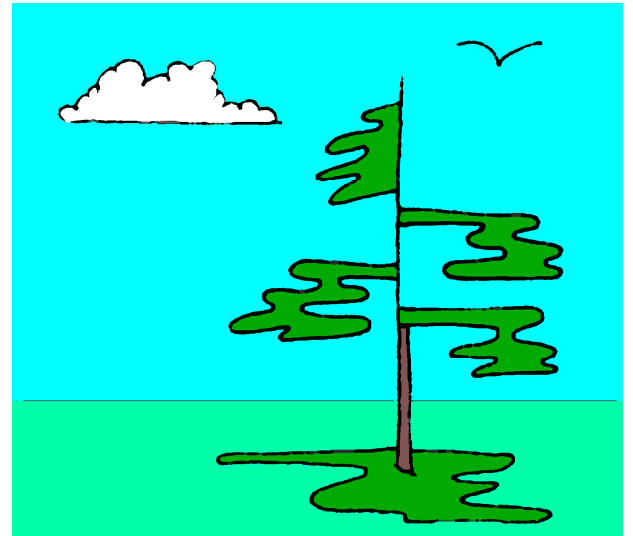


NorthWoods Software



Program Name: Rectangular Beam

Project Name: -

Project Number: -

Project Description: -

Project Designer: Dik

Last Revised (yy-mm-dd): 18-07-29

Reference: Reference?

Created using SMath Studio, a MathCAD workalike from <https://en.smath.info/view/SMathStudio>
The User is responsible to verify data using an alternative method

Menu:

..... Enter Data Space
 Important Output
 Logical Constructs
 Blue Text: Units
..... Summation

Defined Units:

$ft_K := kip\ ft$ Kip-feet (Moment)
 $deg := \frac{\pi}{180} rad$
 $K := kip$ Kips (force)
 $ft_K := ft\ kip$ foot-Kips (Moment)

User Defined Functions:

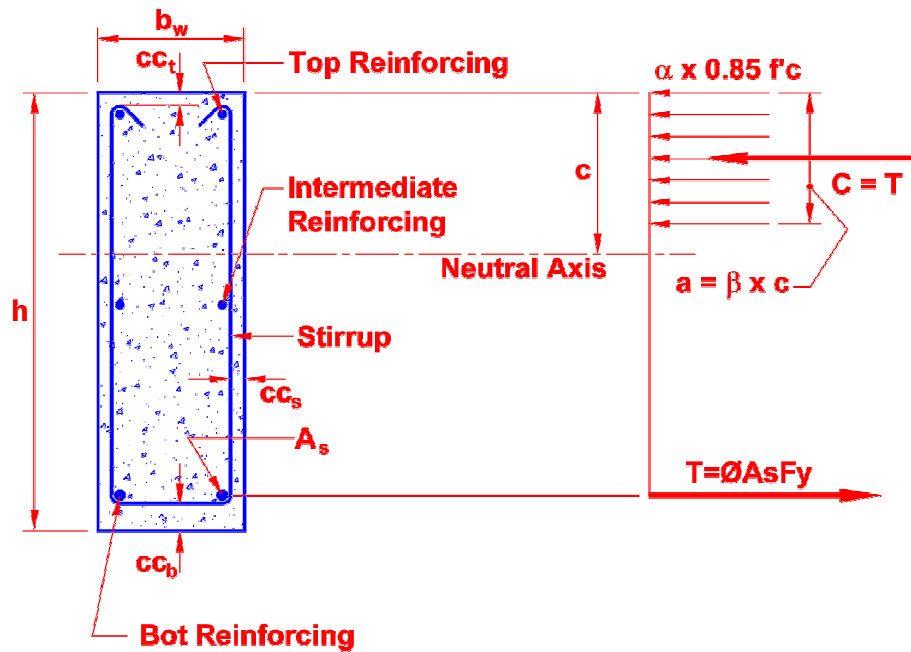
```

ceil(arg1) := if round(arg1, 0) < arg1
               round(arg1, 0) + 1
             else
               round(arg1, 0)
  
```

```

Check(arg) := if arg = 1
               Check := "...OK"
             else
               Check := "...NG"
  
```

$Check(2 = 3) = "...NG"$
 $Check(2 \leq 3) = "...OK"$
 $Check(3 \geq 2) = "...OK"$



Material Resistance Factors:

$$\Phi_s := 0.85$$

Material Factor for Reinforcing Steel

$$\Phi_c := 0.65$$

Material Factor for Concrete 8.4.2

Reinforcing Steel Properties:

1	2	3	4	5	6	1	NDX
1	"10M"	11.3 mm	100 mm ²	35.5 mm	0.785 $\frac{\text{kg}}{\text{m}}$	2	Bar Size
2	"15M"	16.0 mm	200 mm ²	50.1 mm	1.570 $\frac{\text{kg}}{\text{m}}$	3	Bar Diameter (mm)
3	"20M"	19.5 mm	300 mm ²	61.3 mm	2.355 $\frac{\text{kg}}{\text{m}}$	4	Bar Area (mm ²)
4	"25M"	25.2 mm	500 mm ²	79.2 mm	3.925 $\frac{\text{kg}}{\text{m}}$	5	Bar Perimeter (mm)
5	"30M"	29.9 mm	700 mm ²	93.9 mm	5.495 $\frac{\text{kg}}{\text{m}}$	6	Bar Mass/Length (kg/m)
6	"35M"	35.7 mm	1000 mm ²	112.2 mm	7.850 $\frac{\text{kg}}{\text{m}}$		
7	"45M"	43.7 mm	1500 mm ²	137.3 mm	11.775 $\frac{\text{kg}}{\text{m}}$		
8	"55M"	56.4 mm	2500 mm ²	177.2 mm	19.625 $\frac{\text{kg}}{\text{m}}$		

Rebar :=

Input Data:**Materials****Reinforcing Steel Properties**

$f_y := 300 \text{ MPa}$

$f_y = 43.5 \text{ ksi}$

Reinforcing Steel Yield Strength

$E_s := 200000 \text{ MPa}$

$E_s = 29007.5 \text{ ksi}$

Steel Modulus of Elasticity (8.5.4.1)

Concrete

$f'_c := 22 \text{ MPa}$

$f'_c = 3.2 \text{ ksi}$

28 Day Concrete Compressive Strength

$\gamma_c := 2500 \frac{\text{kg}}{\text{m}^3}$

Density of Concrete

 $\lambda = 1.00$ Regular Weight Concrete 2150=2500 $\lambda = 0.85$ Semi-Low Density Concrete 1850-2150 $\lambda = 0.75$ Low Density Concrete less than 1850**Concrete Density Factor**

$\lambda := 1.00$

Minimum Coarse Aggregate Size

$a_g := 20 \text{ mm}$

$a_g = 0.787 \text{ in}$

Coarse Aggregate Size

Temperature Reinforcing

$P_{ts} := .2 \%$

Minimum % Temperature Steel

Reinforcing**Top Reinforcing**

$NDX_t := 2$

$N_t := 2$

NDX	1	2	3	4	5	6	7	8
	10M	15M	20M	25M	30M	35M	45M	55M

Enter Index Number Representing Top Bar Size
Number of Top Bars

$Bar_t := \text{Rebar}_{NDX_t 2}$

$Bar_t = "15M"$

$A_{st} := \text{Rebar}_{NDX_t 4} \cdot N_t$

$A_{st} = 0.62 \text{ in}^2$

$A_{st} = 400 \text{ mm}^2$

$\phi_t := \text{Rebar}_{NDX_t 3}$

$\phi_t = 0.63 \text{ in}$

$\phi_t = 16 \text{ mm}$

Intermediate (Skin) Reinforcing

$NDX_i := 1$

Enter Index Number Representing Bot Bar Size

$S_i := 8 \text{ in}$

$S_i = 203 \text{ mm}$

Maximum Spacing of Intermediate Bars

$N_i := 0$

Initialise Total Number of Intermediate Bars (1/2 ES)

$Bar_i := \text{Rebar}_{NDX_i 2}$

$Bar_i = "10M"$

$A_{si} := \text{Rebar}_{NDX_i 4}$

$A_{si} = 0.155 \text{ in}^2$

$A_{si} = 100 \text{ mm}^2$

$A_{si_prov} := A_{si} \cdot N_i$

$A_{si_prov} = 0 \text{ in}^2$

$A_{si_prov} = 0 \text{ mm}^2$

$$\varphi_i := \text{Rebar}_{NDX_i \ 3}$$

$$\varphi_i = 0.445 \text{ in}$$

$$\varphi_i = 11.3 \text{ mm}$$

Bottom Reinforcing

$$NDX_b := 2 \quad N_b := 2$$

Enter Index Number Representing Bot Bar Size
Number of Bot Bars

$$Bar_b := \text{Rebar}_{NDX_b \ 2}$$

$$Bar_b = "15M"$$

$$A_{sb} := \text{Rebar}_{NDX_t \ 4} \cdot N_t$$

$$A_{sb} = 0.62 \text{ in}^2$$

$$A_{sb} = 400 \text{ mm}^2$$

$$\varphi_b := \text{Rebar}_{NDX_b \ 3}$$

$$\varphi_b = 0.63 \text{ in}$$

$$\varphi_b = 16 \text{ mm}$$

Stirrup Reinforcing

$$NDX_s := 1 \quad N_L := 2$$

Enter Index Number Representing Stirrup Bar Size
Number of Stirrup Legs / Tie

$$N_s := 1$$

Number of Ties / Spacing

$$s_s := 24 \text{ in} \quad s_s = 610 \text{ mm}$$

Stirrup Spacing

$$Bar_s := \text{Rebar}_{NDX_s \ 2}$$

$$Bar_s = "10M"$$

$$A_{ss} := \text{Rebar}_{NDX_s \ 4} \cdot N_L \cdot N_s$$

$$A_{ss} = 0.31 \text{ in}^2$$

$$A_{ss} = 200 \text{ mm}^2$$

$$\varphi_s := \text{Rebar}_{NDX_s \ 3}$$

$$\varphi_s = 0.445 \text{ in}$$

$$\varphi_s = 11.3 \text{ mm}$$

Beam Data:

$$b_w := 9 \text{ in} \quad b_w = 229 \text{ mm}$$

Beam Width

$$h := 29 \text{ in} \quad h = 737 \text{ mm}$$

Beam Depth

$$b_t := b_w \quad b_t = 229 \text{ mm}$$

Width of Beam Tension Zone (Rectangular Beam)

$$cc_t := 1.50 \text{ in} \quad cc_t = 38 \text{ mm}$$

Clear Cover to Top Reinforcing

$$cc_b := 3.0 \text{ in} \quad cc_b = 76 \text{ mm}$$

Clear Cover to Bottom Reinforcing

$$cc_s := 1.5 \text{ in} \quad cc_s = 38 \text{ mm}$$

Clear Cover to Side Reinforcing

$$\alpha_f := 90^\circ$$

Input Loads

$$V_f := 1 \text{ K} \quad V_f = 4.4 \text{ kN} \quad \text{Factored Design Shear}$$

$$V_p := 0 \text{ K} \quad V_p = 0 \text{ kN} \quad \text{Factored Prestressing Shear}$$

$$M_f := 20 \text{ ft_K} \quad M_f = 27.1 \text{ kN m} \quad \text{Factored Design Moment}$$

Calculations:**Calculate Alpha (Equation 10.1)**

$$\alpha_1 := \max \left[\left[0.85 - 0.0015 \cdot \frac{f'_c}{\text{MPa}} \quad 0.67 \right] \right] \quad \alpha_1 = 0.817$$

Calculate Beta (Equation 10.2)

$$\beta_1 := \max \left[\left[0.97 - 0.0025 \cdot \frac{f'_c}{\text{MPa}} \quad 0.67 \right] \right] \quad \beta_1 = 0.915$$

Concrete Modulus of Rupture (Equation 8.3)

$$f_r := 0.6 \cdot \lambda \cdot \sqrt{\frac{f'_c}{\text{MPa}}} \quad \text{MPa} \quad f_r = 2.8142 \text{ MPa} \quad f_r = 0.408 \text{ ksi}$$

Concrete Modulus of Elasticity (Equation 8.1)

$$\text{if } \left(\gamma_c < 1500 \frac{\text{kg}}{\text{m}^3} \right) \vee \left(\gamma_c > 2500 \frac{\text{kg}}{\text{m}^3} \right) \\ E_c := 0.0 \\ \text{else} \\ E_c := \left(3300 \cdot \sqrt{\frac{f'_c}{\text{MPa}}} + 6900 \right) \cdot \left(\frac{\gamma_c}{2300} \right)^{1.5} \quad \text{MPa} \\ E_c = 3678 \text{ ksi} \quad E_c = 25360 \text{ MPa}$$

Alternative Modulus of Elasticity (Equation 8.2)

$$E_{ca} := 4500 \cdot \sqrt{\frac{f'_c}{\text{MPa}}} \quad \text{MPa} \quad E_{ca} = 3061 \text{ ksi} \quad E_{ca} = 21107 \text{ MPa}$$

Beam 'd' to Reinforcing

$$d_t := h - c c_t - \varphi_s - \frac{\varphi_t}{2} \quad d_t = 26.7 \text{ in} \quad d_t = 679 \text{ mm}$$

$$d_b := h - c c_b - \varphi_s - \frac{\varphi_b}{2} \quad d_b = 25.2 \text{ in} \quad d_b = 641 \text{ mm}$$

Minimum Beam Width

$$s := \max \left(\left[30 \text{ mm} \quad 1.4 \cdot a_g \quad 1.4 \cdot \varphi_b \quad 1.4 \cdot \varphi_t \right] \right)$$

$$s = 1.1811 \text{ in}$$

$$s = 30 \text{ mm}$$

$$b_{w_min} := \max \left(\left[\left(2 \cdot (c c_s + \varphi_s) + (N_b \cdot \varphi_b + (N_b - 1) \cdot s) \right) \left(2 \cdot (c c_s + \varphi_s) + (N_t \cdot \varphi_t + (N_t - 1) \cdot s) \right) \right] \right)$$

$$b_{w_min} = 6.3 \text{ in}$$

$$b_{w_min} = 160.8 \text{ mm}$$

'Mr' for Specified Reinforcing**'Mr' for Continuous Span Condition**

$$a_t := \frac{\Phi_s \cdot (A_{st}) \cdot f_y}{\alpha_1 \cdot \Phi_c \cdot f'_c \cdot b_w}$$

$$a_t = 1.5036 \text{ in}$$

$$a_t = 38.2 \text{ mm}$$

$$M_{rt} := \Phi_s \cdot (A_{st}) \cdot f_y \cdot \left(d_t - \frac{a_t}{2} \right)$$

$$M_{rt} = 49.7 \text{ ft_K}$$

$$M_{rt} = 67.3 \text{ kN m}$$

'Mr' for Simple Span or End Span Condition

$$a_b := \frac{\Phi_s \cdot (A_{sb}) \cdot f_y}{\alpha_1 \cdot \Phi_c \cdot f'_c \cdot b_w}$$

$$M_{rb} := \Phi_s \cdot (A_{sb}) \cdot f_y \cdot \left(d_b - \frac{a_b}{2} \right)$$

$$M_{rb} = 46.8 \text{ ft_K}$$

$$M_{rb} = 63.4 \text{ kN m}$$

Temperature Reinforcing

$$A_{s_ts} := P_{ts} \cdot b_t \cdot h$$

$$A_{s_ts} = 0.522 \text{ in}^2$$

$$A_{s_ts} = 337 \text{ mm}^2$$

$$A_{s_prov} := A_{sb} + A_{si} + A_{st}$$

$$A_{s_prov} = 1.395 \text{ in}^2$$

$$A_{s_prov} = 900 \text{ mm}^2$$

'Mf' Increased by 1/3

$$M_{incr} := M_f \cdot 1.33$$

$$M_{incr} = 26.6 \text{ ft_K}$$

$$M_{incr} = 36.1 \text{ kN m}$$

Cracking Moment (Equation 10.3)

$$S_x := \frac{b_w \cdot h^2}{6}$$

$$S_x = 1261.5 \text{ in}^3$$

$$S_x = 2.067 \cdot 10^7 \text{ mm}^3$$

$$M_{cr} := f_r \cdot S_x$$

$$M_{cr} = 42.9 \text{ ft_K}$$

$$M_{cr} = 58.2 \text{ kN m}$$

$$M_{f_cr} := 1.2 \cdot M_{cr}$$

$$M_{f_cr} = 51.5 \text{ ft_K}$$

$$M_{f_cr} = 51.5 \text{ ft_K}$$

Minimum Flexural Reinforcing (Equation 10.4)

$$A_{s_min} := 0.2 \cdot \frac{\sqrt{\frac{f'_c}{\text{MPa}}}}{\frac{f_y}{\text{MPa}}} \cdot b_w \cdot h$$

$$A_{s_min} = 0.8161 \text{ in}^2$$

$$A_{s_min} = 527 \text{ mm}^2$$

$$a_{min} := \frac{\Phi_s \cdot (A_{s_min}) \cdot f_y}{\alpha_1 \cdot \Phi_c \cdot f'_c \cdot b_w}$$

$$a_{min} = 1.9792 \text{ in}$$

$$a_{min} = 50.3 \text{ mm}$$

Minimum Moment for Continuous Span Condition (Equation 10.5)

$$M_{r_mint} := \Phi_s \cdot (A_{s_min}) \cdot f_y \cdot \left(d_t - \frac{a_{min}}{2} \right) \quad M_{r_mint} = 64.8 \text{ ft_K} \quad M_{r_mint} = 87.8 \text{ kN m}$$

Minimum Moment for Simple Span or End Span Condition (Equation 10.5)

$$M_{r_minb} := \Phi_s \cdot (A_{s_min}) \cdot f_y \cdot \left(d_b - \frac{a_{min}}{2} \right) \quad M_{r_minb} = 61 \text{ ft_K} \quad M_{r_minb} = 82.7 \text{ kN m}$$

Minimum Design Moment for Continuous Span Condition

Mf = Factored Design Moment

Mr = Design Moment Resistance with Specified Reinforcing

Mincr = Factored Design Moment increased by 1/3

Mf_cr = 1.2 x Cracking Moment

Mr_min = Minimum Moment based on Min Flexural Reinforcement

Mdes = Design Moment

```

if Mf < Mr_mint
  if Mincr < Mr_mint
    Mdest := Mincr
  else
    Mdest := Mr_mint
else
  Mdest := Mf

```

$$M_f = 20 \text{ ft_K}$$

$$M_{rt} = 49.7 \text{ ft_K}$$

$$M_{r_mint} = 64.8 \text{ ft_K} \quad M_{incr} = 26.6 \text{ ft_K}$$

$$M_{f_cr} = 51.5 \text{ ft_K} \quad M_{dest} = 26.6 \text{ ft_K}$$

```

if Mdest < Mf_cr
  Mdest := Mf_cr
else
  dummy := 0

```

$$M_{dest} = 51.5 \text{ ft_K}$$

```

if  $M_f < M_{r\_minb}$ 
  if  $M_{incr} < M_{r\_minb}$ 
     $M_{desb} := M_{incr}$ 
  else
     $M_{desb} := M_{r\_minb}$ 
else
   $M_{desb} := M_f$ 

if  $M_{desb} < M_{f\_cr}$ 
   $M_{desb} := M_{f\_cr}$ 
else
  dummy := 0

```

$M_f = 20 \text{ ft_K}$ $M_{rb} = 46.8 \text{ ft_K}$
 $M_{r_minb} = 61 \text{ ft_K}$ $M_{incr} = 26.6 \text{ ft_K}$
 $M_{f_cr} = 51.5 \text{ ft_K}$ $M_{desb} = 26.6 \text{ ft_K}$
 $M_{dest} = 51.5 \text{ ft_K}$

Balanced Condition for Continuous Span Condition (Equation 10.5)

$$c_{bal} := \frac{700}{700 + \frac{f_y}{\text{MPa}}} \cdot d_t$$

$c_{bal} = 18.7181 \text{ in}$ $c_{bal} = 475 \text{ mm}$

Depth of Compression Block

$$a_{bal} := c_{bal} \cdot \beta_1$$

$a_{bal} = 17.1271 \text{ in}$ $a_{bal} = 435 \text{ mm}$

Compression Force

$$C_{bal} := \alpha_1 \cdot \Phi_c \cdot f'_c \cdot b_w \cdot a_{bal}$$

$C_{bal} = 261.2 \text{ K}$ $C_{bal} = 1161.9 \text{ kN}$

Area of Steel for Balanced Condition

$$A_{s_bal} := \frac{C_{bal}}{\Phi_s \cdot f_y}$$

$A_{s_bal} = 7.0623 \text{ in}^2$ $A_{s_bal} = 4556 \text{ mm}^2$

Balanced Moment

$$M_{bt} := \Phi_s \cdot A_{s_bal} \cdot f_y \cdot \left(d_t - \frac{a_{bal}}{2} \right)$$

$M_{bt} = 395.6 \text{ ft_K}$ $M_{bt} = 536.4 \text{ kN m}$

Balanced Condition for Simple Span or End Span Condition (Equation 10.5)

$$c_{bal} := \frac{700}{700 + \frac{f_y}{\text{MPa}}} \cdot d_b$$

$c_{bal} = 17.6681 \text{ in}$ $c_{bal} = 449 \text{ mm}$

Depth of Compression Block

$$a_{bal} := c_{bal} \cdot \beta_1$$

$$a_{bal} = 16.1663 \text{ in}$$

$$a_{bal} = 411 \text{ mm}$$

Compression Force

$$C_{bal} := \alpha_1 \cdot \Phi_c \cdot f'_c \cdot b_w \cdot a_{bal}$$

$$C_{bal} = 246.5 \text{ K}$$

$$C_{bal} = 1096.7 \text{ kN}$$

Area of Steel for Balanced Condition

$$A_{s_bal} := \frac{C_{bal}}{\Phi_s \cdot f_y}$$

$$A_{s_bal} = 6.6661 \text{ in}^2$$

$$A_{s_bal} = 4301 \text{ mm}^2$$

Balanced Moment

$$M_{bb} := \Phi_s \cdot A_{s_bal} \cdot f_y \cdot \left(d_b - \frac{a_{bal}}{2} \right)$$

$$M_{bb} = 352.5 \text{ ft_K}$$

$$M_{bb} = 477.9 \text{ kN m}$$

Crack Control for Continuous Span Condition (10.6.1) and Equation 10.6

$$d_c := h - d_t$$

$$d_c = 2.2598 \text{ in}$$

$$d_c = 57 \text{ mm}$$

$$y_t := d_c$$

$$y_t = 2.2598 \text{ in}$$

$$y_t = 57 \text{ mm}$$

$$A := \frac{2 \cdot y_t \cdot b_w}{N_t}$$

$$A = 20.3386 \text{ in}^2$$

$$A = 13122 \text{ mm}^2$$

$$f_s := 0.6 \cdot f_y$$

$$f_s = 26.1068 \text{ ksi}$$

$$f_s = 180 \text{ MPa}$$

$$z_t := \frac{f_s}{\text{MPa}} \cdot \left(\frac{d_c \cdot A}{3} \right)^{\frac{1}{3}} \frac{\text{N}}{\text{mm}}$$

$$z_t = 16377 \frac{\text{N}}{\text{mm}}$$

$$\text{Exp01} := [\text{"Exterior"} \text{"Interior"} \text{"Not Permitted"}]$$

```

if  $z_t \leq 25000 \frac{\text{N}}{\text{mm}}$ 
  Exposurect := Exp011
else
  if  $z_t \leq 30000 \frac{\text{N}}{\text{mm}}$ 
    Exposurect := Exp012
  else
    Exposurect := Exp013

```

$$\text{Exposure}_{ct} = \text{"Exterior"}$$

Crack Control for Simple Span or End Span Condition (10.6.1) and Equation 10.6

$$d_c := h - d_b$$

$$d_c = 3.7598 \text{ in} \quad d_c = 96 \text{ mm}$$

$$y_b := d_c$$

$$y_t = 2.2598 \text{ in} \quad y_t = 57 \text{ mm}$$

$$A := \frac{2 \cdot y_b \cdot b_w}{N_b}$$

$$A = 33.8386 \text{ in}^2 \quad A = 21831 \text{ mm}^2$$

$$f_s := 0.6 \cdot f_y$$

$$f_s = 26.1068 \text{ ksi} \quad f_s = 180 \text{ MPa}$$

$$z_b := \frac{f_s}{\text{MPa}} \cdot \left(\frac{d_c \cdot A}{3} \right)^{\frac{1}{3}} \frac{\text{N}}{\text{mm}}$$

$$z_b = 22995 \frac{\text{N}}{\text{mm}}$$

```

if z_b ≤ 25000  $\frac{\text{N}}{\text{mm}}$ 
  Exposurecb := Exp011
else
  if z_b ≤ 30000  $\frac{\text{N}}{\text{mm}}$ 
    Exposurecb := Exp012
  else
    Exposurecb := Exp013

```

Exposure_{cb} = "Exterior"

Skin Reinforcing for Continuous Span Condition (10.6.2)**Rebar Size for Skin Reinforcing:**

$$x := cc_s + \varphi_s + \frac{\varphi_i}{2}$$

$$x = 2.1673 \text{ in} \quad x = 55 \text{ mm}$$

$$d_{skin} := \left(\frac{h}{2} - 2 \cdot (h - d_t) \right)$$

$$d_{skin} = 9.9803 \text{ in} \quad d_{skin} = 254 \text{ mm}$$

$$N_{skin} := \text{ceil} \left(\frac{d_{skin}}{S_i} \right)$$

$$N_{skin} = 2$$

$$A_{cst} := d_{skin} \cdot x$$

$$A_{cst} = 21.6306 \text{ in}^2 \quad A_{cst} = 13955 \text{ mm}^2$$

```

if h > 750 mm
  if  $z_t \leq 25000 \frac{\text{N}}{\text{mm}}$ 
     $\rho_{sk} := 0.010$ 
     $A_{cst} := \rho_{sk} \cdot A_{cst}$ 
     $N_{it} := \max \left( \left[ \frac{A_{cst}}{A_{si}} N_{skin} \right] \right)$ 
     $A_{cst\_prov} := N_{it} \cdot A_{si} \cdot 2$ 
  else
    if  $z_t \leq 30000 \frac{\text{N}}{\text{mm}}$ 
       $\rho_{sk} := 0.008$ 
       $A_{cst} := \rho_{sk} \cdot A_{cst}$ 
       $N_{it} := \max \left( \left[ \frac{A_{cst}}{A_{si}} N_{skin} \right] \right)$ 
       $A_{cst\_prov} := N_{it} \cdot A_{si} \cdot 2$ 
    else
       $\rho_{sk} := 0.010$ 
       $A_{cst} := \rho_{sk} \cdot A_{cst}$ 
       $N_{it} := \max \left( \left[ \frac{A_{cst}}{A_{si}} N_{skin} \right] \right)$ 
       $A_{cst\_prov} := N_{it} \cdot A_{si} \cdot 2$ 
  else
     $\rho_{sk} := 0.0$ 
     $A_{cst} := 0.0$ 
     $N_{it} := 0$ 
     $A_{cst\_prov} := 0$ 

```

$$N_{it} = 0$$

$$A_{cst} = 0 \text{ in}^2$$

$$A_{cst} = 0 \text{ mm}^2$$

$$A_{cst_prov} = 0 \text{ in}^2$$

$$A_{cst_prov} = 0 \text{ mm}^2$$

Skin Reinforcing for Simple Span or End Span Condition (10.6.2)

$$x := cc_s + \varphi_s + \frac{\varphi_i}{2}$$

$$x = 2.1673 \text{ in}$$

$$x = 55 \text{ mm}$$

$$d_{skin} := \left(\frac{h}{2} - 2 \cdot (h - d_b) \right)$$

$$d_{skin} = 6.9803 \text{ in}$$

$$d_{skin} = 177 \text{ mm}$$

$$N_{skin} := \text{ceil} \left(\frac{d_{skin}}{S_i} \right)$$

$$N_{skin} = 1$$

$$A_{csb} := d_{skin} \cdot x$$

$$A_{csb} = 15.1286 \text{ in}^2$$

$$A_{csb} = 9760 \text{ mm}^2$$

```

if h > 750 mm
  if  $z_b \leq 25000 \frac{\text{N}}{\text{mm}}$ 
     $\rho_{sk} := 0.010$ 
     $A_{csb} := \rho_{sk} \cdot A_{csb}$ 
     $N_{ib} := \max \left( \left[ \frac{A_{csb}}{A_{si}} N_{skin} \right] \right)$ 
     $A_{csb\_prov} := N_{ib} \cdot A_{si} \cdot 2$ 
  else
    if  $z_t \leq 30000 \frac{\text{N}}{\text{mm}}$ 
       $\rho_{sk} := 0.008$ 
       $A_{csb} := \rho_{sk} \cdot A_{csb}$ 
       $N_{ib} := \max \left( \left[ \frac{A_{csb}}{A_{si}} N_{skin} \right] \right)$ 
       $A_{csb\_prov} := N_{ib} \cdot A_{si} \cdot 2$ 
    else
       $\rho_{sk} := 0.10$ 
       $A_{csb} := \rho_{sk} \cdot A_{csb}$ 
       $N_{ib} := \max \left( \left[ \frac{A_{csb}}{A_{si}} N_{skin} \right] \right)$ 
       $A_{csb\_prov} := N_{ib} \cdot A_{si} \cdot 2$ 
    else
       $\rho_{sk} := 0.0$ 
       $A_{csb} := 0.0$ 
       $N_{ib} := 0$ 
       $A_{csb\_prov} := 0$ 

```

$$N_{ib} = 0$$

$$A_{csb} = 0 \text{ in}^2$$

$$A_{csb_prov} = 0 \text{ in}^2$$

$$A_{csb} = 0 \text{ mm}^2$$

$$A_{csb_prov} = 0 \text{ mm}^2$$

Summary:

28 Day Concrete Compressive Strength:	$f'_c = 3.2 \text{ ksi}$	$f'_c = 22 \text{ MPa}$
Reinforcing Steel Yield Strength:	$f_y = 43.5 \text{ ksi}$	$f_y = 300 \text{ MPa}$
Beam Width:	$b_w := 9 \text{ in}$	$b_w = 229 \text{ mm}$
Beam Depth:	$h := 24 \text{ in}$	$h = 610 \text{ mm}$
Top Reinforcing	$Bar_t = "15M"$	
As for Top Reinforcing	$A_{st} = 0.62 \text{ in}^2$	$A_{st} = 400 \text{ mm}^2$
Intermediate Reinforcing	$Bar_i = "10M"$	
As for Intermediate Reinforcing	$A_{si_prov} = 0 \text{ in}^2$	$A_{si_prov} = 0 \text{ mm}^2$
Maximum Spacing for Intermediate Rfg	$S_i := 8 \text{ in}$	$S_i = 203 \text{ mm}$
Bottom Reinforcing	$Bar_b = "15M"$	
As for Bottom Reinforcing	$A_{sb} = 0.62 \text{ in}^2$	$A_{sb} = 400 \text{ mm}^2$
Stirrup Reinforcing	$Bar_s = "10M"$	
As for Stirrup Reinforcing	$A_{ss} = 0.31 \text{ in}^2$	$A_{ss} = 200 \text{ mm}^2$
Number of Stirrup Legs / Tie	$N_L := 2$	
Number of Ties / Spacing	$N_S := 1$	
Stirrup Spacing	$s_s = 24 \text{ in}$	$s_s = 609.60 \text{ mm}$
Av Required	See Shear Calculation Sheet for Av	
As (Total) Provided	$A_{s_prov} = 1.395 \text{ in}^2$	$A_{s_prov} = 900 \text{ mm}^2$
As (Temperature Steel) Required:	$A_{s_ts} = 0.522 \text{ in}^2$	$A_{s_ts} = 337 \text{ mm}^2$
As (Minimum Flexural)	$A_{s_min} = 0.816 \text{ in}^2$	$A_{s_min} = 527 \text{ mm}^2$
Design Factored Moment:	$M_f = 20 \text{ ft_K}$	$M_f = 27.1 \text{ kN m}$
Moment for 1.33 x Factored Moment	$M_{incr} = 26.6 \text{ ft_K}$	$M_{incr} = 36.1 \text{ kN m}$
Moment for 1.2 x Cracked Section:	$M_{f_cr} = 51.5 \text{ ft_K}$	$M_{f_cr} = 51.5 \text{ ft_K}$
Moment Capacity Provided (Top):	$M_{rt} = 49.7 \text{ ft_K}$	$M_{rt} = 67.3 \text{ kN m}$
Minimum Moment Capacity Required (Top):	$M_{dest} = 51.5 \text{ ft_K}$	$M_{dest} = 69.8 \text{ kN m}$
Exposure (Top):	$Exposure_{ct} = "Exterior"$	
Skin Reinforcing (Top):	$A_{cst} = 0 \text{ in}^2$	$A_{cst} = 0 \text{ mm}^2$
Moment Capacity Provided (Bottom):	$M_{rb} = 46.8 \text{ ft_K}$	$M_{rb} = 63.4 \text{ kN m}$
Minimum Moment Capacity Required (Bot):	$M_{desb} = 51.5 \text{ ft_K}$	$M_{dest} = 69.8 \text{ kN m}$
Exposure (Bottom):	$Exposure_{cb} = "Exterior"$	
Skin Reinforcing (Bot):	$A_{csb} = 0 \text{ in}^2$	$A_{csb} = 0 \text{ mm}^2$

$Check\left(b_{w_min} \leq b_w\right) = "...OK"$

$Check\left(M_{incr} \leq M_{rt}\right) = "...OK"$

$Check\left(M_{incr} \leq M_{rb}\right) = "...OK"$

$Check\left(M_{rt} \geq M_{dest}\right) = "...NG"$

$Check\left(M_{rb} \geq M_{dest}\right) = "...NG"$

$Check\left(A_{s_prov} \geq A_{s_min}\right) = "...OK"$

$Check\left(M_{rt} \geq M_{f_cr}\right) = "...NG"$