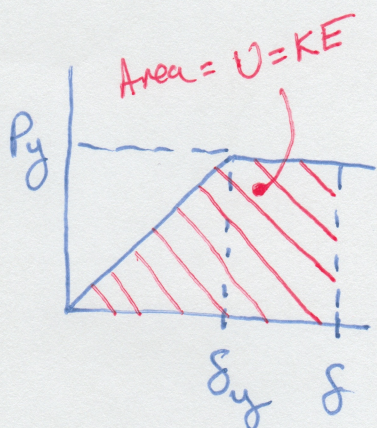


$$\text{Kinetic Energy, } KE = \frac{1}{2} \left[ \frac{W}{g} \right] v^2 \quad (1)$$

Conservation of Energy  $\rightarrow KE = U$

$U = \text{strain energy} = \text{work done by } P$



Assume perfectly elastic-plastic response, where  $P_y$  is the load that causes the post to fully yield.

$$M_y = F_y Z = P_y L \rightarrow P_y = \frac{F_y Z}{L} \quad (2)$$

$$\delta_y = \frac{P_y L^3}{3EI} = \frac{F_y Z L^2}{3EI} \quad (3)$$

$F_y = \text{yield stress}$   
 $Z = \text{plastic modulus}$

Assuming the post yields and continues to deflect, the work done by  $P$  is equal to the area under the  $P$ - $\delta$  graph, which is:

$$U = \frac{1}{2} P_y \delta_y + (\delta - \delta_y) P_y$$

Solve for  $\delta$ :  $\frac{U}{P_y} = \frac{1}{2} \delta_y + \delta - \delta_y \rightarrow \delta = \frac{U}{P_y} + \frac{1}{2} \delta_y$

Setting  $U = KE \Rightarrow (1)$  and  $P_y \Rightarrow (2)$  and  $\delta_y \Rightarrow (3)$ , you can solve for  $\delta$ .