Project				Job Ref.	
Section				Sheet no./rev.	
					1
Calc. by	Date	Chk'd by	Date	App'd by	Date
RSF	1/10/2012				

Reinforced Masonry Wall Out-of-Plane Axial, Bending and Shear Forces;

Referance and notes: Reinforced Masonry Handbook use static equilibrium and strain compatibility. Enter forces per length of wall then use length of wall as center to center spacing of reinforcement. Reinforcement must be tied to be considered effective in carrying vertical load or compressive stress from bending. Because the reinforcement is not tied it will not be considered effective in for axial load.

Wall Geometry and Forces;

 $\label{eq:Height of wall;} \textit{H=12.0ft;}$ Center to Center spacing of reinforcement; b=48in;

 $\text{Reinforcment size (bar number)}; \\ b_{\text{num}} = 5; \\ A_{\text{s}} = \text{pi}/4*(b_{\text{num}}*1\text{in}/8)^2 = \textbf{0.307} \text{in}^2;$

 $\label{eq:potential} Axial Load (per foot of wall); $$P=2kip/ft;$$ Moment (per foot of wall); $$M=0.56kip_ft/ft;$$ Shear; $$V=0.5kip/ft;$$$

Wall Properties (compare to Table GN-8b) Geometry;

(assumes face shells, cell at bar and webs each side of bar are grouted)

$$\label{eq:continuous_problem} \begin{split} &\text{Nominal thickness of unit (height of x-section);} & & h=7.625 \text{in;} \\ &\text{Depth to reinforcement;} & & d=3.81 \text{in;} \\ &\text{Flange thickness;} & & t_{\text{f}}=1.25 \text{in;} \\ &\text{Web thickness;} & & t_{\text{w}}=1.0 \text{in;} \\ \end{split}$$

Width of unit and width of grout; b_{unit}=15.625in; b_{grout}=0.375in;

Nominal width of unit; $b_{nunit} = b_{unit} + b_{grout} = \textbf{16.000} in;$ Width of web cell; $b_{cell} = (b_{unit} - 3^*t_w)/2 = \textbf{6.313} in;$ Width of web; $b_w = b_{cell} + 2^*t_f = \textbf{8.813} in;$ Height of web; $h_w = h - 2^*t_f = \textbf{5.125} in;$

Total area based on rebar spacing; $A=2*b*t_f+h_w*b_w=165.164in^2$;

Total moment of inertia based on rebar spacing; $l=b^*h^3/12-(b-b_w)/2^*h_w^3/12^*2=1333.699in^4$;

Radius of gryation; $r=(I/A)^{0.5}=2.842in;$

Shear Area (disregard kd as max shear will not

occur at max moment); $A_v = b^* t_f + b_w^* (d - t_f) = 82.560 \text{ in}^2$;

Wall Properties Material (See Tbl 2.2B or IBC 2105.2.2.1.2);

Allowable 1/3rd increase; i=1.33;

Maximum masonry compressive stress; f'_m '=1500psi; f'_m =f'_m'*i=1995.000psi; Yeild and Allowable rebar stress; F_v =60ksi; F_s '= F_v /2.5=**24.000**ksi; F_s = F_s '*i=31920.000psi;

Modulus of Elasticity – steel; E_s=29000ksi;

Modulus of Elasticity – masonry; $E_m=900*f'_m=1795.500$ ksi; (use 700 for clay)

 $\label{eq:modular ratio} \mbox{Modular ratio;} & n=E_s/E_m=\textbf{16.151}; \\ \mbox{Allowable compressive stress;} & F_m=f'_m/3=\textbf{665.000} \mbox{psi;} \\ \mbox{}$

Slenderness Ratio; $\gamma = H/r = 50.675$

Reduction factor for slenderness; R1=1- $(\gamma/140)^2$ =**0.869**; R2= $(70/\gamma)^2$ =**1.908**;

R=if(γ <=99,R1,R2)=**0.869**;

Allowable axial stress; Fa=0.25* f'_m *R=433.405psi;

Allowable shear stress; $Fv=min(1psi^*(f'_m/1psi)^{0.5},50psi^*i)= \textbf{44.665}psi;$

Eccentricity required from loads; e_d=M/P=**3.360**in;

Project	Job Ref.				
Section				Sheet no./rev.	
		2			
Calc. by	Date	Chk'd by	Date	App'd by	Date
RSF	1/10/2012				

Analysis of Stesses;

Assume location of NA; kd=2.0 in;

Assume allowable compressive stress of

masonry controls; $f_m=F_m$;

 $\begin{tabular}{ll} Effective flange thickness; & $t'_f = min(t_f, kd) = 1.250 in; \\ Effective height of web; & $y_{cw} = max(0in, kd-t'f)$ \end{tabular}$

 $\begin{array}{ll} \text{Stress at flange/web intersection;} & f_{\text{cw}} = f_{\text{m}}^*(\text{kd-t'}_f)/\text{kd} = \textbf{249.375} \text{psi;} \\ \text{Stress in steel based on compatibility;} & f'_{\text{s}} = n^* f_{\text{m}}/\text{kd}^*(\text{d-kd}) = \textbf{9.720} \text{ksi;} \\ \text{Usable steel stress;} & f_{\text{s}} = \min(F_{\text{s}}, f'_{\text{s}}) = \textbf{9.720} \text{ksi;} \\ \end{array}$

 $\label{eq:compressive} \begin{array}{ll} \text{Compressive force on flange;} & C_f = 0.5^* (f_m + f_{cw})^* t'_i r'_b = \textbf{27.431} \text{kip;} \\ \text{Compressive force on web;} & C_w = 0.5^* y_{cw}^* f_{cw}^* b_w = \textbf{0.824} \text{kip;} \\ \text{Tension force;} & T = \max(0 \text{kip,} A_s^* f_s) = \textbf{2.982} \text{kip;} \\ \end{array}$

Momemt Arm – Flange; $X_{cf}=h/2-t'_f(2^*f_{cw}+f_m)/(3^*(f_{cw}+f_m))=3.282in;$

 $\label{eq:moment_strength} \begin{tabular}{ll} M_{cf}\!=\!X_{cf}{}^*\!C_f\!=\!\textbf{7.503} kip_ft; \\ Moment Arm - Web; & X_{cw}\!=\!h/2\!-\!(t'f\!+\!y_{cw}/3)\!=\!\textbf{2.312} in; \\ Moment strength - Web; & M_{cw}\!=\!X_{cw}{}^*\!C_w\!=\!\textbf{0.159} kip_ft; \\ Moment Arm - Steel; & X_{s1}\!=\!h/2\!-\!d\!=\!\textbf{0.002} in; \\ Moment strength - steel; & M_{s1}\!=\!X_{s1}{}^*\!T\!=\!\textbf{0.001} kip_ft; \\ \end{tabular}$

Compressive force based on assumed kd

location and "fm=Fm"; $P_{ns}=C_f+C_w-T=25.273 \text{kip};$

Moment stength of section based on assumed

kd location and "fm=FM"; $M_{ns}=M_{cf}+M_{cw}-M_{s1}=7.661$ kip_ft;

Eccentricity of section; $e_s=M_{ns}/P_{ns}=3.638$ in;

 $\label{eq:compare to Eccentricity of Required;} \text{Compare to Eccentricity of Required;} \\ \text{e}_{\text{d}}\text{=}\textbf{3.360} \text{in;}$

Checks;

Loads on effective wall length; $P_r=P^*b=8.000$ kip; $M_r=M^*b=2.240$ kip_ft; $V_r=V^*b=2.000$ kip;

Axial Stress; $f_a \!\!=\!\! P_r \!/ A \!\!=\!\! 48.437 psi;$ Shear Stress; $f_v \!\!=\!\! V^* b / A_v \!\!=\!\! 24.225 psi$

 $\begin{array}{lll} \text{Check Axial Stress;} & \text{ChAx=if(f}_a < \text{Fa,"OK","NG")="OK";} \\ \text{Check Shear stress;} & \text{ChV=if(fv} < \text{Fv,"OK","NG")="OK";} \\ \text{Check Axial Strength;} & \text{ChP=if(P}_{ns} > P_{r,"OK","NG")="OK";} \\ \text{Check Moment Strength;} & \text{ChM=if(M}_{ns} > M_{r,"OK","NG")="OK";} \\ \text{Old max reinf. Ratio IBC 2006 (not found in 2009);} & \rho_{max} = n^*f'_m/(2^*F_v^*(n+F_v/f'_m)) = \textbf{0.006}; \\ \end{array}$