

Data	Formulae (IEC 60909-0:2016) and calculation	Impedance Ω
Network feeder Q $U_{nQ} = 110 \text{ kV}$ $I_{kQ}'' = 10,5 \text{ kA}$ $c_Q = c_{\max} = 1,1$ $R_Q = 0,1 \cdot X_Q$	$(6) Z_{Qt} = \frac{c_Q U_{nQ}}{\sqrt{3} \cdot I_{kQ}''} \cdot \frac{1}{t_r^2} = \frac{1,1 \cdot 110 \text{ kV}}{\sqrt{3} \cdot 10,5 \text{ kA}} \cdot \left(\frac{20 \text{ kV}}{110 \text{ kV}} \right)^2$ $X_{Qt} = \frac{Z_{Qt}}{\sqrt{1 + (R_Q/X_Q)^2}} ; R_{Qt} = 0,1 \cdot X_{Qt}$ $\underline{Z}_{Qt} = R_{Qt} + jX_{Qt}$	$Z_{Qt} = 0,2199$ $\underline{Z}_{Qt} = 0,0219 + j0,2188$
Transformer TWP $S_{TWP} = 31,5 \text{ MVA}$ $U_{rTWP HV} = 110 \text{ kV}$ $U_{rTWP LV} = 20 \text{ kV}$ $u_{kr} = 12\%$ $u_{Rr} = 0,6\%$	$(7) Z_{TWP} = \frac{u_{kr}}{100\%} \cdot \frac{U_{rTWP LV}^2}{S_{TWP}} = \frac{12\%}{100\%} \cdot \frac{(20 \text{ kV})^2}{31,5 \text{ MVA}}$ $(8) R_{TWP} = \frac{u_{Rr}}{100\%} \cdot \frac{U_{rTWP LV}^2}{S_{TWP}} = \frac{0,6\%}{100\%} \cdot \frac{(20 \text{ kV})^2}{31,5 \text{ MVA}}$ $(9) X_{TWP} = \sqrt{Z_{TWP}^2 - R_{TWP}^2}$ $\underline{Z}_{TWP} = R_{TWP} + jX_{TWP}$ $(12a) K_T = \frac{0,95 \cdot c_{\max}}{1 + 0,6 \cdot X_{TWP}} = \frac{0,95 \cdot 1,1}{1 + 0,6 \cdot 0,11985} = 0,9749$ $\underline{Z}_{TWPk} = K_T \underline{Z}_{TWP}$	$Z_{TWP} = 1,5238$ $R_{TWP} = 0,0762$ $X_{TWP} = 1,5219$ $\underline{Z}_{TWP} = 0,0762 + j1,5219$ $\underline{Z}_{TWPk} = 0,0743 + j1,4837$
Wind Power Station Units WD $S_{rWD} = 2,5 \text{ MVA}$ $U_{rWD} = U_{rTWD HV} = 20 \text{ kV}$ $i_{WD \max} = 388 \text{ A}$ $I_{kWD \max} = 1,2 \cdot I_{rWD}^a$ $\kappa_{WD} = 1,7 ; R_{WD} = 0,1 X_{WD}$	$(28) Z_{WD} = \frac{\sqrt{2} \cdot \kappa_{WD} \cdot U_{rTWD HV}}{\sqrt{3} \cdot i_{WD \max}} = \frac{\sqrt{2} \cdot 1,7 \cdot 20 \text{ kV}}{\sqrt{3} \cdot 0,388 \text{ kA}}$ $(29) \underline{Z}_{WD} = (R_{WD} + jX_{WD}) \cdot \frac{Z_{WD}}{\sqrt{1 + (R_{WD}/X_{WD})^2}}$	$Z_{WD} = 71,5487$ $\underline{Z}_{WD} = 7,1194 + j71,1936$
Wind Power Station Units WF $S_{rWF} = 2,5 \text{ MVA}$ $U_{rWF} = 20 \text{ kV}$ $I_{skWF} = I_{kWF \max} = 1,3 \cdot I_{rWF}^b$	$I_{rWF} = \frac{S_{rWF}}{\sqrt{3} \cdot U_{rWF}} = \frac{2,5 \text{ MVA}}{\sqrt{3} \cdot 20 \text{ kV}} = 72,17 \text{ A}$ $I_{skWF} = I_{kWF \max} = 1,3 \cdot I_{rWF} = 1,3 \cdot 72,17 \text{ A} = 93,82 \text{ A}$	$Z_{WF} = \infty$
Cable L1 NA2XS2Y 500 mm ² $R' = 0,0681 \Omega/\text{km}$ $X' = 0,102 \Omega/\text{km}$	Two parallel cables: $\underline{Z}_{L1} = \frac{1}{2} \cdot (0,0681 + j0,102) \Omega/\text{km} \cdot 13,1 \text{ km}$	$\underline{Z}_{L1} = 0,4461 + j0,6681$
Cable L2 to L12 NA2XS2Y 150 mm ² $R' = 0,211 \Omega/\text{km}$ $X' = 0,122 \Omega/\text{km}$	$\underline{Z}_{L2} = (0,211 + j0,122) \Omega/\text{km} \cdot 1,1 \text{ km}$ $\underline{Z}_{L3} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,55 \text{ km}$ $\underline{Z}_{L4} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,79 \text{ km}$ $\underline{Z}_{L5} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,17 \text{ km}$ $\underline{Z}_{L6} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,4 \text{ km}$ $\underline{Z}_{L7} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,55 \text{ km}$ $\underline{Z}_{L8} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,95 \text{ km}$ $\underline{Z}_{L9} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,24 \text{ km}$ $\underline{Z}_{L10} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,29 \text{ km}$ $\underline{Z}_{L11} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,495 \text{ km}$ $\underline{Z}_{L12} = (0,211 + j0,122) \Omega/\text{km} \cdot 0,15 \text{ km}$	$\underline{Z}_{L2} = 0,2321 + j0,1342$ $\underline{Z}_{L3} = 0,1161 + j0,0671$ $\underline{Z}_{L4} = 0,1667 + j0,0963$ $\underline{Z}_{L5} = 0,0359 + j0,0207$ $\underline{Z}_{L6} = 0,0844 + j0,0488$ $\underline{Z}_{L7} = 0,1161 + j0,0671$ $\underline{Z}_{L8} = 0,2004 + j0,1159$ $\underline{Z}_{L9} = 0,0506 + j0,0293$ $\underline{Z}_{L10} = 0,0612 + j0,0354$ $\underline{Z}_{L11} = 0,1044 + j0,0604$ $\underline{Z}_{L12} = 0,0316 + j0,0183$

*Note all cables except ZL1 are neglected on purpose.

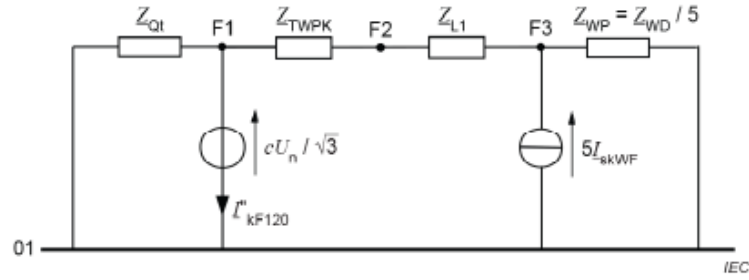


Figure 19 – Equivalent circuit diagram for the calculation of the short-circuit current at the location F1 without the consideration of the internal wind power plant cables (values are related to the 20 kV voltage level), variant 3

The absolute elements of the 3 by 3 nodal impedance matrix in the 20 kV voltage level are:

$$Z = \begin{bmatrix} 0,2171 & 0,1976 & 0,1882 \\ 0,1976 & 1,5318 & 1,4590 \\ 0,1882 & 1,4590 & 2,0806 \end{bmatrix} \Omega$$

The partial short-circuit currents without the influence of the wind power station units WF becomes with $Z_{kFi} = Z_{ii}$ ($i = 1 \dots 3$):

$$I''_{kF1WFO} = \frac{cU_n}{\sqrt{3} \cdot Z_{kF1}} \cdot \frac{U_{nQ}}{U_n} \cdot \frac{1}{t_{rTWP}^2} = \frac{1,1 \cdot 20 \text{ kV}}{\sqrt{3} \cdot 0,2171 \Omega} \cdot \frac{110 \text{ kV}}{20 \text{ kV}} \cdot \left(\frac{20 \text{ kV}}{110 \text{ kV}} \right)^2 = 10,637 \text{ kA}$$

$$I''_{kF2WFO} = \frac{cU_n}{\sqrt{3} \cdot Z_{kF2}} = \frac{1,1 \cdot 20 \text{ kV}}{\sqrt{3} \cdot 1,5318 \Omega} = 8,292 \text{ kA}$$

$$I''_{kF3WFO} = \frac{cU_n}{\sqrt{3} \cdot Z_{kF3}} = \frac{1,1 \cdot 20 \text{ kV}}{\sqrt{3} \cdot 2,0806 \Omega} = 6,105 \text{ kA}$$

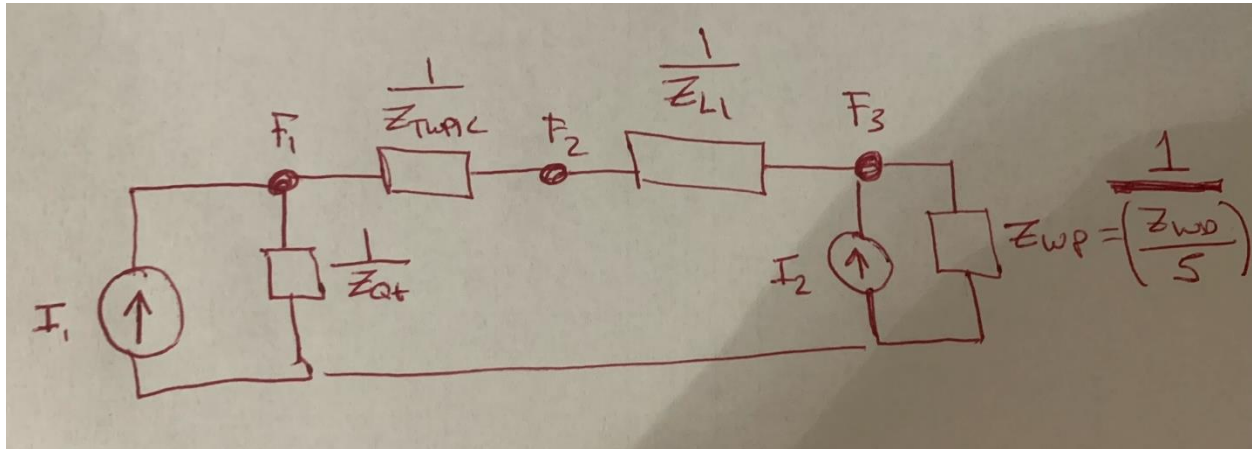
The partial short-circuit currents of the five wind power station units WF for short circuits at F1 to F3 are:

$$I''_{kF1WF} = \frac{Z_{13}}{Z_{11}} \cdot 5 \cdot I_{skWF} \cdot \frac{1}{t_{rTWP}} = \left| \frac{Z_{WP}}{Z_{TWPK} + Z_{L1} + Z_{WP}} \right| \cdot 5 \cdot I_{skWF} \cdot \frac{1}{t_{rTWP}} = 0,4067 \text{ kA} \cdot \frac{1}{5,5} = 0,0739 \text{ kA}$$

$$I''_{kF2WF} = \frac{Z_{23}}{Z_{22}} \cdot 5 \cdot I_{skWF} = \left| \frac{Z_{WP}}{Z_{L1} + Z_{WP}} \right| \cdot 5 \cdot I_{skWF} = 0,4468 \text{ kA}$$

$$I''_{kF3WF} = \frac{Z_{33}}{Z_{33}} \cdot 5 \cdot I_{skWF} = 0,4691 \text{ kA}$$

My Admittance Network:



My Y Matrix:

$$Z_{QtIECOhm} = 0.022 + 0.219i \quad X_{FMRZ_IEC_ohm} = 0.074 + 1.484i \quad \frac{Z_{WD_ohm}}{5} = 1.424 + 14.239i$$

$$Z_{L1_L1B_Cables_Ohm} = 0.446 + 0.668i$$

$$Y_{11} := -1 \cdot \left(\frac{1}{Z_{QtIECOhm}} + \frac{1}{X_{FMRZ_IEC_ohm}} \right) \quad Y_{12} := \left(\frac{1}{X_{FMRZ_IEC_ohm}} \right) \quad Y_{13} := 0$$

$$Y_{21} := \left(\frac{1}{X_{FMRZ_IEC_ohm}} \right) \quad Y_{22} := -1 \cdot \left(\frac{1}{Z_{QtIECOhm}} + \frac{1}{Z_{L1_L1B_Cables_Ohm}} \right) \quad Y_{23} := \left(\frac{1}{Z_{L1_L1B_Cables_Ohm}} \right)$$

$$Y_{31} := 0 \quad Y_{32} := \left(\frac{1}{Z_{L1_L1B_Cables_Ohm}} \right) \quad Y_{33} := -1 \cdot \left(\frac{1}{\frac{Z_{WD_ohm}}{5}} + \frac{1}{Z_{L1_L1B_Cables_Ohm}} \right)$$

$$Y := \begin{pmatrix} Y_{11} & Y_{12} & Y_{13} \\ Y_{21} & Y_{22} & Y_{23} \\ Y_{31} & Y_{32} & Y_{33} \end{pmatrix}$$

$$Z_{mat} := Y^{-1} = \begin{pmatrix} 0.1954 & -0.0293 & 0.0279 \\ -0.0293 & 0.2271 & -0.2163 \\ 0.0279 & -0.2163 & 0.9712 \end{pmatrix}$$