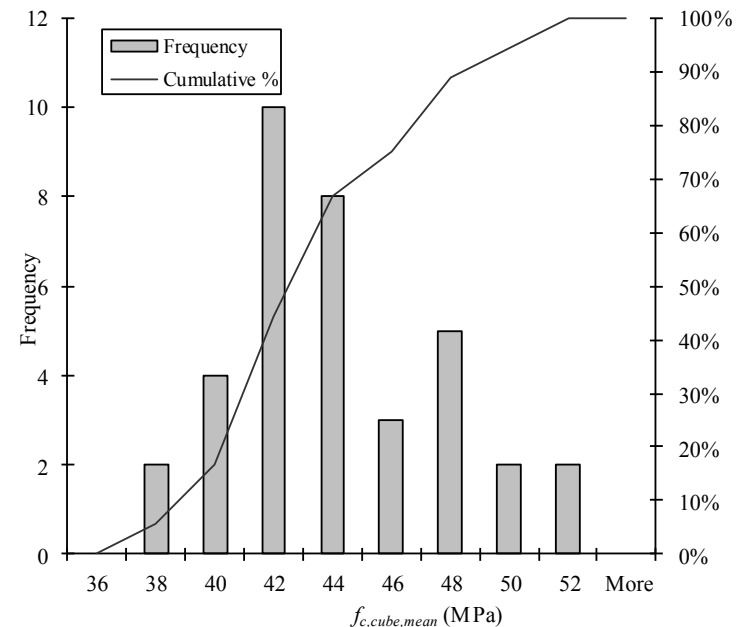
Reliability analysis based on load and resistance

# Code extension proposal

## Random variables



Test/Predicted



concrete compressive strength

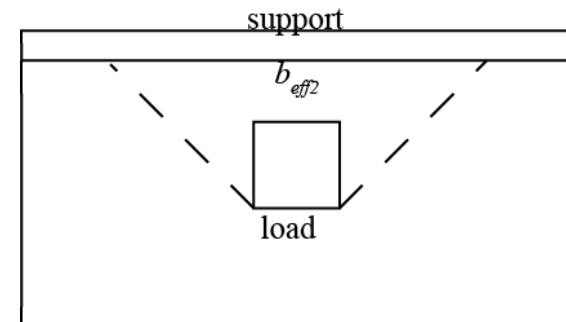


# Code extension proposal

## Slabs subjected to Wheel Loads

$$V_{Rd,c,prop} = C_{Rd,c} k 100 \rho_l f_{ck}^{1/3} b_{eff,red} d_l \left( 1.9 - \frac{f_{ck}}{225} \right)$$

$$b_{eff,red} = \left( 0.52 \frac{l_{sup}}{b} + 0.48 \right) b_{eff}$$



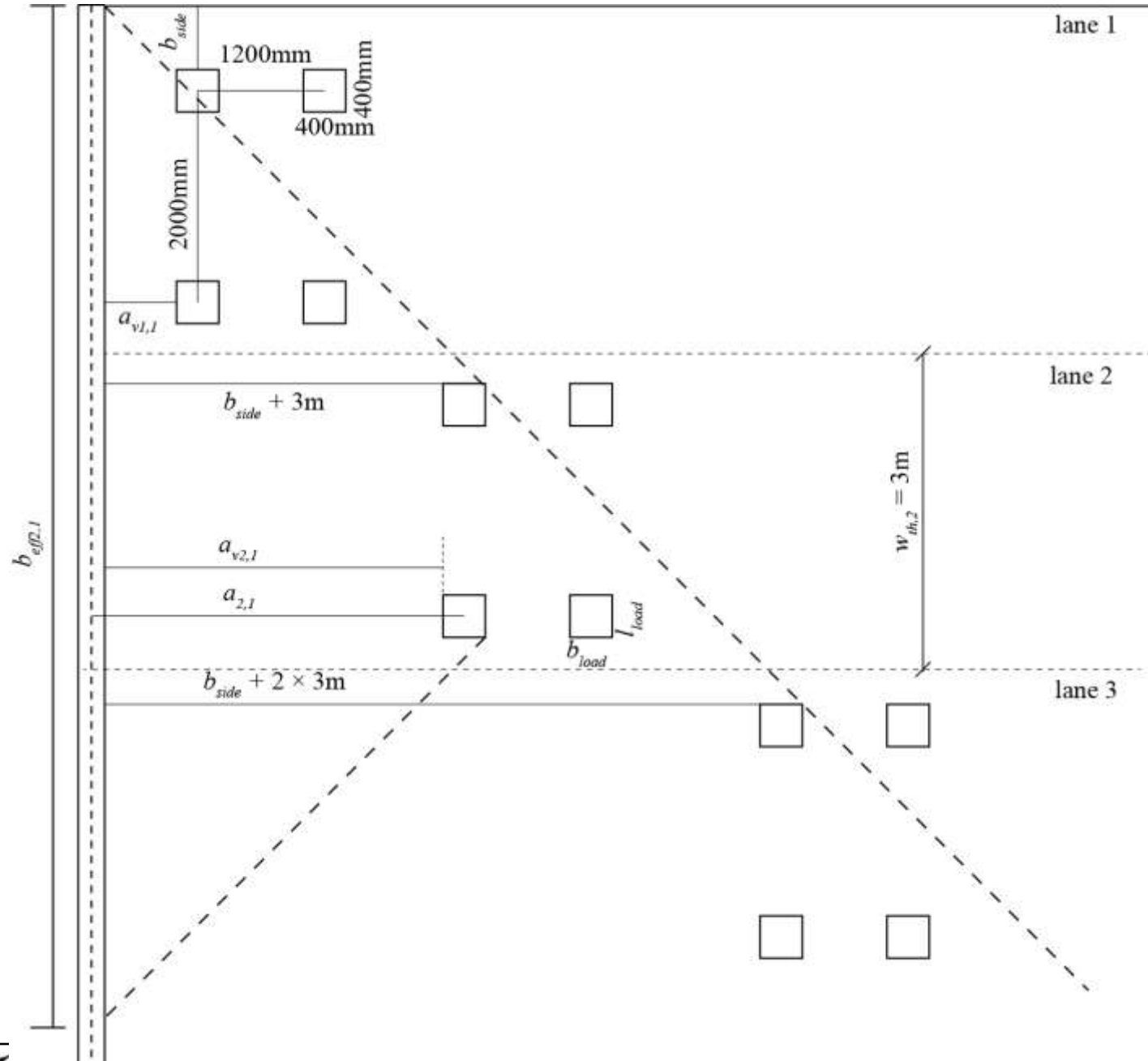
- Enhancement factor depends on  $f_{ck}$ 
  - Experiments:  $f_{ck}$  not as in shear formula
- Effect of reduced support width
- Proposal for  $a_v \leq 2.5d_l$



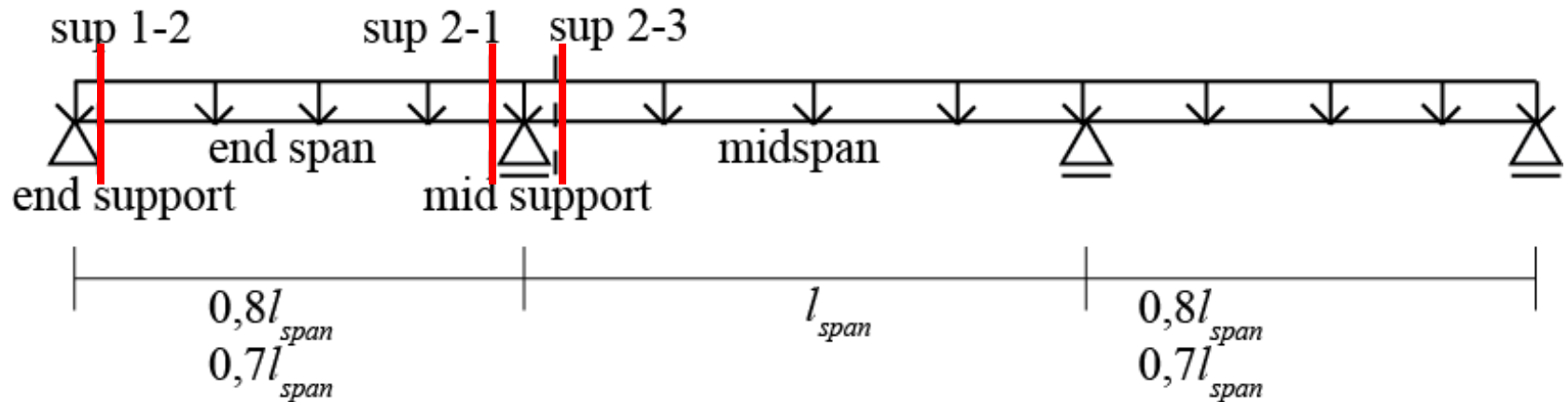
# Application to practice (1)

- Evaluating existing solid slab bridges:
  - NEN-EN 1992-1-1:2005
  - 25% reduction of contribution concentrated load close to support
  - $\beta = a/2d$
  - Combined:  $\beta_{new} = a/2,5d$
  - Effective width: French method and minimum  $4d$





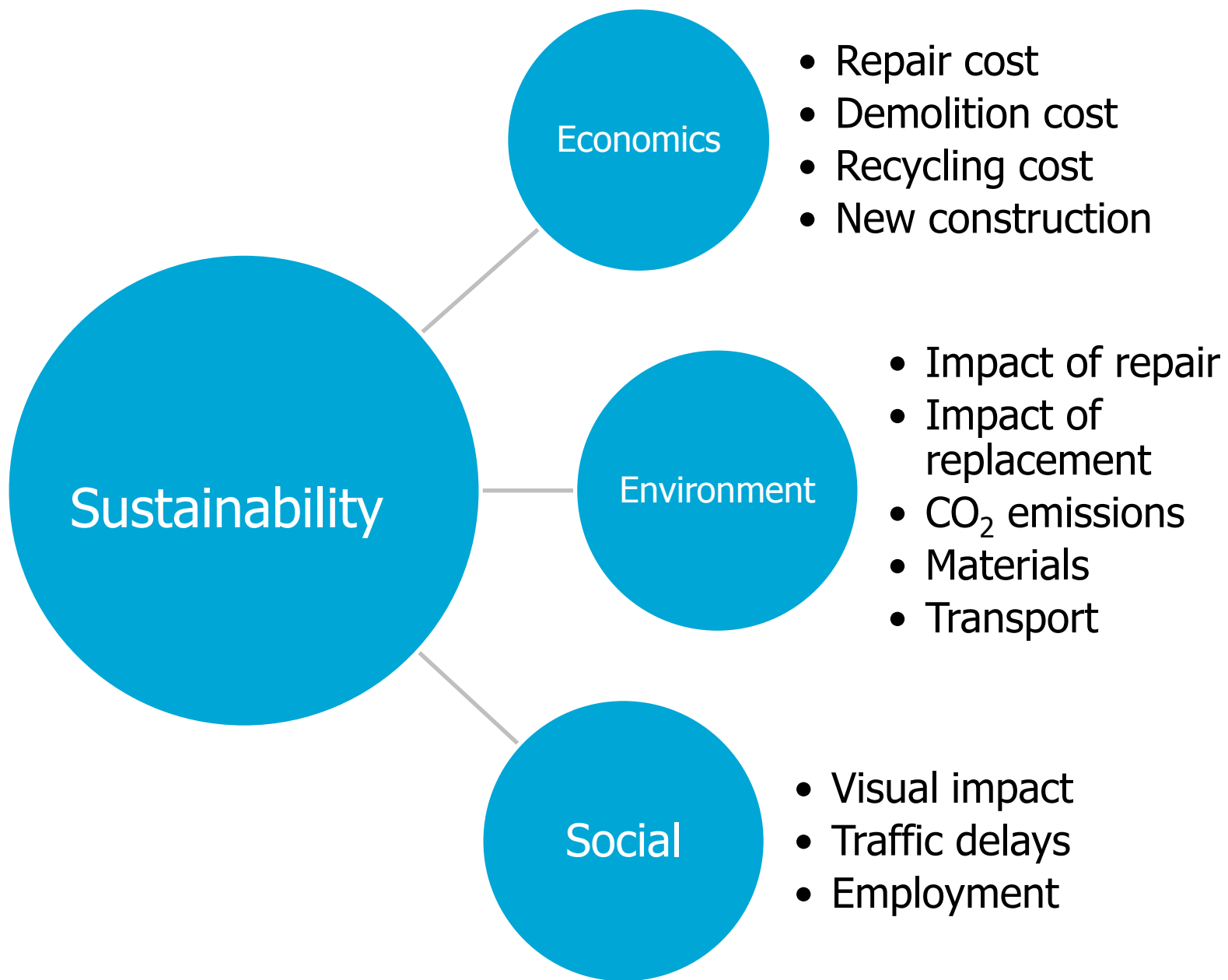
# Application to practice (3)



- Checks at indicated sections
- 9 existing Dutch solid slab bridges

# Application to practice (4)

- Shear **stresses**: influence of recommendations
  - QS-EC2: wheel loads at  $a_v = 2,5d_l$
  - QS-VBC: wheel loads at  $a_v = d_l$
  - QS-EC2 18% reduction in loads
- Shear **capacity**:
  - QS-EC2:  $v_{Rd,c} \sim \rho_l d$
  - low reinforcement + deep section = small shear capacity
  - QS-VBC:  $\tau_1 \sim f_{ck}$  only
- QS-EC2 improved selection ability



# Impact on Sustainability

Example replacement of 3-span slab bridge (deck only)

- Economic cost: 500k – 640k €
- Environmental cost: 136 ton CO<sub>2</sub>
  - Blast furnace cement: 74 ton CO<sub>2</sub>
  - Portland slag cement: 122 ton CO<sub>2</sub>
- Social cost: case-dependent
  - can be 9 times economic cost
- Scope: 600 slab bridges



# Summary & Conclusions

- Slabs under concentrated loads behave differently in shear than beams
- Beneficial effect of transverse load redistribution
- Modified Bond Model improvement as compared to Eurocode
- Code extension proposal for transverse load redistribution
- Application to practice: reduction in loads







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