

Shear Flow in Built-up Members



- Members are built-up from several parts which may slide past each other when the member is subjected to bending
- To prevent this sliding fasteners such as nails, bolts or glue may be needed
- In order to design these fasteners or determine their spacing the shear force resisted must be known
- This force is measured per unit length and is called ***shear flow q***

Shear Flow in Built-up Members

Consider the shear force along the juncture where a segment is connected to the flange of a beam.

From equilibrium, the shear force acting on the junction is

$$dF = \frac{dM}{I} \int_{A'} y dA'$$

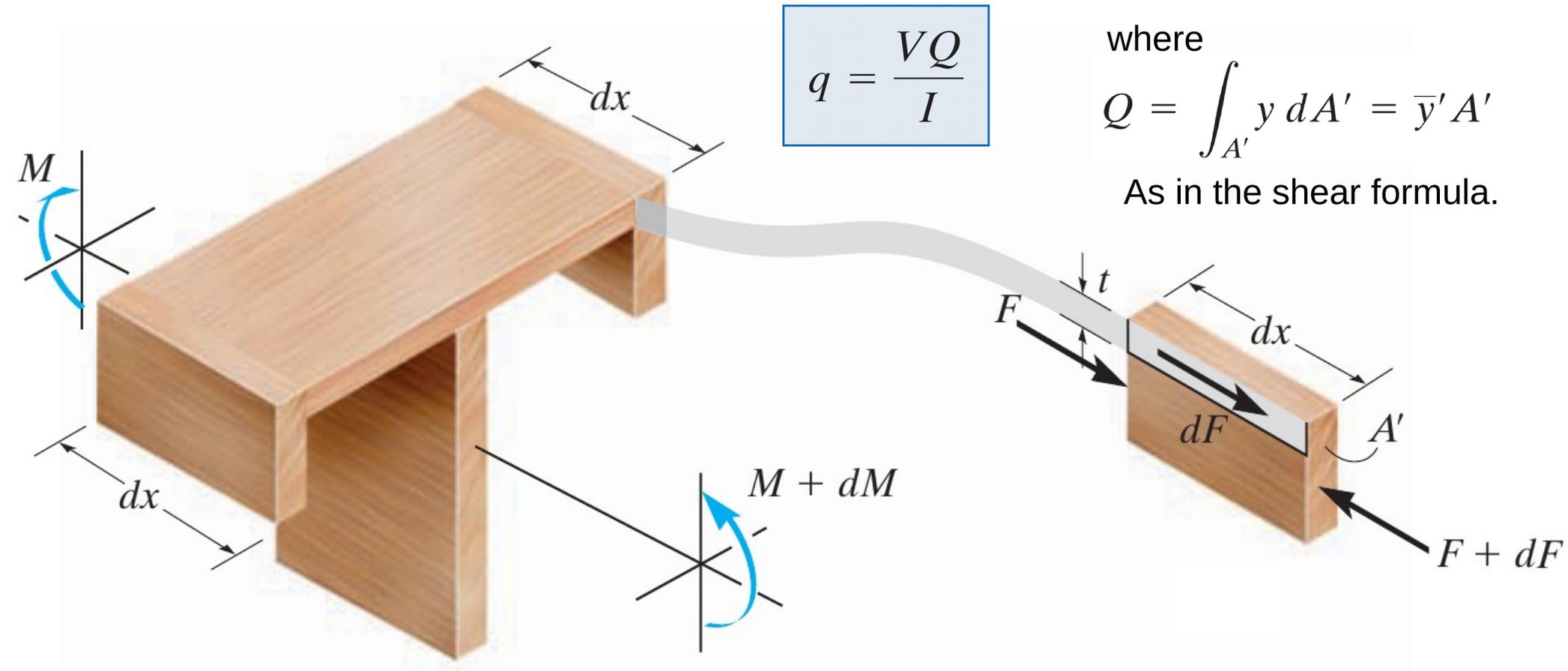
Dividing both sides by dx and noting $dM/dx = V$ we obtain

$$q = \frac{VQ}{I}$$

where

$$Q = \int_{A'} y dA' = \bar{y}' A'$$

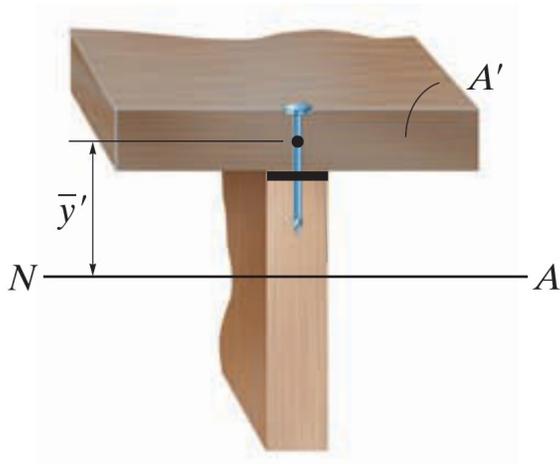
As in the shear formula.



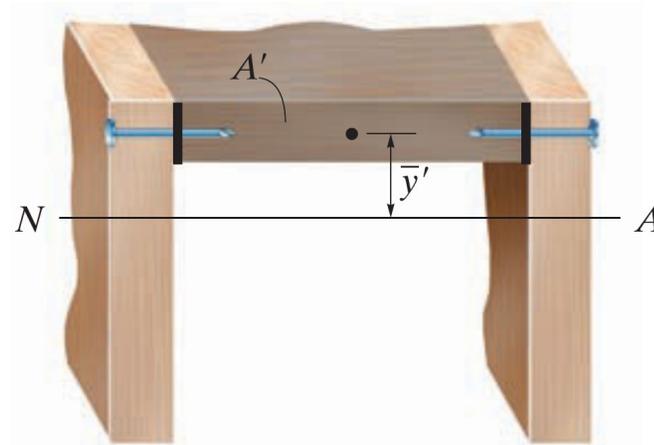
Shear Flow in Built-up Members

It is important to correctly determine Q when computing the shear flow.

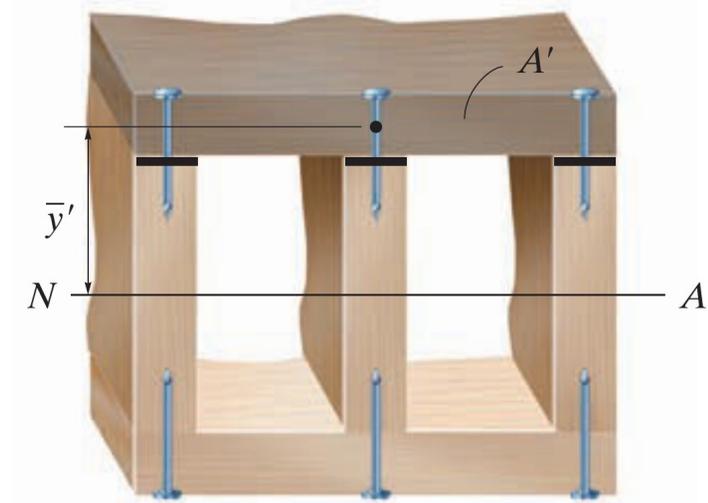
Shaded areas show the areas used to determine Q to compute the shear flow resisted by the fasteners on surface shown with thick segments.



q is resisted by 1 fastener



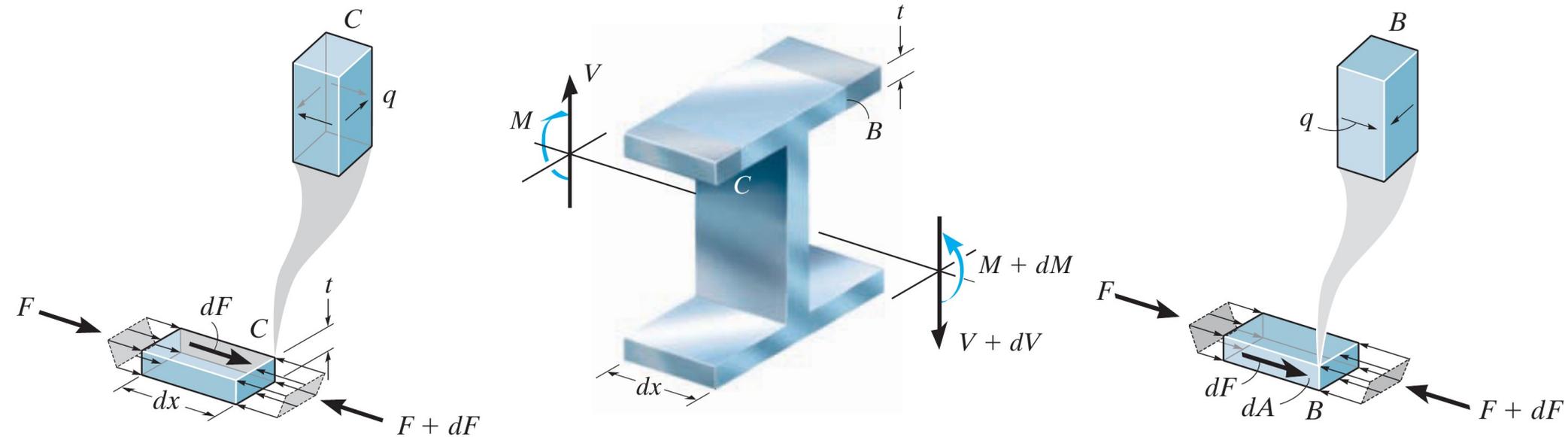
q is resisted by 2 fasteners i.e. $q/2$ is supported by each fastener



q is resisted by 3 fasteners i.e. $q/3$ is supported by each fastener

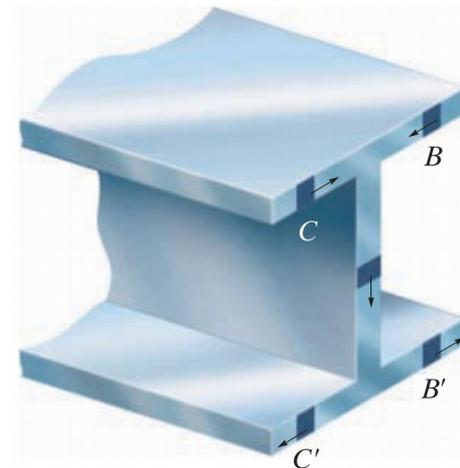
Shear Flow in Thin-Walled Members

Shear flow equation $q = VQ/I$ can be used to find the shear flow distribution throughout a *thin walled* member's cross section.

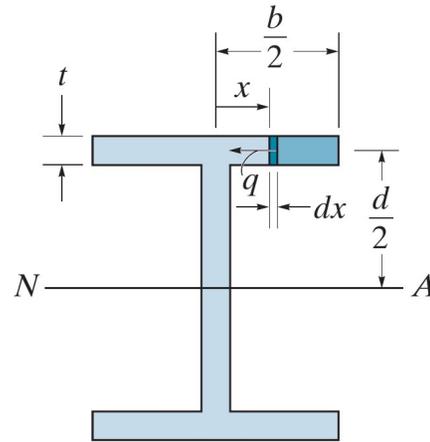
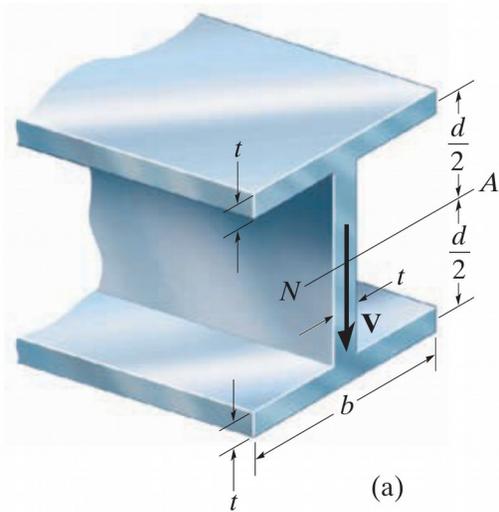


q' assumed to be zero throughout flange thickness since top and bottom of flange are stress free

q assumed constant throughout flange thickness



Shear Flow in Thin-Walled Members

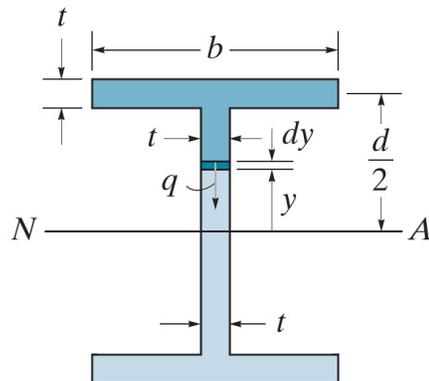


For the flange

$$q = \frac{VQ}{I} = \frac{V[d/2](b/2 - x)t}{I} = \frac{Vtd}{2I} \left(\frac{b}{2} - x \right)$$

$$Q = \bar{y}' A' = [d/2](b/2 - x)t$$

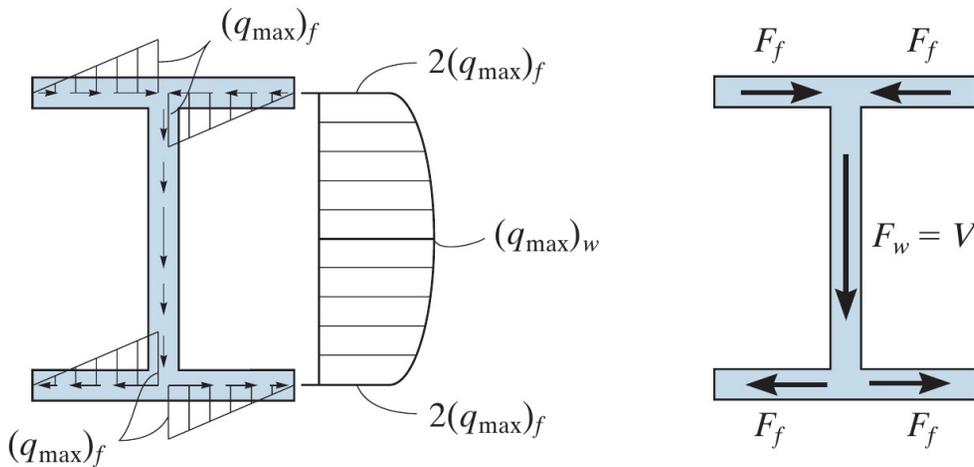
For the web:



$$q = \frac{VQ}{I} = \frac{Vt}{I} \left[\frac{db}{2} + \frac{1}{2} \left(\frac{d^2}{4} - y^2 \right) \right]$$

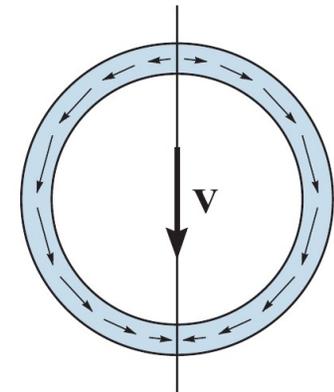
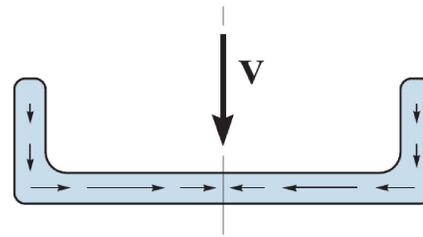
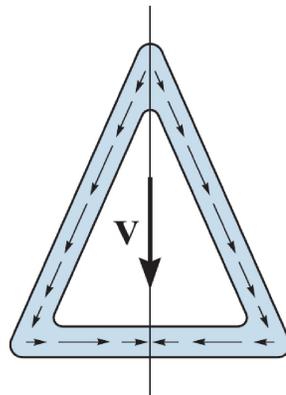
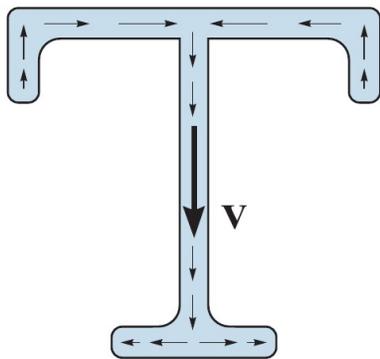
$$\begin{aligned} Q &= \sum \bar{y}' A' = [d/2] (bt) \\ &\quad + [y + (1/2)(d/2 - y)] t(d/2 - y) \\ &= bt(d/2) + (t/2)(d^2/4 - y^2) \end{aligned}$$

Shear Flow in Thin-Walled Members



The shear flow q :

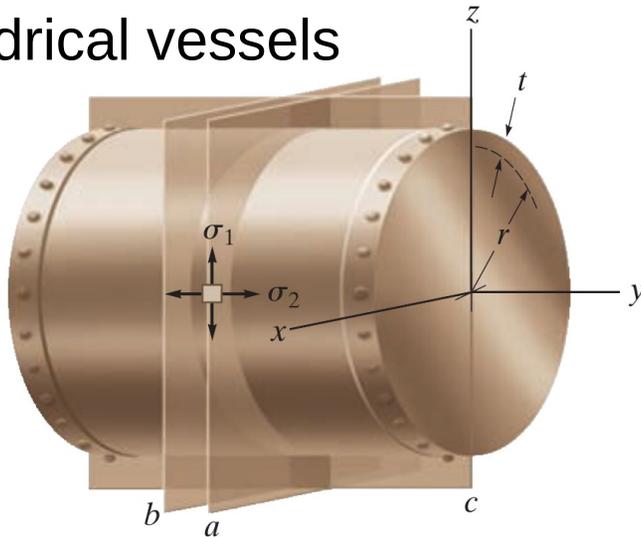
- Varies linearly along the flanges or sections perpendicular to the shear force
- Varies parabolically along inclined segments or segments parallel to the shear force
- Acts always parallel to the walls of the member
- “Flows” inward in the beams top flange, flows downward in the web and outwards in the bottom flange



Thin-Walled Pressure Vessels

- **Thin** wall means the radius over thickness ratio is $r/t \geq 10$
- The stress through thickness is assumed to be uniform (since thickness is small)
- Pressure is the gauge pressure that is above atmospheric pressure

Cylindrical vessels



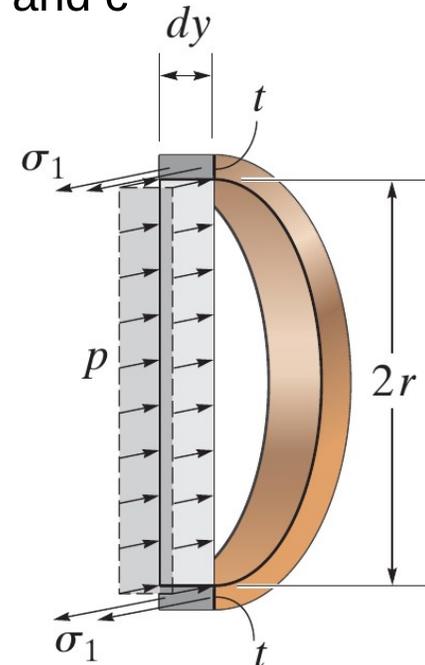
The element is subjected to σ_1 **circumferential** or **hoop** stress and σ_2 **longitudinal** stress

Consider force equilibrium in the x direction of a thin section extracted from the vessel by cutting through planes a, b and c

$$\Sigma F_x = 0$$

$$2[\sigma_1(t dy)] - p(2r dy) = 0$$

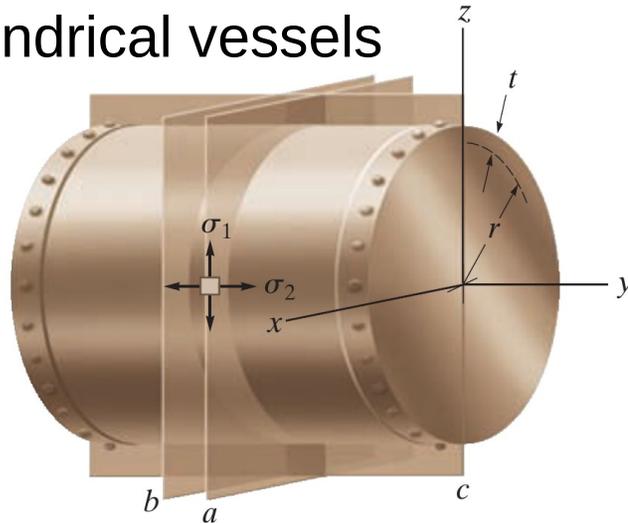
$$\sigma_1 = \frac{pr}{t}$$



Thin-Walled Pressure Vessels

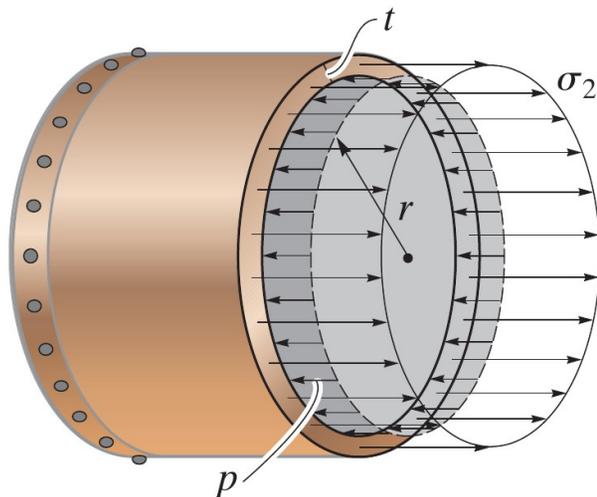
- **Thin** wall means the radius over thickness ratio is $r/t \geq 10$
- The stress through thickness is assumed to be uniform (since thickness is small)
- Pressure is the gauge pressure that is above atmospheric pressure

Cylindrical vessels



The element is subjected to σ_1 **circumferential** or **hoop** stress and σ_2 **longitudinal** stress

Consider force equilibrium in the y (longitudinal) direction of the left portion of the vessel cut by plane b



$$\Sigma F_y = 0 \quad \sigma_2(2\pi r t) - p(\pi r^2) = 0$$

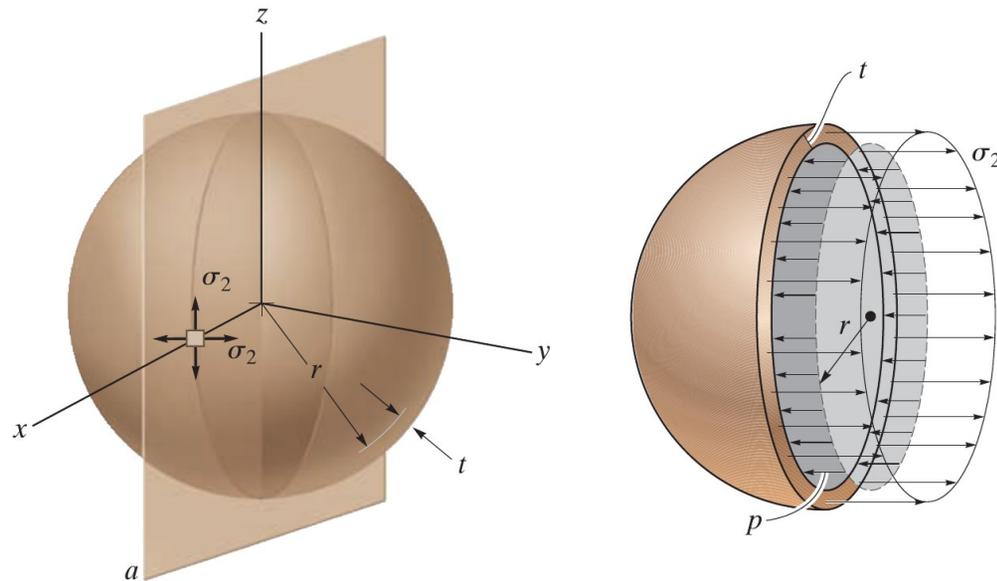
$$\sigma_2 = \frac{pr}{2t}$$

$$\sigma_1 = 2\sigma_2$$

Thin-Walled Pressure Vessels

- **Thin** wall means the radius over thickness ratio is $r/t \geq 10$
- The stress through thickness is assumed to be uniform (since thickness is small)
- Pressure is the gauge pressure that is above atmospheric pressure

Spherical vessels



Consider force equilibrium in the y direction of the left portion of the vessel cut by plane a

$$\Sigma F_y = 0$$

$$\sigma_2(2\pi r t) - p(\pi r^2) = 0$$

$$\sigma_2 = \frac{pr}{2t}$$

The element is subjected to **biaxial** stress $\sigma_1 = \sigma_2$
 σ_3 is neglected, however, varies from $\sigma_3 = p$
inside the vessel to $\sigma_3 = 0$ outside.