

# NorthWoods Software

**Program Name:** NGuardrail-HSSc\_Post\_to\_Stringer

**Project Name:** -

**Project Number:** -

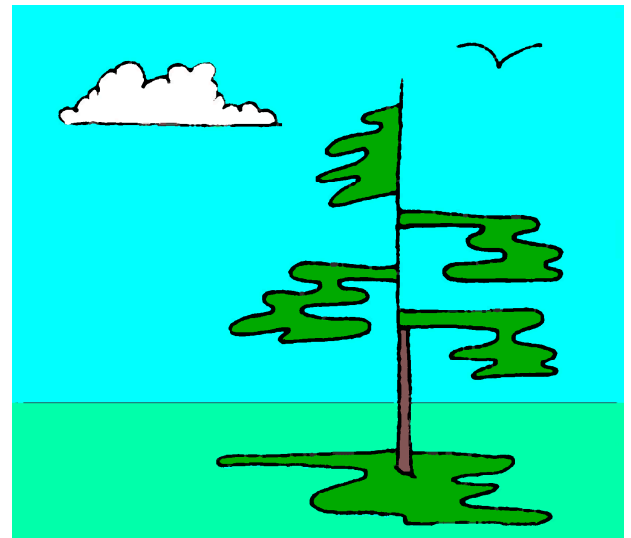
**Project Description:** -

**Project Designer:** Dik

**Last Revised (yy-mm-dd):** 21.07.06

**Reference:** NBCC, CSA S16

Created using SMath Studio, a MathCAD workalike from <https://en.smath.info/view/SMathStudio>. The User is responsible to verify data using an alternative method



## Menu:

<span style="background-color: yellow; border: 1px solid black; padding: 2px;">.....</span> Input Data	<span style="background-color: cyan; border: 1px solid black; padding: 2px;">.....</span> Important Output	<span style="background-color: lightgreen; border: 1px solid black; padding: 2px;">.....</span> Logical Constructs	<span style="background-color: blue; color: white; border: 1px solid black; padding: 2px;">Blue</span> Units
<span style="background-color: pink; border: 1px solid black; padding: 2px;">.....</span> Sum / For	<span style="background-color: red; color: white; border: 1px solid black; padding: 2px;">Red</span> Important Note	<span style="background-color: gray; border: 1px solid black; padding: 2px;">Gray</span> Temporary Variables	

## Defined Units:

$K := \text{kip}$					Force
$K_{ft} := K \text{ ft}$	$kN_m := kN \text{ m}$	$K_{in} := K \text{ in}$	$kN_{mm} := kN \text{ mm}$	$lb_{in} := lbf \text{ in}$	Moment
$pcf := \frac{lbf}{ft^3}$	$kN_{pcm} := \frac{kN}{m^3}$	$kg_{pcm} := \frac{kg}{m^3}$			Density
$K_{lf} := \frac{K}{ft}$	$plf := \frac{lbf}{ft}$	$kN_{pm} := \frac{kN}{m}$	$K_{pi} := \frac{K}{in}$	$kN_{pmm} := \frac{kN}{mm}$	Force/Unit Length
$psf := \frac{lbf}{ft^2}$	$K_{sf} := \frac{K}{ft^2}$	$K_{si} := \frac{K}{in^2}$	$kN_{psm} := \frac{kN}{m^2}$	$psi := \frac{lbf}{in^2}$	Pressure
$N_{psmm} := \frac{N}{mm^2}$					Pressure
$pci := \frac{lbf}{in^3}$					Subgrade Modulus
$psf_{pf} := \frac{psf}{ft}$	$kPa_{pm} := \frac{kPa}{m}$				Pressure per Depth
$pmcf := \frac{lb}{ft^3}$	$lb := lbf$				Force
$mph := \frac{mi}{hr}$	$kph := \frac{km}{hr}$				Velocity
$ispf := \frac{in^2}{ft}$	$mm_{spm} := \frac{mm^2}{m}$				Area per Unit Length

## User Defined Functions:

```

Check (arg) := if arg = 1
                Check := "...OK"
            else
                Check := "...NG"

```

c  $Check (2 = 3) = "...NG"$

$Check (2 \neq 3) = "...OK"$

b  $Check (2 \leq 3) = "...OK"$

$Check (3 \geq 2) = "...OK"$

a

**Input Data****Material Property Factors:**

$$\phi_s := 0.90$$

$$\phi_b := 0.8$$

$$\phi_w := 0.67$$

$$\phi_{br} := 0.8$$

**Load Factors:**

$$\alpha_L := 1.50$$

$$\alpha_D := 1.25$$

**Steel Properties:**

**HSSc Section:**  $st_{NDX} := 1$

NDX	des	fy	Fu
1	"G40.21-350W"	50 Ksi	65 Ksi
2	"G40.21-300W"	44 Ksi	65 Ksi
3	"A36"	36 Ksi	58 Ksi

$$desM_{st1} := st_{NDX} \quad f_{y1} := st_{NDX} \quad F_{u1} := st_{NDX} \quad E_s := 29000 \text{ Ksi}$$

$$\nu := 0.3 \quad G_s := \frac{E_s}{2 \cdot (1 + \nu)} \quad \gamma_s := 489 \text{ pcf}$$

**C Section:**  $st_{NDX} := 2$

$$desM_{st2} := st_{NDX} \quad f_{y2} := st_{NDX} \quad F_{u2} := st_{NDX}$$

**Section Properties-HSSc (Circular):**  $pp_{NDX} := 6$

NDX	desl	desM	d	t
1	"HSS 1.90x0.188"	"HSS 48.3x4.8"	1.90 in	0.188 in
2	"HSS 1.90x0.145"	"HSS 48.3x3.8"	1.90 in	0.150 in
3	"HSS 1.90x0.125"	"HSS 48.3x3.2"	1.90 in	0.125 in
4	"HSS 1.66x0.191"	"HSS 42.2x4.9"	1.66 in	0.191 in
5	"HSS 1.66x0.140"	"HSS 42.2x3.6"	1.66 in	0.140 in
6	"HSS 1.66x0.125"	"HSS 42.2x3.2"	1.66 in	0.125 in
7	"HSS 1.32x0.125"	"HSS 33.4x3.2"	1.315 in	0.125 in

$$desI_p := pp_{NDX} \quad desM_p := pp_{NDX} \quad \phi_{od} := pp_{NDX} \quad t_p := pp_{NDX}$$

$\phi_{id} := \phi_{od} - 2 \cdot t_p$	$\phi_{od} = 1.66 \text{ in}$	$\phi_{od} = 42.2 \text{ mm}$	HSSc Outer $\phi$
	$t_p = 0.125 \text{ in}$	$t_p = 3.2 \text{ mm}$	HSSc Wall Thickness
	$\phi_{id} = 1.41 \text{ in}$	$\phi_{id} = 35.8 \text{ mm}$	HSSc Inner $\phi$
$A_p := \pi \cdot \frac{(\phi_{od}^2 - \phi_{id}^2)}{4}$	$A_p = 0.6028 \text{ in}^2$	$A_p = 389 \text{ mm}^2$	HSSc Area
$Z_p := \frac{(\phi_{od}^3 - \phi_{id}^3)}{6}$	$Z_p = 0.2952 \text{ in}^3$	$Z_p = 4837 \text{ mm}^3$	HSSc Plastic Section

**Factored Loading:**

$$V_f := 2 \text{ K}$$

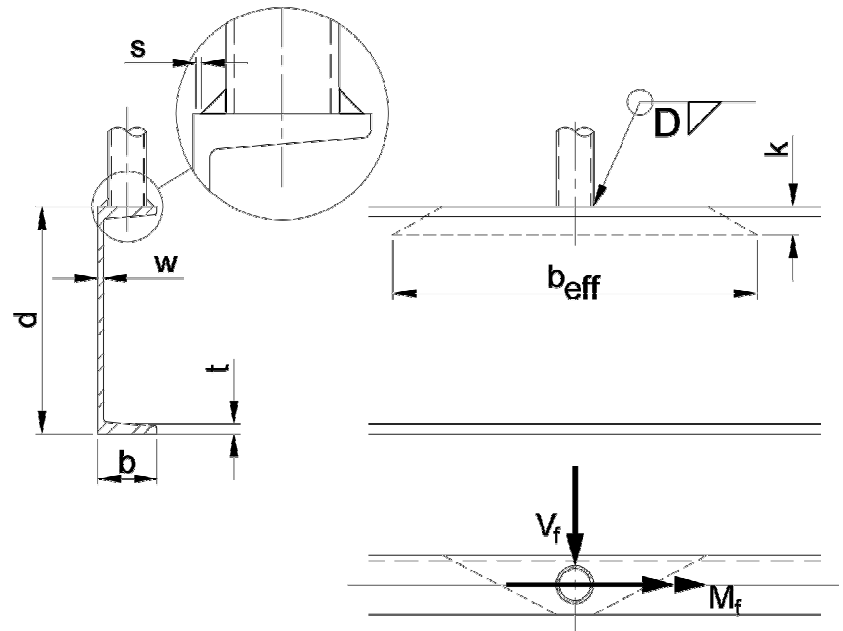
$$V_f = 2.00 \text{ K}$$

$$V_f = 8.90 \text{ kN}$$

$$M_f := 1.0 \text{ K\_ft}$$

$$M_f = 12.00 \text{ K\_in}$$

$$M_f = 1355.82 \text{ kN\_mm}$$



**Slope Information:**

$$rise := 0 \text{ in}$$

$$rise = 0 \text{ in}$$

$$rise = 0$$

Rise

$$run := 703.5 \text{ in}$$

$$run = 703.5 \text{ in}$$

$$run = 17.869 \text{ m}$$

Run

$$\phi := \text{atan}\left(\frac{rise}{run}\right)$$

$$\phi = 0^\circ$$

Guardrail Angle

$$\alpha_1 := \frac{1}{\cos(\phi)}$$

$$\alpha_1 = 1$$

Amplification Factor

**C Section Geometry:**

$$desI_c := "C10 \times 15.3"$$

$$desI_c = "C10 \times 15.3"$$

Imperial Beam Designation

$$desM_c := "C250 \times 23"$$

$$desM_c = "C250 \times 23"$$

Metric Beam Designation

$$d := 10.00 \text{ in}$$

$$d = 10.00 \text{ in}$$

$$d = 254.0 \text{ mm}$$

Depth

$$b := 2.60 \text{ in}$$

$$b = 2.60 \text{ in}$$

$$b = 66.0 \text{ mm}$$

Width

$$t := 0.436 \text{ in}$$

$$t = 0.44 \text{ in}$$

$$t = 11.1 \text{ mm}$$

Flange Thickness

$$w := 0.240 \text{ in}$$

$$w = 0.24 \text{ in}$$

$$w = 6.1 \text{ mm}$$

Web Thickness

$$k := 1.00 \text{ in}$$

$$k = 1.00 \text{ in}$$

$$k = 25.4 \text{ mm}$$

Web Fillet Distance

**Weld:**

$$\text{Electrodes: } we_{NDX} := 2$$

NDX	Desl	DesM	UTS
1	"E60xx"	"E43xx"	60 ksi
2	"E70xx"	"E49xx"	70 ksi
3	"E80xx"	"E55xx-x"	80 ksi
4	"E90xx"	"E62xx-x"	90 ksi

$$we := \begin{bmatrix} 1 & "E60xx" & "E43xx" & 60 \text{ ksi} \\ 2 & "E70xx" & "E49xx" & 70 \text{ ksi} \\ 3 & "E80xx" & "E55xx-x" & 80 \text{ ksi} \\ 4 & "E90xx" & "E62xx-x" & 90 \text{ ksi} \end{bmatrix}$$

$$desI_w := we_{we_{NDX} 2} \quad desM_w := we_{we_{NDX} 3} \quad X_u := we_{we_{NDX} 4}$$

$$\text{Sizes: } ws_{NDX} := 7$$

NDX	desl	desM	D
1	"	"3mm"	0.11811 in
2	"1/8"	"	0.125 in
3	"	"4mm"	0.15748 in
4	"3/16"	"	0.1875 in
5	"	"5mm"	0.19685 in
6	"	"6mm"	0.23622 in
7	"1/4"	"	0.25 in
8	"	"7mm"	0.275591 in
9	"5/16"	"	0.3125 in
10	"	"8mm"	0.314961 in
11	"	"9mm"	0.354331 in
12	"3/8"	"	0.375 in
13	"	"10mm"	0.3937 in
14	"	"11mm"	0.4331 in
15	"7/16"	"	0.4375 in
16	"	"12mm"	0.4724 in
17	"1/2"	"	0.50 in

$$ws := \begin{bmatrix} 1 & "" & "3mm" & 0.11811 \text{ in} \\ 2 & "1/8" & "" & 0.125 \text{ in} \\ 3 & "" & "4mm" & 0.15748 \text{ in} \\ 4 & "3/16" & "" & 0.1875 \text{ in} \\ 5 & "" & "5mm" & 0.19685 \text{ in} \\ 6 & "" & "6mm" & 0.23622 \text{ in} \\ 7 & "1/4" & "" & 0.25 \text{ in} \\ 8 & "" & "7mm" & 0.275591 \text{ in} \\ 9 & "5/16" & "" & 0.3125 \text{ in} \\ 10 & "" & "8mm" & 0.314961 \text{ in} \\ 11 & "" & "9mm" & 0.354331 \text{ in} \\ 12 & "3/8" & "" & 0.375 \text{ in} \\ 13 & "" & "10mm" & 0.3937 \text{ in} \\ 14 & "" & "11mm" & 0.4331 \text{ in} \\ 15 & "7/16" & "" & 0.4375 \text{ in} \\ 16 & "" & "12mm" & 0.4724 \text{ in} \\ 17 & "1/2" & "" & 0.50 \text{ in} \end{bmatrix}$$

$$desI_D := ws_{ws_{NDX} 2} \quad desM_D := ws_{ws_{NDX} 3} \quad D := ws_{ws_{NDX} 4}$$

**Moment Resistance of Channel (from AISC DG 34):**

$$b_{eff} := \phi_{od} + 2 \cdot 2.5 \cdot \left( \left( k - \frac{t}{2} \right) + b \right)$$

$$b_{eff} = 18.57 \text{ in}$$

$$b_{eff} = 471.7 \text{ mm}$$

Equation 7.1

$$Z_x := \frac{b_{eff} \cdot t^2}{4}$$

$$Z_x = 0.88 \text{ in}^3$$

$$Z_x = 14462 \text{ mm}^3$$

$$M_{rc} := \phi_s \cdot f_{y2} \cdot Z_x$$

$$M_{rc} = 34.95 \text{ K\_in}$$

$$M_{rc} = 3949 \text{ kN\_mm}$$

**Moment Capacity HSSc:**

$$M_{rp} := \phi_s \cdot f_{y1} \cdot Z_p$$

$$M_{rp} = 13.28 \text{ K\_in}$$

$$M_{rp} = 1501 \text{ kN\_mm}$$

**Weld Design:**

$$s := \frac{1}{16} \text{ in}$$

$$s = 0.0625 \text{ in}$$

$$s = 1.6 \text{ mm}$$

Shelf Distance

$$b_{min} := \phi_{od} + 2 \cdot (D + s)$$

$$b_{min} = 2.29 \text{ in}$$

$$b_{min} = 58.0 \text{ mm}$$

Minimum Width of C Section

**Weld Material Strength**

$$v_{rw} := \phi_w \cdot 0.67 \cdot X_u \cdot \frac{1}{\sqrt{2}}$$

$$v_{rw} = 22.2 \text{ ksi}$$

$$v_{rw} = 153.2 \text{ MPa}$$

**Base Metal Strength**

$$v_{rb1} := \phi_w \cdot 0.67 \cdot F_{u1}$$

$$v_{rb1} = 29.2 \text{ Ksi}$$

$$v_{rb1} = 201.2 \text{ MPa}$$

HSSc Section

$$v_{rb2} := \phi_w \cdot 0.67 \cdot F_{u2}$$

$$v_{rb2} = 29.2 \text{ Ksi}$$

$$v_{rb2} = 201.2 \text{ MPa}$$

C Section

**Minimum Weld Capacity**

$$V_{rw} := \min \left( \left[ v_{rw} \quad v_{rb1} \quad v_{rb2} \right] \right) \quad V_{rw} = 22.2 \text{ Ksi}$$

$$V_{rw} = 153.2 \text{ MPa}$$

**Section Properties of Weld:**

$$A_w := \frac{\pi \cdot \left( \left( \phi_{od} + 2 \cdot D \right)^2 - \phi_{od}^2 \right)}{4} \quad A_w = 1.50 \text{ in}^2$$

$$A_w = 968 \text{ mm}^2$$

$$I_{x_w} := \frac{\pi}{4} \cdot \left( \left( \frac{\phi_{od}}{2} + D \right)^4 - \left( \frac{\phi_{od}}{2} \right)^4 \right)$$

$$I_{x_w} = 0.70 \text{ in}^4$$

$$I_{x_w} = 2.90 \cdot 10^5 \text{ mm}^4$$

$$S_{x_w} := \frac{2 \cdot I_{x_w}}{\left( \phi_{od} + 2 \cdot D \right)}$$

$$S_{x_w} = 0.64 \text{ in}^3$$

$$S_{x_w} = 10557 \text{ mm}^3$$

**Stress due to Shear**

$$\sigma_v := \frac{V_f}{A_w}$$

$$\sigma_v = 1.3 \text{ Ksi}$$

$$\sigma_v = 9.2 \text{ MPa}$$

**Stress due to Flexure**

$$\sigma_f := \frac{M_f}{S_{x_w}}$$

$$\sigma_f = 18.6 \text{ Ksi}$$

$$\sigma_f = 128.4 \text{ MPa}$$

**Combined Stress**

$$\sigma := \sqrt{\sigma_v^2 + \sigma_f^2}$$

$$\sigma = 18.7 \text{ Ksi}$$

$$\sigma = 128.8 \text{ MPa}$$

**Moment Resistance of Weld**

$$M_{rw} := V_{rw} \cdot S_{x_w}$$

$$M_{rw} = 14.3 \text{ K\_in}$$

$$M_{rw} = 1617.4 \text{ kN\_mm}$$

**Minimum Moment Resistance**

$$M_r := \min \left( \left[ M_{rc} \quad M_{rp} \quad M_{rw} \right] \right)$$

$$M_r = 13.28 \text{ K\_in}$$

$$M_r = 1501 \text{ kN\_mm}$$

$$\text{Check} \left( M_r \geq M_f \right) = \text{"...OK"}$$

**Summary:****Material Property Factors**

$$\text{Welds} \quad \phi_w = 0.67$$

$$\text{Steel} \quad \phi_s = 0.9$$

$$\text{Dead Load Factor} \quad \alpha_D = 1.25$$

$$\text{Live Load Factor} \quad \alpha_L = 1.5$$

$$\text{Check } (\alpha_D \geq 1.25) = "...OK"$$

$$\text{Check } (\alpha_L \geq 1.5) = "...OK"$$

**Steel Properties****HSSr Post**

Yield Strength

Ultimate Strength

**C Section**

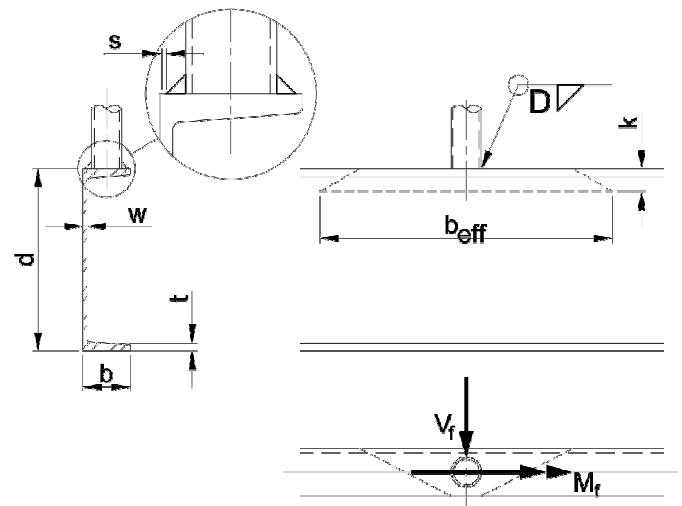
Yield Strength

Ultimate Strength

Young's Modulus

Shear Modulus

Density



$$f_{y1} = 50 \text{ Ksi}$$

$$f_{y1} = 345 \text{ MPa}$$

$$F_{u1} = 65 \text{ Ksi}$$

$$F_{u1} = 448 \text{ MPa}$$

$$f_{y2} = 44 \text{ Ksi}$$

$$f_{y2} = 303 \text{ MPa}$$

$$F_{u2} = 65 \text{ Ksi}$$

$$F_{u2} = 448 \text{ MPa}$$

$$E_s = 29000 \text{ Ksi}$$

$$E_s = 2.00 \cdot 10^5 \text{ MPa}$$

$$G_s = 11153.8462 \text{ Ksi}$$

$$G_s = 76903 \text{ MPa}$$

$$\gamma_s = 489 \text{ pcf}$$

$$\gamma_s = 76.8 \text{ kNpcm}$$

**Section Properties****HSSr Section**

Designation (Imperial)

Designation (Metric)

HSSc Outer  $\phi$ 

HSSc Wall Thickness

HSSc Inner  $\phi$ 

HSSc Area

HSSc Plastic Section

$$desI_p = "HSS \ 1.66 \times 0.125"$$

$$desM_p = "HSS \ 42.2 \times 3.2"$$

$$\phi_{od} = 1.66 \text{ in}$$

$$\phi_{od} = 42.2 \text{ mm}$$

$$t_p = 0.125 \text{ in}$$

$$t_p = 3.2 \text{ mm}$$

$$\phi_{id} = 1.41 \text{ in}$$

$$\phi_{id} = 35.8 \text{ mm}$$

$$A_p = 0.6028 \text{ in}^2$$

$$A_p = 389 \text{ mm}^2$$

$$Z_p = 0.2952 \text{ in}^3$$

$$Z_p = 4837 \text{ mm}^3$$

**C Section**

Designation (Imperial)

Designation (Metric)

Depth

Width

Flange Thickness

Web Thickness

Web Fillet Distance

Shelf Distance

Minimum Width of C Section

$$desI_c = "C10 \times 15.3"$$

$$desM_c = "C250 \times 23"$$

$$d = 10.00 \text{ in}$$

$$d = 254 \text{ mm}$$

$$b = 2.60 \text{ in}$$

$$b = 66 \text{ mm}$$

$$t = 0.44 \text{ in}$$

$$t = 11.1 \text{ mm}$$

$$w = 0.24 \text{ in}$$

$$w = 6.1 \text{ mm}$$

$$k = 1.00 \text{ in}$$

$$k = 25.4 \text{ mm}$$

$$s = 0.06 \text{ in}$$

$$s = 1.6 \text{ mm}$$

$$b_{min} = 2.29 \text{ in}$$

$$b_{min} = 58.0 \text{ mm}$$

$$\text{Check } (b \geq b_{min}) = "...OK"$$

**Slope Information**

Rise	$rise = 0 \text{ in}$	$rise = 0$
Run	$run = 703.5 \text{ in}$	$run = 17.869 \text{ m}$
Guardrail Angle	$\phi = 0^\circ$	
Amplification Factor	$\alpha_1 = 1$	

**Factored Loads**

Factored Moment	$M_f = 1 \text{ K\_ft}$	$M_f = 1.4 \text{ kN\_m}$
Factored Shear	$V_f = 2 \text{ K}$	$V_f = 8.9 \text{ kN}$

**Welding**

Designation (Welding Electrode)	$desI_w = \text{"E70xx"}$	$desM_w = \text{"E49xx"}$
Ultimate Strength (Welding Electrode)	$X_u = 70 \text{ Ksi}$	$X_u = 483 \text{ MPa}$
Designation (Fillet Weld Size)	$desI_D = \text{"1/4"}$	$desM_D = \text{" "}$
Fillet Weld Size	$D = 0.25 \text{ in}$	$D = 6.35 \text{ mm}$
Minimum Weld Capacity	$V_{rw} = 22.2 \text{ Ksi}$	$V_{rw} = 153.2 \text{ MPa}$

**Section Properties of Weld:**

Area	$A_w = 1.50 \text{ in}^2$	$A_w = 968 \text{ mm}^2$
Moment of Inertia	$Ix_w = 0.70 \text{ in}^4$	$Ix_w = 2.90 \cdot 10^5 \text{ mm}^4$
Section Modulus	$Sx_w = 0.64 \text{ in}^3$	$Sx_w = 10557 \text{ mm}^3$

**Weld Stresses**

Stress due to Shear	$\sigma_v = 1.3 \text{ Ksi}$	$\sigma_v = 9.2 \text{ MPa}$
Stress due to Flexure	$\sigma_f = 18.6 \text{ Ksi}$	$\sigma_f = 128.4 \text{ MPa}$
Combined Stress	$\sigma = 18.7 \text{ Ksi}$	$\sigma = 128.8 \text{ MPa}$

$$Check \left( V_{rw} \geq \sigma \right) = \text{"...OK"}$$

$$Check \left( \frac{V_{rw}}{\phi_s} \geq \sigma \right) = \text{"...OK"} \quad \text{Allow for Overload}$$

**Moment Resistance**

C Section	$M_{rc} = 34.9 \text{ K\_in}$	$M_{rc} = 3949 \text{ kN\_mm}$
HSSc Section	$M_{rp} = 13.3 \text{ K\_in}$	$M_{rp} = 1501 \text{ kN\_mm}$
Weld	$M_{rw} = 14.3 \text{ K\_in}$	$M_{rw} = 1617 \text{ kN\_mm}$
Minimum	$M_r = 13.3 \text{ K\_in}$	$M_r = 1501 \text{ kN\_mm}$

$$Check \left( M_r \geq M_f \right) = \text{"...OK"}$$

$$Check \left( \frac{M_r}{\phi_s} \geq M_f \right) = \text{"...OK"} \quad \text{Allow for Overload}$$