

Beam Data

mp := 10

Beam length (ft) =	length := 77.0	
Composite slab strength (psi) =	fc := 4	
Concrete unit weight (pcf) =	γc := 0.150	
Initial strength of concrete (ksi) =	fci := 5.8	
Final Strength of concrete (ksi) =	fcf := 7.0	
Modulus of beam concrete based on final (ksi) =	$E_c := 33000 \cdot \gamma_c^{1.5} \cdot \sqrt{f_{cf}}$	$E_c = 5072.241$
Modulus of slab concrete (ksi) =	$E_{sl} := 33000 \cdot \gamma_c^{1.5} \cdot \sqrt{f_c}$	$E_{sl} = 3834.254$
Haunch thickness (in) =	ha := 0	
Effective compression slab width (in) =	ETFW := 110	
Slab thickness (in) =	ts := 8.5	Note: 8.25 was used in slab calculations, the value of 8.5 use here is arbitrary.
Live Load distribution factor for moment =	LLDF := 0.852	
Non composite DL (excluding beams)(k/ft) =	DLnc := 1.003	

Span Lengths (ft) =	span := $\begin{pmatrix} 77 \\ 77 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$
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Number of spans =	number := 2	ns := 0.. number·10	$sp_{ns} := 1 + \frac{ns}{10}$
Strength of reinforcing steel (ksi) =	fy := 60		
Factor for slabs =	β1 := 0.85		
Size of bar to try =	size := 9	As of one bar	Asone := 1.0
Bar diameter (in) =	bd := 1.128	clear cover (in) =	cover := 2.5

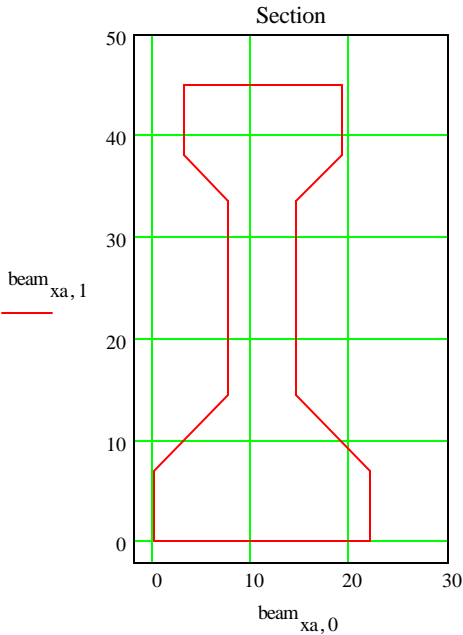
Beam type to use

type := 3

- 1 = AASHTO TYPE I
- 2 = AASHTO TYPE II
- 3 = AASHTO TYPE III
- 4 = AASHTO TYPE IV
- 5 = BT54
- 6 = BT63
- 7 = BT72



Beam area (in^2) =	Area := beam_data_type, 1	Area = 560	
Dist from bottom to cg (in) =	y b := beam_data_type, 2	y b = 20.27	
Section inertia (in^2) =	Inc := beam_data_type, 3	Inc = 125390	Ic := Inc
Beam weight (k/ft) =	bwt := beam_data_type, 4	bwt = 0.583	
Maximum span (ft) =	max_span := beam_data_type, 5	max_span = 80	
Total beam depth (in) =	h := beam_data_type, 6	h = 45	
Width of top flange (in) =	fw t := beam_data_type, 7	fw t = 16	



Composite moment of Inertia

Haunch thickness (in) =

$$ha = 0$$

Effective compression slab width (in) =

$$ETFW = 110$$

Modular ratio =

$$\eta := \frac{\sqrt{f_c}}{\sqrt{f_{cf}}} \quad \eta = 0.756$$

Transformed slab width (in) =

$$b1 := ETFW \cdot \eta \quad b1 = 83.152$$

Slab thickness (in) =

$$ts = 8.5$$

Composite distance from bottom to c.g. (in) =

$$ybc := \frac{b1 \cdot ts \cdot \left(h + ha + \frac{ts}{2} \right) + Area \cdot yb}{b1 \cdot ts + Area} \quad ybc = 36.439$$

Composite N.A. to top beam (in) =

$$ytb = h - ybc \quad ytb = 8.561$$

Composite N.A. to top slab (in) =

$$yts = h + ts - ybc \quad yts = 17.061$$

Composite moment of inertia (in⁴) =

$$Ic := Inc + \frac{b1 \cdot ts^3}{12} + Area \cdot (yb - ybc)^2 + b1 \cdot ts \cdot \left(yts - \frac{ts}{2} \right)^2$$

$$Ic = 392050.137$$

Composite Section Modulus

Section modulus bottom of beam (in³) =

$$Sbc := \frac{Ic}{ybc} \quad Sbc = 10759.059$$

Section modulus top beam (in³) =

$$Stb := \frac{Ic}{ytb} \quad Stb = 45795.29$$

Section modulus top concrete (in³) =

$$Stc := \frac{Ic}{yts} \cdot \frac{1}{\eta} \quad Stc = 30398.91$$

Non-Composite Section Modulus

Section modulus bottom of beam (in³) =

$$Sb := \frac{Inc}{yb} \quad Sb = 6185.989$$

Section modulus top beam (in³) =

$$St := \frac{Inc}{h - yb} \quad St = 5070.36$$

Non compostie Moments

Total load including beam weight (k/ft) = $DL := bwt + DLnc$ $DL = 1.586$

Define range (ft) =
$$x1_{ns} := \left\{ \begin{array}{l} j_{ns} \leftarrow \text{ceil}\left(\frac{ns + 0.001}{10} - 1\right) \\ j1_{ns} \leftarrow (sp_{ns} - j_{ns} - 1) \cdot \text{span}(j_{ns}) \end{array} \right.$$

Indicate which span =
$$a1_{ns} := \left\{ \begin{array}{l} j_{ns} \leftarrow \text{ceil}\left(\frac{ns + 0.001}{10} - 1\right) \\ j1_{ns} \leftarrow \text{span}(j_{ns}) \end{array} \right.$$

Calculate moment at tenth points from beam =
$$Mb_{ns} := \frac{bwt \cdot x1_{ns}}{2} \cdot (a1_{ns} - x1_{ns})$$

Calculate moment at tenth points from other =
$$Mo_{ns} := \frac{DLnc \cdot x1_{ns}}{2} \cdot (a1_{ns} - x1_{ns})$$

$$\begin{pmatrix} \text{fullq} \\ \text{fp1} \\ \text{fn1} \end{pmatrix} :=$$
[illegible]

(Mb Mo)

Live load distribution factor has been applied to the Live Loads shown here.

fullq

Service III loads (moment)

SIII1

SIII2

SIII3

SIII4

SIII5

SIII6

SIII7

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	SIII1	SIII2	SIII3	SIII4	SIII5	SIII5	SIII7	
	DC LOADS (non-comp)		DW Loads	LL + I		TOTAL LOADS		
LOCATION	self wt	other (slab)	(comp)	M (+)	M (-)	M (+)	M (-)	
1.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
1.1	155.55	267.61	111.00	553.60	-72.80	1087.75	461.35	
1.2	276.53	475.74	188.00	935.20	-144.80	1875.47	795.47	
1.3	362.94	624.41	231.00	1154.40	-216.80	2372.76	1001.56	
1.4	414.79	713.61	239.00	1252.00	-289.60	2619.41	1077.81	
1.5	432.08	743.35	213.00	1227.20	-362.40	2615.62	1026.02	
1.6	414.79	713.61	154.00	1100.00	-363.20	2382.41	919.21	
1.7	362.94	624.41	60.00	849.60	-508.00	1896.96	539.36	
1.8	276.53	475.74	-69.00	502.40	-580.00	1185.67	103.27	
1.9	155.55	267.61	-230.00	189.60	-801.60	382.75	-608.45	
2.0	0.00	0.00	-427.00	0.00	-1281.60	-427.00	-1708.60	
2.1	155.55	267.61	-231.00	189.60	-801.60	381.75	-609.45	
2.2	276.53	475.74	-69.00	502.40	-580.00	1185.67	103.27	
2.3	362.94	624.41	60.00	849.60	-508.00	1896.96	539.36	
2.4	414.79	713.61	154.00	1100.00	-363.20	2382.41	919.21	
2.5	432.08	743.35	213.00	1227.20	-362.40	2615.62	1026.02	
2.6	414.79	713.61	239.00	1252.00	-289.60	2619.41	1077.81	
2.7	362.94	624.41	231.00	1154.40	-216.80	2372.76	1001.56	
2.8	276.53	475.74	188.00	935.20	-144.80	1875.47	795.47	
2.9	155.55	267.61	111.00	553.60	-72.80	1087.75	461.35	
3.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	

full

Strength I loads (moment)

Maximum 1.25*DW + 1.5*DW + 1.75*(LL + IM)
Minimum 0.9*DC + 0.65*DW + 1.75*(LL + IM)

The loads shown in the DL columns reflect the values from Service I. The appropriate load combination (max or min) is shown in the total loads columns. The minimum load factors for dead load are used when dead load and future wearing surface stresses are of opposite sign to that of the live load.

STI1

STI2

STI3

STI4

STI5

STI6

STI7

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	STI1	STI2	STI3	STI4	STI5	STI6	STI7	
	DC LOADS (non-comp)		DW Loads	LL + I		TOTAL LOADS		
LOCATION	self wt	other (slab)	(comp)	M (+)	M (-)	M (+)	M (-)	
1.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
1.1	155.55	267.61	111.00	692.00	-91.00	1906.44	293.74	
1.2	276.53	475.74	188.00	1169.00	-181.00	3268.09	482.49	
1.3	362.94	624.41	231.00	1443.00	-271.00	4105.95	564.52	
1.4	414.79	713.61	239.00	1565.00	-362.00	4507.76	537.42	
1.5	432.08	743.35	213.00	1534.00	-453.00	4473.28	403.58	
1.6	414.79	713.61	154.00	1375.00	-454.00	4047.76	321.17	
1.7	362.94	624.41	60.00	1062.00	-635.00	3182.70	-183.63	
1.8	276.53	475.74	-69.00	628.00	-725.00	1994.49	-695.21	
1.9	155.55	267.61	-230.00	237.00	-1002.00	794.19	-1717.66	
2.0	0.00	0.00	-427.00	0.00	-1602.00	0.00	-3444.00	
2.1	155.55	267.61	-231.00	237.00	-1002.00	793.54	-1719.16	
2.2	276.53	475.74	-69.00	628.00	-725.00	1994.49	-695.21	
2.3	362.94	624.41	60.00	1062.00	-635.00	3182.70	-183.63	
2.4	414.79	713.61	154.00	1375.00	-454.00	4047.76	321.17	
2.5	432.08	743.35	213.00	1534.00	-453.00	4473.28	403.58	
2.6	414.79	713.61	239.00	1565.00	-362.00	4507.76	537.42	
2.7	362.94	624.41	231.00	1443.00	-271.00	4105.95	564.52	
2.8	276.53	475.74	188.00	1169.00	-181.00	3268.09	482.49	
2.9	155.55	267.61	111.00	692.00	-91.00	1906.44	293.74	
3.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	

LRFD 5.7.3.3.2 minimum reinforcement

Unless otherwise specified, at any section of a flexural component, the amount of prestressed and nonprestressed tensile reinforcement shall be adequate to develop a factored flexural resistance, M_r , at least equal to the lesser of

1.2* the cracking strength

1.33 times the factored moment required by Strength I

What I shall do is calculate required steel based on the cracking moment. Then I shall calculate the required steel based on strength. If any of the required are less than 1.2*Mcr I shall increase the required by 4/3.

$$\text{LRFD 5.4.2.6 the modulus of rupture (ksi)} = \quad f_r := 0.24 \cdot \sqrt{f_c} \quad f_r = 0.48$$

$$\text{Cracking moment (k*ft)} = \quad M_{cr} := \frac{f_r \cdot S_{tc}}{12} \quad M_{cr} = 1215.956$$

$$\text{Effective section depth (in)} = \quad d := h + \frac{t_s}{2} \quad d = 49.25 \quad \text{assume steel in center of slab}$$

$$A_{cr} := 0 \quad A_s := 0 \quad A_r := 0 \quad A_{rt} := 0$$

$$\text{Required steel based on } 1.2 \cdot M_{cr} \text{ (in}^2\text{)} = \quad A_{cr} := \text{root} \left[\left| 12 \cdot M_{cr} \right| - 0.9 \cdot A_{cr} \cdot f_y \cdot \left(d - \frac{A_{cr} \cdot f_y}{1.7 \cdot f_c \cdot b} \right), A_{cr} \right]$$

$$A_{cr} = 5.756$$

CALCULATIONS BASED ON RECTANGULAR SECTION

$$\text{Required steel (pure strength)(in}^2\text{)} = \quad A_{r_{ns}} := \begin{cases} j_{ns} \leftarrow \text{root} \left[\left| 12 \cdot STI7_{ns} \right| - 0.9 \cdot A_r \cdot f_y \cdot \left(d - \frac{A_r \cdot f_y}{1.7 \cdot f_c \cdot b} \right), A_r \right] & \\ 0 \text{ if } (STI7_{ns} \geq 0) & \\ j_{ns} \text{ otherwise} & \end{cases} \quad A_{r_{mp}} = 18.253$$

$$\text{Required Steed (in}^2\text{)} = \quad A_{s1_{ns}} := \begin{cases} 0 \text{ if } STI7_{ns} \geq 0 & \\ \text{otherwise} & \\ \frac{4}{3} \cdot A_{r_{ns}} \text{ if } A_{r_{ns}} < A_{cr} & \\ A_{r_{ns}} \text{ otherwise} & \end{cases} \quad A_{s1_{mp}} = 18.253$$

$$\text{Distance between the N.A. and the compression flange (in)} = \quad c1_{ns} := \frac{A_{s1_{ns}} \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b} \quad c1_{mp} = 17.225$$

CALCULATIONS BASED ON "T" SECTION

$$hf := tbf$$

Required steel for "T" section

$$Art_{ns} := \text{root} \left[\left| 12 \cdot STI7_{ns} \right| - 0.9 \cdot Art \cdot fy \cdot \left[d - \frac{Art \cdot fy - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} \right] - 0.85 \cdot fc \cdot (b - bw) \cdot \beta 1 \cdot hf \cdot \left[\frac{Art \cdot fy - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} - \frac{hf}{2} \right], Art \right]$$

Apply the requirements of 1.2*Mcr to "T" section behavior

Required Steed (in^2) =

$$As2_{ns} := \begin{cases} 0 & \text{if } STI7_{ns} \geq 0 \\ \text{otherwise} \\ \begin{cases} \frac{4}{3} \cdot Art_{ns} & \text{if } Art_{ns} < Acr \\ Art_{ns} & \text{otherwise} \end{cases} \end{cases} \quad As2_{mp} = 16.955$$

Check rectangular section behavior

Thickness of bottom flange (compression flange) (in) =

$$tbf = 7$$

Check

$$ck1_{ns} := \begin{cases} "R" & \text{if } tbf > c1_{ns} \\ "T" & \text{otherwise} \end{cases}$$

Actual steel to use (in^2) =

$$As_{ns} := \begin{cases} As1_{ns} & \text{if } ck1_{ns} = "R" \\ As2_{ns} & \text{otherwise} \end{cases}$$

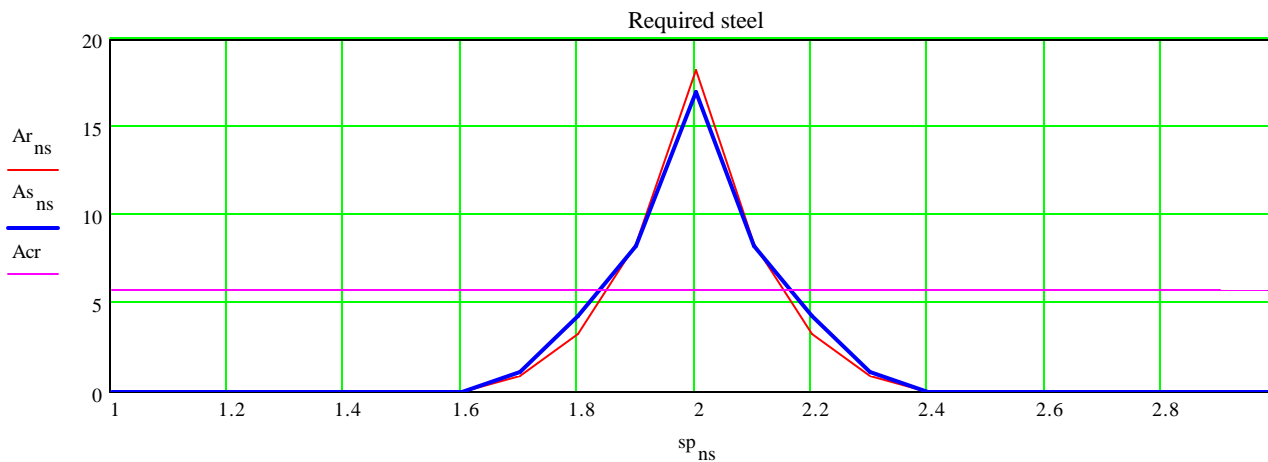
$$disp_{ns,0} := sp_{ns} \quad disp_{ns,1} := x1_{ns} \quad disp_{ns,2} := STI7_{ns} \quad disp_{ns,3} := Ar_{ns} \quad disp_{ns,4} := As1_{ns}$$

$$disp_{ns,5} := c1_{ns} \quad disp_{ns,6} := ck1_{ns} \quad disp_{ns,7} := Art_{ns} \quad disp_{ns,8} := As2_{ns} \quad disp_{ns,9} := As_{ns}$$

column 0 = span point
 column 1 = range
 column 2 = Strength I Negative moment
 column 3 = required steel for negative moment based on rectangular section
 column 4 = Required steel using $1.2 \cdot M_{cr}$
 column 5 = "c" value based on rectangular section
 column 6 = check rectangular section "R" denotes rectangular "T" denotes "T" section
 column 7 = required steel based on "T" section non considering $1.2 \cdot M_{cr}$
 column 8 = required steel based on "T" section and using $1.2 \cdot M_{cr}$
 column 9 = actual steel to use

	0	1	2	3	4	5	6	7	8	9
0	1	0	0	0	0	0	"R"	0.617	0	0
1	1.1	7.7	293.737	0	0	0	"R"	1.851	0	0
2	1.2	15.4	482.494	0	0	0	"R"	2.656	0	0
3	1.3	23.1	564.521	0	0	0	"R"	3.009	0	0
4	1.4	30.8	537.417	0	0	0	"R"	2.892	0	0
5	1.5	38.5	403.582	0	0	0	"R"	2.318	0	0
6	1.6	46.2	321.167	0	0	0	"R"	1.967	0	0
7	1.7	53.9	-183.629	0.834	1.112	1.05	"R"	1.385	1.847	1.112
8	1.8	61.6	-695.206	3.221	4.295	4.053	"R"	3.576	4.768	4.295
9	1.9	69.3	-1717.663	8.313	8.313	7.845	"T"	8.197	8.197	8.197
10	2	0	-3444	18.253	18.253	17.225	"T"	16.955	16.955	16.955
11	2.1	7.7	-1719.163	8.321	8.321	7.852	"T"	8.204	8.204	8.204
12	2.2	15.4	-695.206	3.221	4.295	4.053	"R"	3.576	4.768	4.295
13	2.3	23.1	-183.629	0.834	1.112	1.05	"R"	1.385	1.847	1.112
14	2.4	30.8	321.167	0	0	0	"R"	1.967	0	0
15	2.5	38.5	403.582	0	0	0	"R"	2.318	0	0
16	2.6	46.2	537.417	0	0	0	"R"	2.892	0	0
17	2.7	53.9	564.521	0	0	0	"R"	3.009	0	0
18	2.8	61.6	482.494	0	0	0	"R"	2.656	0	0
19	2.9	69.3	293.737	0	0	0	"R"	1.851	0	0
20	3	0	0	0	0	0	"R"	0.617	0	0

disp =



LRFD 5.7.3.4 CONTROL OF CRACKING BY DISTRIBUTION OF REINFORCEMENT

The provisions specified herein shall apply to the reinforcement of all concrete components, except that of deck slabs designed in accordance with Article 9.7.2, in which tension in the cross-section exceeds 80 percent of the modulus of rupture, specified in article 5.4.2.6, at applicable service limit state load combination specified in Table 3.4.1-1.

Since this is the main negative moment reinforcement parallel to traffic I shall apply the provisions of this article.

Components shall be so proportioned that the tensile stress in the mild steel reinforcement at the service limit state, f_{sa} does not exceed:

$$f_{sa} = \frac{Z}{(dc \cdot A)^{\frac{1}{3}}} \leq 0.6 \cdot f_y \quad 5.7.3.4-1$$

dc = depth of concrete measured from extreme tension fiber to center of bar or wire located closest thereto; for calculation purposes, the thickness of clear coner used to compute dc shall not be taken to be greater than 2 in.

A = area fo concrete having the same centroid as the principal tensile reinforcement and bounded by the surfaces of hte cross-section and a straight line parallel to the neutral axis, divided by the number of bars or wires; for calculation purposes the thickness of clear concrete cover used to compute A shall not be taken to be greater than 2.0 in.

Z = crack width parameter - use 170 k/in for moderate exposure.

Max Required number of bars using input bar size =
(formula will chose an even number of bars)

$$n_{max} := \begin{cases} j \leftarrow \text{ceil} \left(\frac{\max(A_s \langle \phi \rangle)}{A_{sone}} \right) & n_{max} = 18 \\ j \text{ if } \text{ceil} \left(\frac{j}{2} \right) = \frac{j}{2} \\ j + 1 & \text{otherwise} \end{cases}$$

Maximim steel (in^2) =

$$A_{smax} := n_{max} \cdot A_{sone} \quad A_{smax} = 18$$

Minimum number of bars (after cutoff) =

$$n_{min} := \frac{n_{max}}{2} \quad n_{min} = 9$$

Minimum steel (in^2) =

$$A_{smin} := n_{min} \cdot A_{sone} \quad A_{smin} = 9$$

SL moment to be used (use 0 if the moment is positive) $M1_{ns} := \begin{cases} |SI7_{ns}| & \text{if } SI7_{ns} < 0 \\ 0 & \text{otherwise} \end{cases}$ $M1_{mp} = 2029$

$$F := 0$$

Stress in steel for rectangular section

SL Stress in max steel (psi) = $fsmax1_{ns} := \text{root} \left[12 \cdot M1_{ns} - Asmax \cdot F \cdot \left(d - \frac{Asmax \cdot F}{1.7 \cdot fc \cdot b} \right), F \right]$ $fsmax1_{mp} = 29.607$

SL Stress in min steel (psi) = $fsmin1_{ns} := \text{root} \left[12 \cdot M1_{ns} - Asmin \cdot F \cdot \left(d - \frac{Asmin \cdot F}{1.7 \cdot fc \cdot b} \right), F \right]$ $fsmin1_{mp} = 59.214$

Stress in steel for "T" section

$$fsmax2_{ns} := \text{root} \left[\left| 12 \cdot M1_{ns} \right| - 0.9 \cdot Asmax \cdot F \cdot \left[d - \frac{Asmax \cdot F - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} \right] - 0.85 \cdot fc \cdot (b - bw) \cdot \beta 1 \cdot hf \cdot \left[\frac{Asmax \cdot F - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} - \frac{hf}{2} \right], F \right]$$

$$fsmax2_{mp} = 32.259$$

$$fsmin2_{ns} := \text{root} \left[\left| 12 \cdot M1_{ns} \right| - 0.9 \cdot Asmin \cdot F \cdot \left[d - \frac{Asmin \cdot F - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} \right] - 0.85 \cdot fc \cdot (b - bw) \cdot \beta 1 \cdot hf \cdot \left[\frac{Asmin \cdot F - \beta 1 \cdot fc \cdot (b - bw) \cdot hf}{1.7 \cdot fc \cdot b} - \frac{hf}{2} \right], F \right]$$

$$fsmin2_{mp} = 64.518$$

Chose values of stress to use (rectangular or "T" stress)

Max stress (ksi) = $fsmax_{ns} := \begin{cases} 0 & \text{if } M1_{ns} = 0 \\ \text{otherwise} \\ \begin{cases} fsmax1_{ns} & \text{if } ck1_{ns} = "R" \\ fsmax2_{ns} & \text{otherwise} \end{cases} \end{cases}$ $fsmax_{mp} = 32.259$

Minimum stress (ksi) = $fsmin_{ns} := \begin{cases} 0 & \text{if } M1_{ns} = 0 \\ \text{otherwise} \\ \begin{cases} fsmin2_{ns} & \text{if } ck1_{ns} = "R" \\ fsmin2_{ns} & \text{otherwise} \end{cases} \end{cases}$ $fsmin_{mp} = 64.518$

Allowable Stress

Cracking factor = $z := 170$

Total Section Height (in) = $\text{height} := h + t_s$ $\text{height} = 53.5$

Distance from extreme tension fiber to CL. reinforcing $dc := \min\left(\left(\frac{\text{cover}}{2}\right)\right) + 0.75 + \frac{bd}{2}$ $dc = 3.314$

Effective tension flange area $A_{max} := \frac{2 \cdot dc \cdot \text{ETFW}}{n_{max}}$ $A_{max} = 40.504$

$A_{min} := \frac{2 \cdot dc \cdot \text{ETFW}}{n_{min}}$ $A_{min} = 81.009$

Allowable Stress

$fs_{max_{ns}} := \min\left[\left[\frac{z}{(dc \cdot A_{max})^{\frac{1}{3}}}\right], 0.6 \cdot f_y\right]$ $fs_{max_{mp}} = 33.202$

$fs_{min_{ns}} := \min\left[\left[\frac{z}{(dc \cdot A_{min})^{\frac{1}{3}}}\right], 0.6 \cdot f_y\right]$ $fs_{min_{mp}} = 26.352$

Check max steel for cracking moment

$ck_{max_{ns}} := \begin{cases} \text{"fail max"} & \text{if } fs_{max_{ns}} < fs_{max_{ns}} \\ \text{"pass"} & \text{otherwise} \end{cases}$ $ck_{max_{mp}} = \text{"pass"}$

Check min steel for cracking moment

$ck_{min_{ns}} := \begin{cases} \text{"fail min"} & \text{if } fs_{min_{ns}} < fs_{min_{ns}} \\ \text{"pass"} & \text{otherwise} \end{cases}$ $ck_{min_{mp}} = \text{"pass"}$

Prepare output display $\text{disp} := 0$

$\text{disp}_{ns,0} := sp_{ns}$ $\text{disp}_{ns,1} := fs_{max_{ns}}$ $\text{disp}_{ns,4} := fs_{min_{ns}}$

$\text{disp}_{ns,2} := fs_{max_{ns}}$ $\text{disp}_{ns,5} := fs_{min_{ns}}$

$\text{disp}_{ns,3} := ck_{max_{ns}}$ $\text{disp}_{ns,6} := ck_{min_{ns}}$

disp =

	0	1	2	3	4	5	6
0	1	0	33.202	"pass"	0	26.352	"pass"
1	1.1	0	33.202	"pass"	0	26.352	"pass"
2	1.2	0	33.202	"pass"	0	26.352	"pass"
3	1.3	0	33.202	"pass"	0	26.352	"pass"
4	1.4	0	33.202	"pass"	0	26.352	"pass"
5	1.5	0	33.202	"pass"	0	26.352	"pass"
6	1.6	0	33.202	"pass"	0	26.352	"pass"
7	1.7	0	33.202	"pass"	0	26.352	"pass"
8	1.8	0.566	33.202	"pass"	5.27	26.352	"pass"
9	1.9	13.575	33.202	"pass"	27.151	26.352	"fail min"
10	2	32.259	33.202	"pass"	64.518	26.352	"fail min"
11	2.1	13.59	33.202	"pass"	27.18	26.352	"fail min"
12	2.2	0.566	33.202	"pass"	5.27	26.352	"pass"
13	2.3	0	33.202	"pass"	0	26.352	"pass"
14	2.4	0	33.202	"pass"	0	26.352	"pass"
15	2.5	0	33.202	"pass"	0	26.352	"pass"
16	2.6	0	33.202	"pass"	0	26.352	"pass"
17	2.7	0	33.202	"pass"	0	26.352	"pass"
18	2.8	0	33.202	"pass"	0	26.352	"pass"
19	2.9	0	33.202	"pass"	0	26.352	"pass"
20	3	0	33.202	"pass"	0	26.352	"pass"
21							

column 0 = span point
column 1 = stress on max
column 2 = allowable on max
column 3 = pass/fail for max
column 4 = stress on min
column 5 = allowable on min
column 6 = pass/fail for min

column 0 = span point
column 1 = stress on max
column 2 = allowable on max
column 3 = pass/fail for max
column 4 = stress on min
column 5 = allowable on min
column 6 = pass/fail for min

LRFD 5.5.3.2 Fatigue

The stress range in straight reinforcement resulting from the fatigue load combination, specified in Table 3.4.1-1 shall not exceed:

$$f_f = 21 - 0.33 \cdot f_{min} + 8 \cdot \frac{r}{h}$$

f_f = stress range (ksi)

f_{min} = the minimum live load stress resulting from the fatigue load combination specified in Table 3.4.1-1

r/h = ratio of base radius to height of rolled-on transverse deformations; if the actual value is not known, 0.3 may be used

Apply LLDF to the fatigue truck =

$$f_{p_{ns}} := f_{p1_{ns}} \cdot LLDF$$

$$f_{p_{mp}} = 0$$

$$f_{n_{ns}} := f_{n1_{ns}} \cdot LLDF$$

$$f_{n_{mp}} = -422.592$$

Using maximum steel

Determine if section is rectangular or "T" section for max and min amounts of steel used. The previous determination was done based on the required steel of a rectangular section. This calculation will be based on the actual steel used (max and min).

"c" value for "T" section	$c_t := \frac{A_{smax} \cdot f_y - 0.85 \cdot \beta_1 \cdot f_c \cdot (b - b_w) \cdot h_f}{0.85 \cdot f_c \cdot \beta_1 \cdot b_w}$	$c_t = 38.386$
---------------------------	---	----------------

"c" value for rectangular	$c_r := \frac{A_{smax} \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b}$	$c_r = 16.986$
---------------------------	--	----------------

determine rectangular or "T"	$ck2 := \begin{cases} \text{"R"} & \text{if } c_r \leq t_{bf} \\ \text{"T"} & \text{otherwise} \end{cases}$	$ck2 = \text{"T"}$
------------------------------	---	--------------------

jd for rectangular section	$j_{dmax} := d - \frac{A_{smax} \cdot f_y}{0.85 \cdot f_c \cdot b}$	$j_{dmax} = 34.811$
----------------------------	---	---------------------

jd for "T" section	$j_{dtmax} := d - \frac{\beta_1 \cdot c_t}{2}$	$j_{dtmax} = 32.936$
--------------------	--	----------------------

Pick value of jd for rectangular or "T" section	$j_{dmax} := \begin{cases} j_{dmax} & \text{if } ck2 = \text{"R"} \\ j_{dtmax} & \text{otherwise} \end{cases}$	$j_{dmax} = 32.936$
---	--	---------------------

Stress in steel for fatigue limit state

$$f_{\max p_{ns}} := \begin{cases} \frac{-f_{p_{ns}} \cdot 12}{A_{\max} \cdot j_{d\max}} & \text{if } f_{p_{ns}} < 0 \\ \frac{-f_{p_{ns}} \cdot [y_{ts} - (\text{height} - d)] \cdot 2 \cdot \eta \cdot 12}{I_c} & \text{otherwise} \end{cases} \quad f_{\max p_{mp}} = 0$$

$$f_{\max n_{ns}} := \begin{cases} \frac{-f_{n_{ns}} \cdot 12}{A_{\max} \cdot j_{d\max}} & \text{if } f_{n_{ns}} < 0 \\ \frac{-f_{n_{ns}} \cdot [y_{ts} - (\text{height} - d)] \cdot 2 \cdot \eta \cdot 12}{I_c} & \text{otherwise} \end{cases} \quad f_{\max n_{mp}} = 8.554$$

Stress range for max steel

$$ff_{\max ns} := |f_{\max p_{ns}} - f_{\max n_{ns}}| \quad ff_{\max mp} = 8.554$$

Min stress for Max steel

$$f_{m1_{ns}} := \min \left(\begin{pmatrix} f_{\max p_{ns}} \\ f_{\max n_{ns}} \end{pmatrix} \right) \quad f_{m1_{mp}} = 0$$

Allowable stress range

$$f_{\max ns} := 21 - 0.33 \cdot f_{m1_{ns}} + 8 \cdot 0.3 \quad f_{\max mp} = 23.4$$

Check stress range

$$f_{\max ns} := \begin{cases} \text{"fail"} & \text{if } ff_{\max ns} > f_{\max ns} \\ \text{"pass"} & \text{otherwise} \end{cases} \quad f_{\max mp} = \text{"pass"}$$

$$\text{disp} := 0$$

$$\text{disp}_{ns,0} := sp_{ns} \quad \text{disp}_{ns,1} := ck2 \quad \text{disp}_{ns,2} := jd_{\max} \quad \text{disp}_{ns,3} := f_{\max p_{ns}} \quad \text{disp}_{ns,4} := f_{\max n_{ns}}$$

$$\text{disp}_{ns,5} := ff_{\max ns} \quad \text{disp}_{ns,6} := f_{\max ns} \quad \text{disp}_{ns,7} := f_{\max ns}$$

disp =

	0	1	2	3	4	5	6	7
0	1	"T"	32.936	0	0	0	23.4	"pass"
1	1.1	"T"	32.936	-0.198	0.862	1.06	23.465	"pass"
2	1.2	"T"	32.936	-0.324	1.725	2.048	23.507	"pass"
3	1.3	"T"	32.936	-0.401	2.57	2.971	23.532	"pass"
4	1.4	"T"	32.936	-0.422	3.432	3.854	23.539	"pass"
5	1.5	"T"	32.936	-0.401	4.277	4.677	23.532	"pass"
6	1.6	"T"	32.936	-0.377	5.139	5.516	23.525	"pass"
7	1.7	"T"	32.936	-0.299	5.984	6.283	23.499	"pass"
8	1.8	"T"	32.936	-0.174	6.847	7.02	23.457	"pass"
9	1.9	"T"	32.936	-0.075	7.709	7.784	23.425	"pass"
10	2	"T"	32.936	0	8.554	8.554	23.4	"pass"
11	2.1	"T"	32.936	-0.075	7.709	7.784	23.425	"pass"
12	2.2	"T"	32.936	-0.174	6.847	7.02	23.457	"pass"
13	2.3	"T"	32.936	-0.299	5.984	6.283	23.499	"pass"
14	2.4	"T"	32.936	-0.377	5.139	5.516	23.525	"pass"
15	2.5	"T"	32.936	-0.401	4.277	4.677	23.532	"pass"
16	2.6	"T"	32.936	-0.422	3.432	3.854	23.539	"pass"
17	2.7	"T"	32.936	-0.401	2.57	2.971	23.532	"pass"
18	2.8	"T"	32.936	-0.324	1.725	2.048	23.507	"pass"
19	2.9	"T"	32.936	-0.198	0.862	1.06	23.465	"pass"
20	3	"T"	32.936	0	0	0	23.4	"pass"
21								

0 = span point
 1 = section type
 2 = "jd" value
 3 = stress for positive moment
 4 = stress for negative moment
 5 = stress range
 6 = allowable stress range
 7 = pass/fail

Using minimum steel

Determine if section is rectangular or "T" section for max and min amounts of steel used. The previous determination was done based on the required steel of a rectangular section. This calculation will be based on the actual steel used (max and min).

"c" value for "T" section	$c_t := \frac{A_{smin} \cdot f_y - 0.85 \cdot \beta_1 \cdot f_c \cdot (b - b_w) \cdot h_f}{0.85 \cdot f_c \cdot \beta_1 \cdot b_w}$	$c_t = 11.693$
---------------------------	---	----------------

"c" value for rectangular	$c_r := \frac{A_{smin} \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b}$	$c_r = 8.493$
---------------------------	--	---------------

determine rectangular or "T"	$ck2 := \begin{cases} \text{"R"} & \text{if } c_r \leq tbf \\ \text{"T"} & \text{otherwise} \end{cases}$	$ck2 = \text{"T"}$
------------------------------	--	--------------------

jd for rectangular section	$j_{drmin} := d - \frac{A_{smax} \cdot f_y}{0.85 \cdot f_c \cdot b}$	$j_{drmin} = 34.811$
----------------------------	--	----------------------

jd for "T" section	$j_{dtmin} := d - \frac{\beta_1 \cdot c_t}{2}$	$j_{dtmin} = 44.28$
--------------------	--	---------------------

Pick value of jd for rectangular or "T" section	$j_{dmin} := \begin{cases} j_{drmin} & \text{if } ck2 = \text{"R"} \\ j_{dtmin} & \text{otherwise} \end{cases}$	$j_{dmin} = 44.28$
---	---	--------------------

Stress in steel for fatigue limit state

$$f_{minp_{ns}} := \begin{cases} \frac{-f_{p_{ns}} \cdot 12}{A_{min} \cdot j_{dmin}} & \text{if } f_{p_{ns}} < 0 \\ \frac{-f_{p_{ns}} \cdot [y_{ts} - (\text{height} - d)] \cdot 2 \cdot \eta \cdot 12}{I_c} & \text{otherwise} \end{cases} \quad f_{minp_{mp}} = 0$$

$$f_{minn_{ns}} := \begin{cases} \frac{-f_{n_{ns}} \cdot 12}{A_{min} \cdot j_{dmin}} & \text{if } f_{n_{ns}} < 0 \\ \frac{-f_{n_{ns}} \cdot [y_{ts} - (\text{height} - d)] \cdot 2 \cdot \eta \cdot 12}{I_c} & \text{otherwise} \end{cases} \quad f_{minn_{mp}} = 12.725$$

Stress range for min steel

$$ff_{min_{ns}} := |f_{minp_{ns}} - f_{minn_{ns}}| \quad ff_{min_{mp}} = 12.725$$

Min stress for Min steel

$$f_{m2_{ns}} := \min \left(\begin{pmatrix} f_{minp_{ns}} \\ f_{minn_{ns}} \end{pmatrix} \right) \quad f_{m2_{mp}} = 0$$

Allowable stress range

$$f_{min_{ns}} := 21 - 0.33 \cdot f_{m1_{ns}} + 8 \cdot 0.3 \quad f_{min_{mp}} = 23.4$$

Check stress range

$$f_{rmin_{ns}} := \begin{cases} \text{"fail"} & \text{if } ff_{min_{ns}} > f_{min_{ns}} \\ \text{"pass"} & \text{otherwise} \end{cases} \quad f_{rmin_{mp}} = \text{"pass"}$$

$$disp := 0$$

$$disp_{ns,0} := sp_{ns} \quad disp_{ns,1} := ck2 \quad disp_{ns,2} := jdmin \quad disp_{ns,3} := f_{minp_{ns}} \quad disp_{ns,4} := f_{minn_{ns}}$$

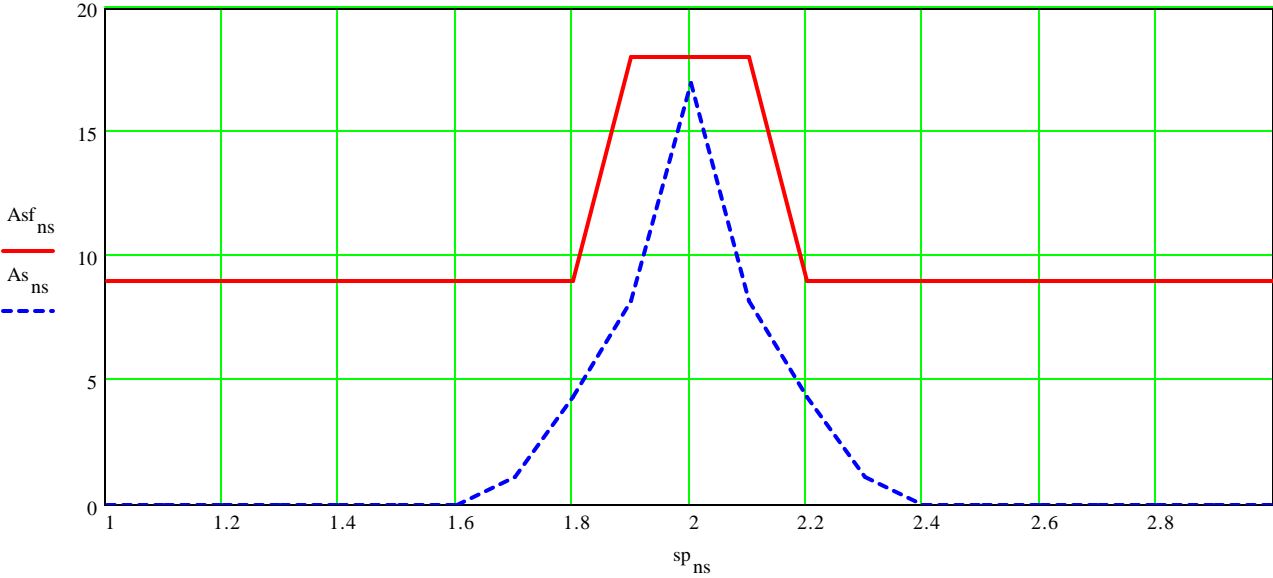
$$disp_{ns,5} := ff_{min_{ns}} \quad disp_{ns,6} := f_{min_{ns}} \quad disp_{ns,7} := f_{rmin_{ns}}$$

	0	1	2	3	4	5	6	7
0	1	"T"	44.28	0	0	0	23.4	"pass"
1	1.1	"T"	44.28	-0.198	1.283	1.481	23.465	"pass"
2	1.2	"T"	44.28	-0.324	2.565	2.889	23.507	"pass"
3	1.3	"T"	44.28	-0.401	3.823	4.224	23.532	"pass"
4	1.4	"T"	44.28	-0.422	5.105	5.528	23.539	"pass"
5	1.5	"T"	44.28	-0.401	6.362	6.763	23.532	"pass"
6	1.6	"T"	44.28	-0.377	7.645	8.022	23.525	"pass"
7	1.7	"T"	44.28	-0.299	8.902	9.201	23.499	"pass"
8	1.8	"T"	44.28	-0.174	10.185	10.359	23.457	"pass"
9	1.9	"T"	44.28	-0.075	11.468	11.543	23.425	"pass"
disp = 10	2	"T"	44.28	0	12.725	12.725	23.4	"pass"
11	2.1	"T"	44.28	-0.075	11.468	11.543	23.425	"pass"
12	2.2	"T"	44.28	-0.174	10.185	10.359	23.457	"pass"
13	2.3	"T"	44.28	-0.299	8.902	9.201	23.499	"pass"
14	2.4	"T"	44.28	-0.377	7.645	8.022	23.525	"pass"
15	2.5	"T"	44.28	-0.401	6.362	6.763	23.532	"pass"
16	2.6	"T"	44.28	-0.422	5.105	5.528	23.539	"pass"
17	2.7	"T"	44.28	-0.401	3.823	4.224	23.532	"pass"
18	2.8	"T"	44.28	-0.324	2.565	2.889	23.507	"pass"
19	2.9	"T"	44.28	-0.198	1.283	1.481	23.465	"pass"
20	3	"T"	44.28	0	0	0	23.4	"pass"
21								

0 = span point
 1 = section type
 2 = "jd" value
 3 = stress for positive moment
 4 = stress for negative moment
 5 = stress range
 6 = allowable stress range
 7 = pass/fail

Final steel selection

$$Asf_{ns} := \left\{ \begin{array}{l} As_{min} \text{ if } (As_{min} > As_{ns}) \cdot (ckmin_{ns} = \text{"pass"}) \cdot (fmin_{ns} = \text{"pass"}) \\ \text{otherwise} \\ As_{max} \text{ if } (As_{max} > As_{ns}) \cdot (ckmax_{ns} = \text{"pass"}) \cdot (fmax_{ns} = \text{"pass"}) \\ \text{"fail" otherwise} \end{array} \right.$$

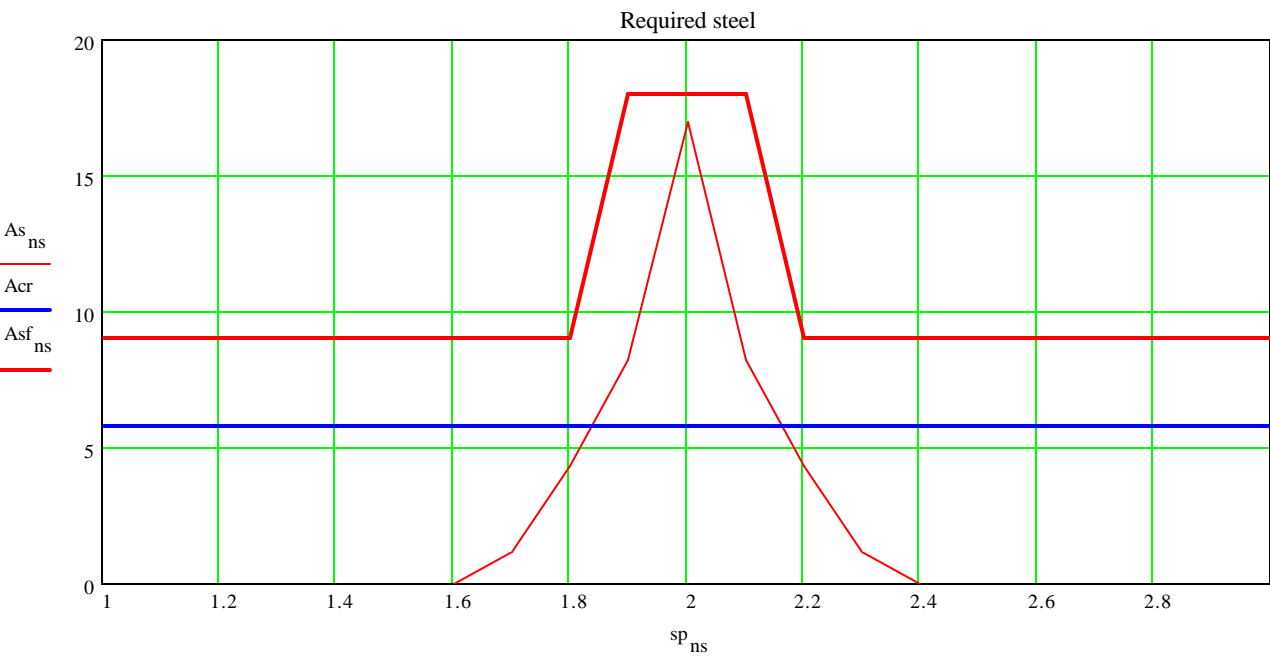


Embedment length (in)

$$embed := \max \left(\left(\begin{array}{c} 15 \cdot bd \\ d \\ \frac{span_0}{12} \cdot 12 \end{array} \right) \right)$$

embed = 77

Final bar output data



Size of bar used = size = 9

	0	1	2
0	1	0	9
1	1.1	0	9
2	1.2	0	9
3	1.3	0	9
4	1.4	0	9
5	1.5	0	9
6	1.6	0	9
7	1.7	1.112	9
8	1.8	4.295	9
9	1.9	8.197	18
10	2	16.955	18
11	2.1	8.204	18
12	2.2	4.295	9
13	2.3	1.112	9
14	2.4	0	9
15	2.5	0	9
16	2.6	0	9
17	2.7	0	9
18	2.8	0	9
19	2.9	0	9
20	3	0	9
21			

column 0 = span point
column 1 = Total area of steel required
column 2 = Number of bars per beam

disp =