

Client:
Project Location:
Project Desc:

Roof Desc:
Job Number:
Revision #:

Designed By:
Checked By:
Date:

Company Logo

Internal Pontoon Floating Roof Design Per API 650, Appendix H

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Internal Pontoon Floating Design

A. Introduction

This program designs pontoon floating roofs to the requirements of API 650, Appendix H (internal roofs)

Design methodologies are as follows:

1. Pontoon ring is designed using section properties determined in accordance with the AISI Cold-Formed Steel Design Manual (accounts for local buckling of plates with large width to thickness ratios)
2. Floating roof legs are designed in accordance with AISC 360, Latest Edition for loads listed in API 650, Appendix H.
3. Deck stresses and deflections are determined in accordance with the paper: "Stresses in Ruptured Floating Roofs", H.I. Epstein and J.R. Buzek, 1978 ASME Journal of Pressure Vessel Technology.
4. Pontoon ring is modeled as a ring on elastic foundation.
5. Pontoon ring strength is evaluated in accordance with AISI Cold-Formed Steel Design Manual.

B. Pontoon Geometry

Diameter

$$D := 220 \cdot \text{ft}$$

Rim space

$$S_{\text{rim}} := 8 \cdot \text{in}$$

Pontoon width

$$W_{\text{pon}} := 12 \cdot \text{ft}$$

Height of inner rim

$$H_{\text{ir}} := 30 \cdot \text{in}$$

Height of outer rim

$$H_{\text{or}} := 30 \cdot \text{in}$$

Width of inner rim extension

$$W_{\text{iExt}} := 0 \cdot \text{in}$$

Width of outer rim extension

$$W_{\text{oExt}} := 0 \cdot \text{in}$$

Height of outer rim extension

$$H_{\text{oExt}} := 3 \cdot \text{in}$$

Backslope

$$BS := 0 \cdot \text{in}$$

Cover slope

$$CS_{\text{min}} := -.1875 \cdot \frac{\text{in}}{\text{ft}}$$

Deck thickness

$$t_{\text{d}} := .1875 \cdot \text{in}$$

Cover thickness

$$t_{\text{c}} := .1875 \cdot \text{in}$$

Bulkhead thickness

$$t_{\text{bh}} := .1875 \cdot \text{in}$$

Inner rim thickness

$$t_{\text{ir}} := .75 \cdot \text{in}$$

Outer rim thickness

$$t_{\text{or}} := .75 \cdot \text{in}$$

Suggested number of bulkheads

$$\frac{(D - 2 \cdot S_{\text{rim}}) \cdot \pi}{17.75 \cdot \text{ft}} = 38.70$$

Suggested number of posts per rafter

$$\text{floor} \left(\frac{W_{\text{pon}}}{6 \cdot \text{ft}} \right) = 2.00$$

Rafters per Pontoon

$$N_{\text{rp}} := 2$$

Number of bulkheads

$$N_{\text{bh}} := 40$$

Posts per Rafter

$$N_{\text{pp}} := 2$$

Spacing of weld to rafter

$$S_{\text{wr}} := 12 \cdot \text{in}$$

Length of weld per spacing

$$L_{\text{wr}} := 2 \cdot \text{in}$$

Weld size for cover to rafter connection

$$t_{\text{wr}} := .1875 \cdot \text{in}$$

- Angle Rafters
 Channel Rafters

Angle Rafter

L2X2X3/16 / L51X51X4.8
L2-1/2X2X3/16 / L64X51X4.8
L2-1/2X2-1/2X3/16 / L64X64X4.8
L3X2X3/16 / L76X51X4.8

Channel Rafter

C3X4.1 / C75X6.1
C4X4.5 / C100X6.7
C3X5 / C75X7.4
C4X5.4 / C100X8

Internal Pontoon Floating Roof Design

C. Leg Geometry

- Low Legs Stops
- Low Leg Sleeves

Leg diameter

$$d_{legs} := 2.875 \cdot \text{in}$$

Leg thickness

$$t_{legs} := .276 \cdot \text{in}$$

Sleeve diameter

$$d_{slv} := 3.5 \cdot \text{in}$$

Sleeve thickness

$$t_{slv} := .216 \cdot \text{in}$$

Maximum leg spacing

$$S_{legMax} := 24 \cdot \text{ft}$$

Low leg setting

$$H_{low} := 3 \cdot \text{ft}$$

High leg setting

$$H_{hi} := 7 \cdot \text{ft}$$

Sleeve extension below deck

$$H_{dslv} := 3 \cdot \text{in}$$

Radius to deck legs

$$R_{legs} := \begin{pmatrix} 12 \\ 32 \\ 52 \\ 72 \end{pmatrix} \cdot \text{ft}$$

Pin height for deck legs

$$H_{pin} := \begin{pmatrix} 24 \\ 24 \\ 24 \\ 24 \end{pmatrix} \cdot \text{in}$$

$$\frac{D}{2} - S_{rim} - W_{pon} = 97.33 \text{ ft}$$

$$n := 1 \dots \text{rows}(R_{legs})$$

$$N_{legMin}_n := \text{ceil} \left(\frac{2 \cdot \pi \cdot R_{legs}_n}{S_{legMax}} \right)$$

$$N_{legMin} = \begin{pmatrix} 4.00 \\ 9.00 \\ 14.00 \\ 19.00 \end{pmatrix}$$

Number of deck legs at each radius

$$N_{legs} := \begin{pmatrix} 4 \\ 10 \\ 16 \\ 20 \end{pmatrix}$$

Number of inner rim legs

$$N_{irlegs} := 36$$

Internal Pontoon Floating Roof Design

D. Appurtenance Geometry

Center Weight Used?

Weight of pontoon manway

$$w_{pmw} := 75 \cdot \text{lbs}$$

Weight of center weight

$$W_{cw} := 1 \cdot \text{lbs}$$

Diameter of centerweight

$$D_{cw} := 20 \cdot \text{ft}$$

Length of ladder track

$$L_{ltr} := 45 \cdot \text{ft}$$

Number of deck manways

$$N_{dmw} := 2$$

Weight of deck manways

$$w_{dmw} := 100 \cdot \text{lbs}$$

Number of bleeder vents

$$N_{bv} := 2$$

Weight of bleeder vents

$$w_{bv} := 250 \cdot \text{lbs}$$

E. Corrosion Allowances

Outer rim corrosion allowance

$$CA_{or} := 0 \cdot \text{in}$$

Inner rim corrosion allowance

$$CA_{ir} := 0 \cdot \text{in}$$

Deck corrosion allowance

$$CA_d := 0 \cdot \text{in}$$

Cover plate corrosion allowance

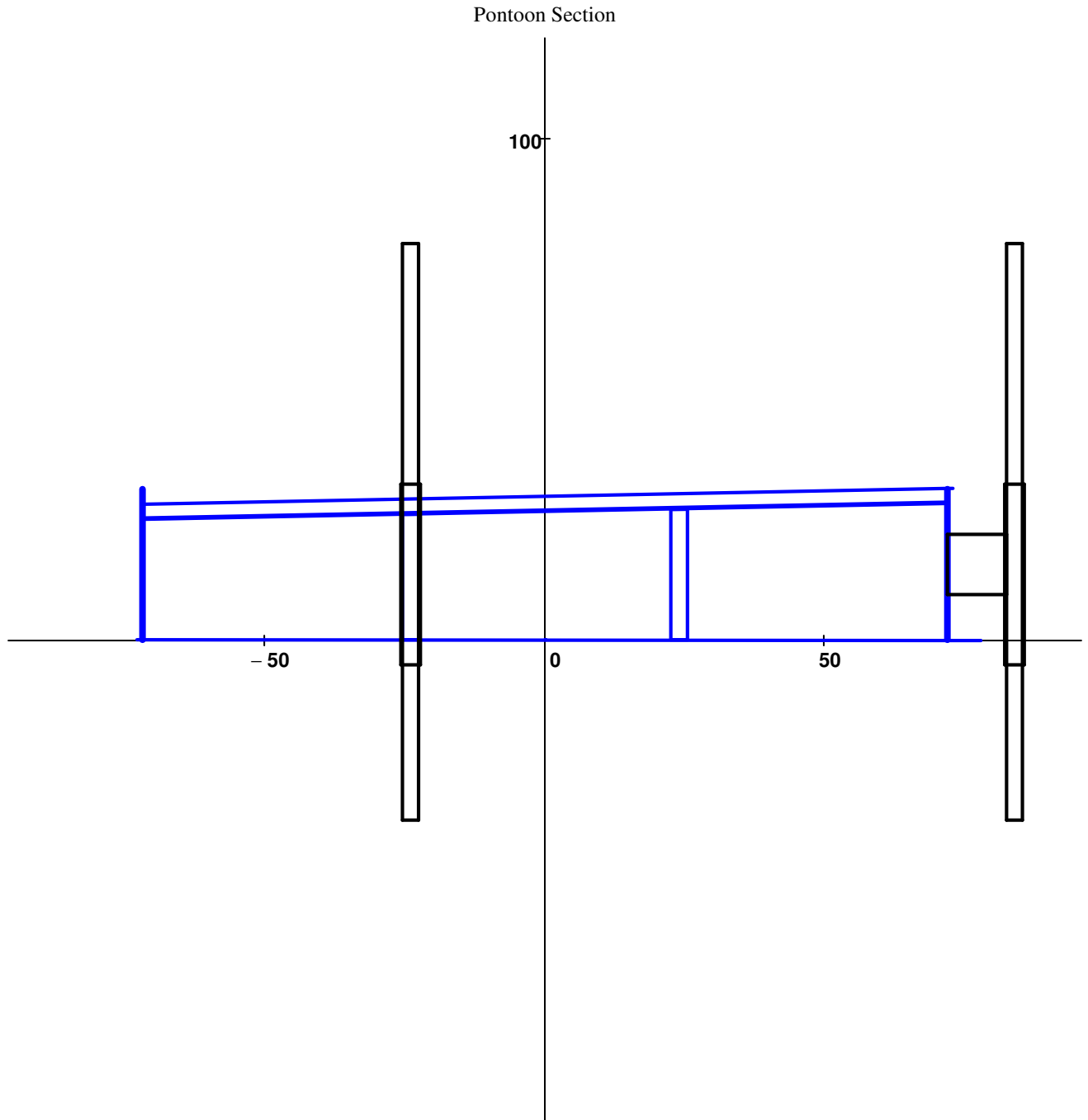
$$CA_c := 0 \cdot \text{in}$$

Corrosion allowance on legs

$$CA_{legs} := 0 \cdot \text{in}$$

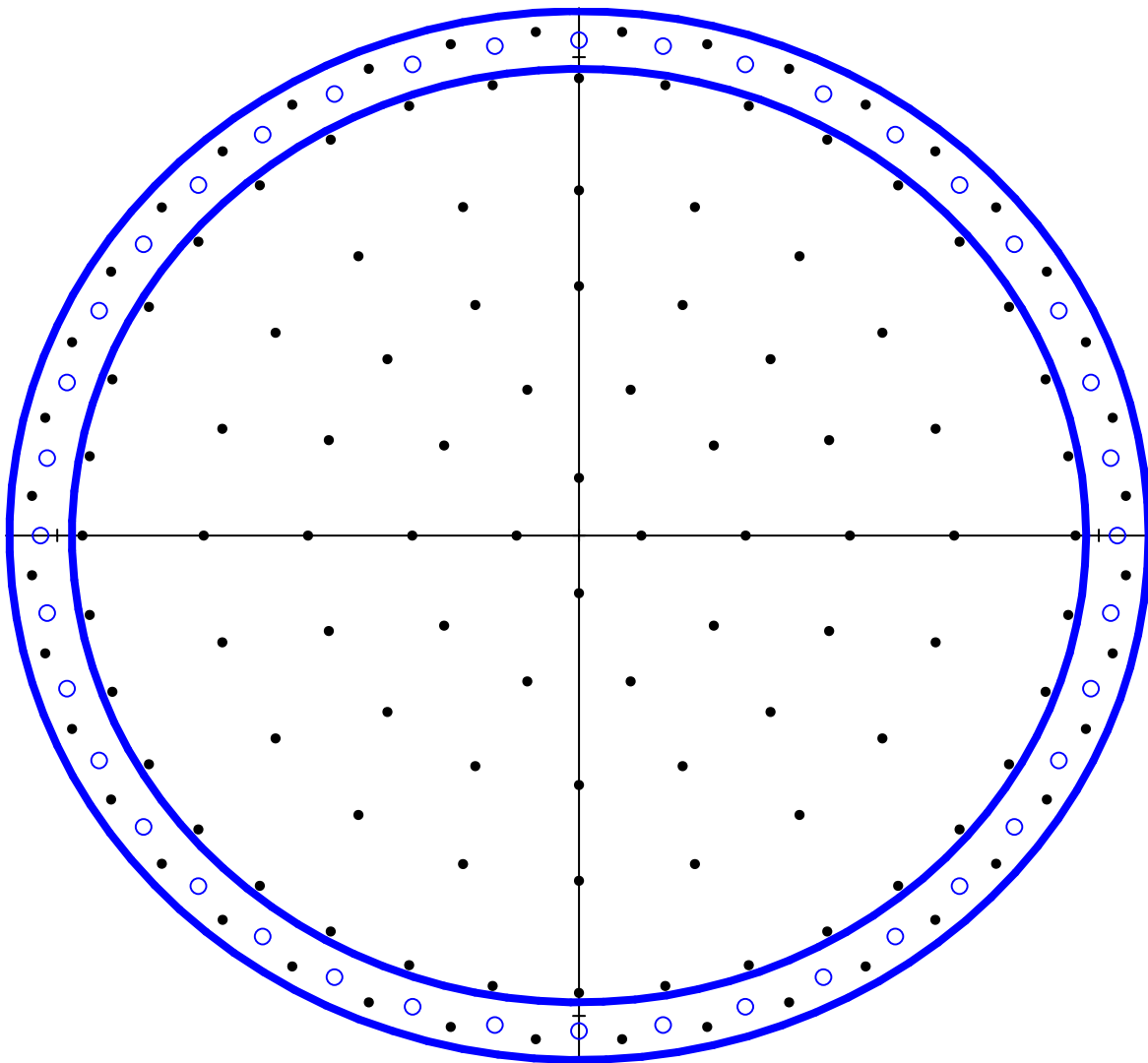
Internal Pontoon Floating Roof Design

SK



Internal Pontoon Floating Roof Design

Plan View of Roof



Internal Pontoon Floating Roof Design

E. Material Properties

Yield strength
of rim plate

$$F_{yrim} := 36 \cdot \text{ksi}$$

Yield strength of
deck plate

$$F_{yd} := 36 \cdot \text{ksi}$$

Yield strength
of plate

$$F_{yp} := 36 \cdot \text{ksi}$$

Yield strength
of rafter

$$F_{yr} := 36 \cdot \text{ksi}$$

Weld tensile strength

$$F_{uw} := 60 \cdot \text{ksi}$$

Leg yield strength

$$F_{ylegs} := 35 \cdot \text{ksi}$$

F. Design Criteria

Live load

$$LL := 12.5 \cdot \text{psf}$$

Minimum
specific gravity

$$SG_{min} := 0.7$$

Number of punctured
pontoons

$$N_p := 2$$

Friction from seal

$$\mu_{seal} := 15 \cdot \frac{\text{lbs}}{\text{ft}}$$

Unit weight of seal

$$w_{seal} := 20 \cdot \text{plf}$$

Radial force from seal

$$k_{seal} := 45 \cdot \frac{\text{lbs}}{\text{ft}}$$

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G. Roof Weight

$$W_{or} := t_{or} \cdot (H_{or} + W_{oExt}) \cdot 2 \cdot \pi \cdot R_{or} \cdot \gamma_s \quad W_{or} = 52595.50 \cdot \text{lbs} \quad \text{Weight of outer rim}$$

$$W_{ir} := t_{ir} \cdot (H_{ir} + W_{iExt}) \cdot 2 \cdot \pi \cdot R_{ir} \cdot \gamma_s \quad W_{ir} = 46822.82 \cdot \text{lbs} \quad \text{Weight of inner rim}$$

$$W_{cover} := \frac{W_{pon}}{\cos(\alpha_c)} \cdot \left[2 \cdot \pi \cdot \left(\frac{R_{ir} + R_{or}}{2} \right) \right] \cdot t_c \cdot \gamma_s \quad W_{cover} = 59663.93 \cdot \text{lbs} \quad \text{Weight of cover plate}$$

$$W_{BS} := \frac{W_{pon}}{\cos(\alpha_{BS})} \cdot \left[2 \cdot \pi \cdot \left(\frac{R_{ir} + R_{or}}{2} \right) \right] \cdot t_d \cdot \gamma_s \quad W_{BS} = 59650.99 \cdot \text{lbs} \quad \text{Weight of backslope}$$

$$W_{bh} := N_{bh} \cdot W_{pon} \cdot \left[\frac{H_{ir} + (H_{or} - H_{oExt})}{2} \right] \cdot t_{bh} \cdot \gamma_s \quad W_{bh} = 8728.13 \cdot \text{lbs} \quad \text{Weight of bulkheads}$$

$$w_{raft} = 4.10 \cdot \text{plf}$$

$$W_{raft} := N_{rp} \cdot N_{bh} \cdot \frac{W_{pon}}{\cos(\alpha_c)} \cdot w_{raft} \quad W_{raft} = 3936.85 \cdot \text{lbs} \quad \text{Weight of rafters}$$

$$W_{post} := N_{rp} \cdot N_{pp} \cdot N_{bh} \cdot \left(\frac{H_{or} - H_{oExt} + H_{ir}}{2} \right) \cdot w_{raft} \quad W_{post} = 1558.00 \cdot \text{lbs} \quad \text{Weight of posts}$$

$$W_{seal} := w_{seal} \cdot \pi \cdot D \quad W_{seal} = 13823.01 \cdot \text{lbs} \quad \text{Weight of seal}$$

$$F_{fseal} := \mu_{seal} \cdot \pi \cdot D \quad F_{fseal} = 10367.26 \cdot \text{lbs} \quad \text{Total frictional force on seal}$$

Internal Pontoon Floating Roof Design

G. Roof Weight

$$W_{deck} := \pi \cdot R_{ir}^2 \cdot t_d \cdot \gamma_s \cdot 1.05 \quad W_{deck} = 239264.61 \cdot \text{lbs} \quad \text{Weight of deck}$$

$$W_{slv} := \begin{cases} \left[\sum_{n=1}^{\text{rows}(H_{pin})} \left[(H_{pin_n} + H_{dslv} + 2 \cdot \text{in}) \cdot N_{legs_n} \right] \right] \cdot w_{slv} & \text{if SleeveType} = 1 \\ \left[\sum_{n=1}^{\text{rows}(H_{pin})} \left[(H_{pin_n} + H_{low} + 2 \cdot \text{in}) \cdot N_{legs_n} \right] \right] \cdot w_{slv} & \text{otherwise} \end{cases}$$

$$W_{slv} = 916.28 \cdot \text{lbs} \quad \text{Weight of deck sleeves}$$

$$W_{legs} := \sum_{n=1}^{\text{rows}(H_{pin})} \left[(H_{pin_n} + H_{dslv} + H_{hi} + 2 \cdot \text{in}) \cdot N_{legs_n} \right] \cdot w_{legs} \quad \text{Weight of deck legs}$$

$$W_{legs} = 3610.49 \cdot \text{lbs}$$

$$W_{pslv} := (N_{bh} \cdot H_{pslv} + N_{irlegs} \cdot H_{irslv}) \cdot w_{slv} \quad W_{pslv} = 1728.92 \cdot \text{lbs} \quad \text{Weight of pontoon sleeves}$$

$$W_{plegs} := [N_{bh} \cdot (H_{pslv} + H_{hi}) + N_{irlegs} \cdot (H_{irslv} + H_{hi})] \cdot w_{legs}$$

$$W_{plegs} = 5827.90 \cdot \text{lbs} \quad \text{Weight of pontoon legs}$$

$$W_{cw} = 1.00 \cdot \text{lbs} \quad \text{Weight of centerweight}$$

$$W_{pmw} := w_{pmw} \cdot N_{bh} \quad W_{pmw} = 3000.00 \cdot \text{lbs} \quad \text{Weight of pontoon manways}$$

$$W_{dmw} := N_{dmw} \cdot w_{dmw} \quad W_{dmw} = 200.00 \cdot \text{lbs} \quad \text{Weight of deck manways}$$

$$W_{bv} := N_{bv} \cdot w_{bv} \quad W_{bv} = 500.00 \cdot \text{lbs} \quad \text{Weight of bleeder vents}$$

Internal Pontoon Floating Roof Design

G. Roof Weight

$$W_{PON} := W_{or} + W_{ir} + W_{cover} + W_{BS} + W_{bh} + W_{raff} + W_{seal} + W_{plegs} + W_{pslv} + W_{pmw} + W_{post}$$

$$W_{PON} = 257336.05 \cdot \text{lbs} \quad \text{Total pontoon weight}$$

$$W_{dTOT} := W_{deck} + W_{legs} + W_{slv} + W_{bv} + W_{dmw} \quad \text{Total deck weight}$$

$$W_{dTOT} = 244491.38 \cdot \text{lbs}$$

$$W_{roof} := W_{PON} + W_{dTOT} \quad \text{Total roof weight}$$

$$W_{roof} = 501827.43 \cdot \text{lbs}$$

$$\gamma_{deck} := \frac{W_{dTOT}}{\pi \cdot R_{ir}^2} \quad \gamma_{deck} = 8.21 \cdot \text{psf} \quad \text{Unit weight of deck considering appurtenances}$$

H. Check Cover Slope

$$CS := \frac{H_{or} - H_{oExt} - BS - H_{ir}}{W_{pon}} = -0.25 \cdot \frac{\text{in}}{\text{ft}}$$

CS_{min}	= 75.00 %
CS	

Check minimum cover slope

Internal Pontoon Floating Roof Design

J. Check Rafters

RafterName = "C3X4.1"

Rafter size used

$w_{\text{rafter}} = 4.10 \cdot \text{plf}$

Weight of rafter per foot

$$S_{ro} := \frac{2 \cdot \pi \cdot R_{or}}{N_{bh} \cdot (N_{rp} + 1)} \quad S_{ro} = 5.72 \text{ ft}$$

Spacing at outer end of rafter

$$\frac{S_{ro}}{7 \cdot \text{ft}} = 81.78 \%$$

Check maximum spacing

$$S_{ri} := \frac{2 \cdot \pi \cdot R_{ir}}{N_{bh} \cdot (N_{rp} + 1)}$$

Spacing at inner end of rafter

$S_{ri} = 5.10 \text{ ft}$

$DL := \gamma_s \cdot t_c$

Dead load on rafter

$DL = 7.66 \cdot \text{psf}$

$LL = 12.50 \cdot \text{psf}$

Live load on rafter

Internal Pontoon Floating Roof Design

J. Check Rafters

$$q_1 := \begin{cases} S_{ro} \cdot DL + w_{raft} + S_{ro} \cdot LL & \text{if } W_{pon} > \frac{S_{ro}}{2} + \frac{S_{ri}}{2} \\ W_{pon} \cdot DL + w_{raft} + W_{pon} \cdot LL & \text{otherwise} \end{cases} \quad \begin{array}{l} \text{Uniform load toward outer end of} \\ \text{rafter} \end{array}$$

$$q_2 := \begin{cases} S_{ri} \cdot DL + w_{raft} + S_{ri} \cdot LL & \text{if } W_{pon} > \frac{S_{ro}}{2} + \frac{S_{ri}}{2} \\ W_{pon} \cdot DL + w_{raft} + W_{pon} \cdot LL & \text{otherwise} \end{cases} \quad \begin{array}{l} \text{Uniform load toward inner end of} \\ \text{rafter} \end{array}$$

$$x_1 := \begin{cases} \frac{S_{ro}}{2} & \text{if } W_{pon} > \frac{S_{ro}}{2} + \frac{S_{ri}}{2} \\ \frac{W_{pon}}{2} & \text{otherwise} \end{cases} \quad x_1 = 2.86 \text{ ft} \quad \begin{array}{l} \text{Location of } q_1 \text{ loading form outer} \\ \text{end} \end{array}$$

$$x_2 := \begin{cases} \frac{S_{ri}}{2} & \text{if } W_{pon} > \frac{S_{ro}}{2} + \frac{S_{ri}}{2} \\ \frac{W_{pon}}{2} & \text{otherwise} \end{cases} \quad x_2 = 2.55 \text{ ft} \quad \begin{array}{l} \text{Location of } q_2 \text{ loading form inner} \\ \text{end} \end{array}$$

$$x_3 := W_{pon} - x_1 - x_2$$

$$x_3 = 6.59 \text{ ft}$$

Width of transition loading

$$q_{ur}(x) := \begin{cases} \frac{x}{x_1} \cdot q_1 & \text{if } x < x_1 \\ q_1 - \frac{(x - x_1)}{x_3} \cdot (q_1 - q_2) & \text{if } (x \geq x_1) \cdot (x < x_1 + x_3) \\ q_2 - \frac{[x - (x_1 + x_3)]}{x_2} \cdot q_2 & \text{otherwise} \end{cases} \quad \begin{array}{l} \text{Uniform load as a function of } x \end{array}$$

Internal Pontoon Floating Roof Design

J. Check Rafters

$$R_1 := \frac{\int_{0 \cdot \text{ft}}^{W_{\text{pon}}} q_{\text{ur}}(x) \cdot x \, dx}{W_{\text{pon}}}$$

Reaction at outer end of rafter

$$R_1 = 0.52 \cdot \text{kip}$$

$$x_{\text{max}} := \begin{array}{l} \text{xx} \leftarrow \frac{W_{\text{pon}}}{3} \\ \text{while } \int_{0 \cdot \text{ft}}^{\text{xx}} q_{\text{ur}}(\text{xx}) \, d\text{xx} < R_1 \\ \text{xx} \leftarrow \text{xx} + .5 \cdot \text{in} \\ \text{xx} \end{array}$$

Location of maximum moment

$$x_{\text{max}} = 5.92 \text{ ft}$$

$$M_{\text{ur}}(x) := R_1 \cdot x - \int_{0 \cdot \text{ft}}^x q_{\text{ur}}(x_1) \cdot (x - x_1) \, dx_1$$

Ultimate moment in rafter

$$M_{\text{ur}}(x_{\text{max}}) = 1.86 \cdot \text{ft} \cdot \text{kip}$$

$$\Omega_B := 1.67$$

Safety factor for bending

$$M_{\text{nr}} := S_{\text{xr}} \cdot F_{\text{yr}}$$

Nominal moment capacity of rafter per AISC 360-05

$$\frac{M_{\text{ur}}(x_{\text{max}})}{M_{\text{nr}}} = 45.00 \cdot \%$$

Compare moment to nominal capacity

$$v_{\text{fr}} := \frac{R_1 \cdot Q_r}{I_{\text{xr}}} \quad v_{\text{fr}} = 0.15 \cdot \frac{\text{kip}}{\text{in}}$$

Ultimate shear flow at rafter cover connection

$$\Omega_w := 2$$

Safety factor for weld

$$v_{\text{fn}} := 0.6 \cdot .7071 \cdot t_{\text{wr}} \cdot \frac{L_{\text{wr}}}{S_{\text{wr}}} \cdot \frac{F_{\text{uw}}}{\Omega_w} \quad v_{\text{fn}} = 0.40 \cdot \frac{\text{kip}}{\text{in}}$$

Nominal shear strength of weld at rafter to cover connection

$$\frac{v_{\text{fr}}}{v_{\text{fn}}} = 38.88 \cdot \%$$

Compare shear flow to nominal capacity

Internal Pontoon Floating Roof Design

K. Check Legs

$$R_{\text{legs}} = \begin{pmatrix} 12.00 \\ 32.00 \\ 52.00 \\ 72.00 \end{pmatrix} \text{ ft}$$

$$N_{\text{legs}} = \begin{pmatrix} 4.00 \\ 10.00 \\ 16.00 \\ 20.00 \end{pmatrix}$$

$$N_{\text{irlegs}} = 36.00$$

$$N_{\text{bh}} = 40.00$$

$$TL_{\text{deck}} := \gamma_{\text{deck}} + LL$$

$$TL_{\text{deck}} = 20.71 \cdot \text{psf}$$

Deck load

Internal Pontoon Floating Roof Design

K. Check Legs

$$P_{ulegs} := \text{for } i \in 1.. \text{rows}(R_{legs})$$

$$P_i \leftarrow \frac{\pi \cdot \left(\frac{R_{legs_i} + R_{ir}}{2} \right)^2 \cdot TL_{deck}}{N_{legs_i}} \quad \text{if } (i = 1) \cdot (i = \text{rows}(R_{legs}))$$

$$P_i \leftarrow \frac{\pi \cdot \left[\left(\frac{R_{legs_{i+1}} + R_{legs_i}}{2} \right)^2 - \left(\frac{R_{legs_i} + R_{legs_{i-1}}}{2} \right)^2 \right] \cdot TL_{deck}}{N_{legs_i}} \quad \text{if } (i > 1) \cdot (i < \text{rows}(R_{legs}))$$

$$P_i \leftarrow \frac{\pi \cdot \left[\left(\frac{R_{legs_{i+1}} + R_{legs_i}}{2} \right)^2 \right] \cdot TL_{deck}}{N_{legs_i}} \quad \text{if } (i = 1) \cdot (i < \text{rows}(R_{legs})) \cdot (R_{legs_i} > 0 \cdot \text{ft})$$

$$P_i \leftarrow \frac{1}{2} \cdot \frac{\pi \cdot \left[(R_{legs_{i+1}})^2 \right] \cdot TL_{deck}}{N_{legs_i}} \quad \text{if } (i = 1) \cdot (i < \text{rows}(R_{legs})) \cdot (R_{legs_i} = 0 \cdot \text{ft})$$

$$P_i \leftarrow \frac{\pi \cdot \left[\left(\frac{R_{ir} + R_{legs_i}}{2} \right)^2 - \left(\frac{R_{legs_i} + R_{legs_{i-1}}}{2} \right)^2 \right] \cdot TL_{deck}}{N_{legs_i}} \quad \text{if } (i > 1) \cdot (i = \text{rows}(R_{legs}))$$

$$P_i \leftarrow \frac{\pi \cdot \left[\left(\frac{R_{legs_{i+1}} + R_{legs_i}}{2} \right)^2 - \left(\frac{R_{legs_i} + R_{legs_{i-1}}}{2} \right)^2 \right] \cdot TL_{deck}}{N_{legs_i}} \quad \text{otherwise}$$

$$P$$

$$P_{ulegs} = \begin{pmatrix} 7.87 \\ 8.33 \\ 8.46 \\ 10.82 \end{pmatrix} \cdot \text{kip}$$

Load at deck legs

Internal Pontoon Floating Roof Design

K. Check Legs

$$P_{uirlegs} := \begin{cases} \frac{\pi \cdot \left[(R_{ir})^2 - \left(\frac{R_{ir} + R_{legs_rows}(R_{legs})}{2} \right)^2 \right] \cdot TL_{deck} + \frac{1}{4} \cdot \frac{1.2 \cdot W_{PON}}{N_{irlegs}}}{N_{irlegs}} \dots & \text{if } N_{irlegs} > 0 \\ \frac{1}{4} \cdot \frac{1.6 \cdot \left[\pi \cdot (R_{or}^2 - R_{ir}^2) \right] \cdot LL}{N_{bh}} & \\ 0 \cdot \text{kip} & \text{otherwise} \end{cases}$$

$P_{uirlegs} = 7.29 \cdot \text{kip}$

Load at inner rim legs

$$P_{uplegs} := \begin{cases} \frac{\pi \cdot \left[(R_{ir})^2 - \left(\frac{R_{ir} + R_{legs_rows}(R_{legs})}{2} \right)^2 \right] \cdot TL_{deck} + \frac{1.2 \cdot W_{PON}}{N_{bh}}}{N_{bh}} \dots & \text{if } N_{irlegs} = 0 \\ \frac{1.6 \cdot \left[\pi \cdot (R_{or}^2 - R_{ir}^2) \right] \cdot LL}{N_{bh}} & \\ \frac{3}{4} \cdot \frac{1.2 \cdot W_{PON}}{N_{bh}} + \frac{3}{4} \cdot \frac{1.6 \cdot \left[\pi \cdot (R_{or}^2 - R_{ir}^2) \right] \cdot LL}{N_{bh}} & \text{otherwise} \end{cases}$$

$P_{uplegs} = 8.71 \cdot \text{kip}$

Load at pontoon legs

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K. Check Legs

$$PR_{TOT} := N_{bh} \cdot P_{uplegs} \cdot \left(R_{ir} + \frac{2}{3} \cdot W_{pon} \right) + N_{irlegs} \cdot P_{uirlegs} \cdot R_{ir}$$

$$PR_{TOT} = 62234.58 \text{ ft} \cdot \text{kip}$$

$$QR_{TOT} := \sum_{n=1}^{\text{rows}(R_{legs})} \left(P_{ulegs_n} \cdot N_{legs_n} \cdot R_{legs_n} \right)$$

$$QR_{TOT} = 25659.11 \text{ ft} \cdot \text{kip}$$

$$K_{plegs} := 2.0 \cdot \sqrt{\frac{QR_{TOT} + PR_{TOT}}{PR_{TOT}}}$$

$$K_{plegs} = 2.38$$

$$K_{legs} := 1.0$$

Internal Pontoon Floating Roof Design

K. Check Legs

$$d_{\text{legs}} = 2.88 \cdot \text{in}$$

Leg diameter

$$t_{\text{legs}} = 0.28 \cdot \text{in}$$

Leg thickness

$$d_{\text{clegs}} := d_{\text{legs}} - 2 \cdot CA_{\text{legs}}$$

Leg diameter - corroded

$$t_{\text{clegs}} := t_{\text{legs}} - CA_{\text{legs}}$$

Leg thickness - corroded

$$A_{\text{clegs}} := \frac{\pi}{4} \cdot \left[(d_{\text{clegs}})^2 - (d_{\text{clegs}} - 2 \cdot t_{\text{clegs}})^2 \right]$$

Leg cross sectional area - corroded

$$A_{\text{clegs}} = 2.25 \cdot \text{in}^2$$

$$I_{\text{clegs}} := \frac{\pi}{64} \cdot \left[(d_{\text{clegs}})^4 - (d_{\text{clegs}} - 2 \cdot t_{\text{clegs}})^4 \right]$$

Moment of inertia - corroded

$$I_{\text{clegs}} = 1.92 \cdot \text{in}^4$$

$$S_{\text{clegs}} := \frac{2 \cdot I_{\text{clegs}}}{d_{\text{clegs}}}$$

$$S_{\text{clegs}} = 1.34 \cdot \text{in}^3$$

Section modulus

$$r_{\text{clegs}} := \sqrt{\frac{I_{\text{clegs}}}{A_{\text{clegs}}}}$$

$$r_{\text{clegs}} = 0.92 \cdot \text{in}$$

Radius of gyration

Internal Pontoon Floating Roof Design

K. Check Legs

$$\lambda_{plegs} := \frac{K_{plegs} \cdot \left[H_{hi} - \left(\frac{2}{3} \cdot BS \right) - H_{dslv} \right]}{r_{clegs}} \quad \lambda_{plegs} = 208.34$$

$$F_{Eplegs} := \frac{\pi^2 \cdot E_s}{(\lambda_{plegs})^2} \quad \text{Euler buckling load for pontoon legs}$$

$$F_{crplegs} := \begin{cases} \frac{F_{ylegs}}{F_{Eplegs}} \cdot F_{ylegs} & \text{if } \lambda_{plegs} \leq 4.71 \cdot \sqrt{\frac{E_s}{F_{ylegs}}} \\ 0.877 \cdot F_{Eplegs} & \text{otherwise} \end{cases}$$

$$F_{crplegs} = 5782.75 \text{ psi} \quad \text{Critical buckling load for pontoon legs}$$

$$\Omega_C := 1.67 \quad \text{Safety factor for compression}$$

$$P_{nplegs} := \frac{F_{crplegs} \cdot A_{clegs}}{\Omega_C} = 7803.384 \text{ lbs} \quad \text{Allowable Strength fo pontoon legs}$$

$$\frac{P_{uplegs}}{P_{nplegs}} = 111.64\% \quad \text{Check pontoon legs}$$

$$F_{Eirlegs} := \frac{\pi^2 \cdot E_s}{(\lambda_{plegs})^2} \quad \text{Euler buckling load for inner rim legs}$$

$$F_{crrlegs} := \begin{cases} \frac{F_{ylegs}}{F_{Eirlegs}} \cdot F_{ylegs} & \text{if } \lambda_{plegs} \leq 4.71 \cdot \sqrt{\frac{E_s}{F_{ylegs}}} \\ 0.877 \cdot F_{Eirlegs} & \text{otherwise} \end{cases}$$

$$F_{crrlegs} = 5782.75 \text{ psi} \quad \text{Critical buckling load for inner rim legs}$$

$$P_{nirlegs} := \frac{F_{crrlegs} \cdot A_{clegs}}{\Omega_C} = 7803.384 \text{ lbs} \quad \text{Allowable Strength fo inner rim legs}$$

$$\frac{P_{uirlegs}}{P_{nirlegs}} = 93.37\% \quad \text{Check inner rim legs}$$

Internal Pontoon Floating Roof Design

K. Check Legs

$$\lambda_{\text{legs}} := \frac{K_{\text{legs}} \cdot H_{\text{hi}}}{r_{\text{clegs}}} \quad \lambda_{\text{legs}} = 90.90$$

$$F_{\text{Elegs}} := \frac{\pi^2 \cdot E_s}{(\lambda_{\text{legs}})^2} \quad \text{Euler buckling load for deck legs}$$

$$F_{\text{crlegs}} := \begin{cases} \frac{F_{\text{ylegs}}}{F_{\text{Elegs}}} \cdot F_{\text{ylegs}} & \text{if } \lambda_{\text{legs}} \leq 4.71 \cdot \sqrt{\frac{E_s}{F_{\text{ylegs}}}} \\ 0.877 \cdot F_{\text{Elegs}} & \text{otherwise} \end{cases}$$

$$F_{\text{crlegs}} = 22929.02 \text{ psi}$$

Critical buckling load for deck rim legs

$$P_{\text{nlegs}} := \frac{F_{\text{crlegs}} \cdot A_{\text{clegs}}}{\Omega_C} = 30940.989 \text{ lbs}$$

Allowable Strength for deck legs

$\frac{P_{\text{ulegs}}}{P_{\text{nlegs}}} =$	25.45	.%
	26.92	
	27.34	
	34.96	

Check deck legs

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$H_{BScone} := R_{or} \cdot \tan\left(\operatorname{atan}\left(\frac{BS}{W_{pon}}\right)\right)$$

$$H_{BStrunc} := H_{BScone} - BS$$

$$V_{BS} := \pi \cdot R_{or}^2 \cdot BS - \left(\frac{\pi}{3} \cdot R_{or}^2 \cdot H_{BScone} - \frac{\pi}{3} \cdot R_{ir}^2 \cdot H_{BStrunc}\right)$$

$$w_{dNET} := \frac{W_{dTOT}}{\pi R_{ir}^2} \cdot \left(\frac{\gamma_s - SG_{min} \cdot \gamma_w}{\gamma_s}\right)$$

$$\frac{W_{PON} + w_{dNET} \cdot \pi \cdot R_{ir}^2 - V_{BS} \cdot SG_{min} \cdot \gamma_w}{\pi \cdot (R_{or}^2 - R_{ir}^2) \cdot SG_{min} \cdot \gamma_w} = 1.41 \cdot \text{ft}$$

$$CRise := H_{or} - H_{oExt} - H_{ir} - BS$$

$$b_c := \sqrt{CRise^2 + W_{pon}^2}$$

$$b_c = 144.03 \cdot \text{in}$$

$$b_{BS} := \sqrt{BS^2 + W_{pon}^2} \quad b_{BS} = 12.00 \text{ ft}$$

$$\theta_{BS} := \operatorname{atan}\left(\frac{BS}{W_{pon}}\right)$$

$$A_p := b_{BS} \cdot t_d + b_c \cdot t_c + (H_{ir} + W_{iExt}) \cdot t_{ir} + (H_{or} + W_{oExt}) \cdot t_{or}$$

$$A_p = 99.01 \cdot \text{in}^2$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$c_{py} := \frac{1}{A_p} \left[\begin{aligned} &H_{or} \cdot (t_{or} - CA_{or}) \cdot \frac{H_{or}}{2} + H_{ir} \cdot (t_{ir} - CA_{ir}) \cdot \left(BS + \frac{H_{ir}}{2} \right) \dots \\ &+ b_c \cdot (t_c - CA_c) \cdot \left(\frac{H_{or} - H_{oExt} + BS + H_{ir}}{2} \right) \dots \\ &+ b_{BS} \cdot (t_d - CA_d) \cdot \left(\frac{BS}{2} \right) \dots \\ &+ W_{oExt} \cdot (t_{or} - CA_{or}) \cdot H_{or} + W_{iExt} \cdot (t_{ir} - CA_{ir}) \cdot (BS + H_{ir}) \end{aligned} \right]$$

$$c_{py} = 14.59 \cdot \text{in}$$

$$I_{zp} := \frac{(t_{or} - CA_{or}) \cdot H_{or}^3}{12} + \frac{(t_{ir} - CA_{ir}) \cdot H_{ir}^3}{12} + H_{or} \cdot (t_{or} - CA_{or}) \cdot \left(\frac{H_{or}}{2} - c_{py} \right)^2 \dots$$

$$+ H_{ir} \cdot (t_{ir} - CA_{ir}) \cdot \left(BS + \frac{H_{ir}}{2} - c_{py} \right)^2 + b_c \cdot (t_c - CA_c) \cdot \left(\frac{H_{or} - H_{oExt} + BS + H_{ir}}{2} - c_{py} \right)^2 \dots$$

$$+ W_{iExt} \cdot (t_{ir} - CA_{ir}) \cdot (BS + H_{ir} - c_{py})^2 \dots$$

$$+ \int_{0 \cdot \text{ft}}^{W_{pon}} \frac{(t_d - CA_d) \cdot \left(\frac{x}{W_{pon}} \cdot BS - c_{py} \right)^2}{\cos(\theta_{BS})} dx + W_{oExt} \cdot (t_{or} - CA_{or}) \cdot (H_{or} - c_{py})^2$$

$$I_{zp} = 14355.32 \cdot \text{in}^4$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$c_{px} := \frac{1}{A_p} \left[H_{or} \cdot \frac{(t_{or})^2}{2} + H_{ir} \cdot (t_{ir}) \cdot W_{pon} + \frac{W_{oExt}^2 \cdot (t_{or})}{2} \dots \right]$$

$$+ W_{iExt} \cdot (t_{ir}) \cdot \left(W_{pon} + \frac{W_{iExt}}{2} \right) \dots$$

$$+ b_c \cdot (t_c) \cdot \left(\frac{W_{pon}}{2} \right) \dots$$

$$+ b_{BS} \cdot (t_d) \cdot \left(\frac{W_{pon}}{2} \right)$$

$$c_{px} = 6.01 \text{ ft}$$

$$I_{yp} := H_{or} \cdot (t_{or} - CA_{or}) \cdot \left(c_{px} - \frac{t_{or} - CA_{or}}{2} \right)^2 + H_{ir} \cdot (t_{ir} - CA_{ir}) \cdot (W_{pon} - c_{px})^2 \dots$$

$$+ \frac{(t_c - CA_c) \cdot (b_c)^3}{12} + (t_c - CA_c) \cdot b_c \cdot \left(c_{px} - \frac{b_c}{2} \right)^2 \dots$$

$$+ \frac{(t_d - CA_d) \cdot (b_{BS})^3}{12} + (t_d - CA_d) \cdot b_{BS} \cdot \left(c_{px} - \frac{b_{BS}}{2} \right)^2 \dots$$

$$+ \frac{(t_{or} - CA_{or}) \cdot W_{oExt}^3}{12} + (t_{or} - CA_{or}) \cdot W_{oExt} \cdot \left(c_{px} - \frac{W_{oExt}}{2} \right)^2 \dots$$

$$+ \frac{(t_{ir} - CA_{ir}) \cdot W_{iExt}^3}{12} + (t_{ir} - CA_{ir}) \cdot W_{iExt} \cdot \left(W_{pon} + \frac{W_{iExt}}{2} - c_{px} \right)^2$$

$$I_{yp} = 325409.76 \cdot \text{in}^4$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$C_{wCH}(d, bf, tf, tw) := \frac{tf \cdot (d - tf)^2 \cdot \left(bf - \frac{tw}{2}\right)^3}{6} \cdot \left[\frac{\left(bf - \frac{tw}{2}\right) \cdot tf + 2 \cdot (d - tf) \cdot tw}{(d - tf) \cdot tw + 2 \cdot \left(bf - \frac{tw}{2}\right) \cdot tw} \right]$$

$$A_{pJ} := \left(\frac{H_{or} - H_{oExt} + H_{ir}}{2} \right) (W_{pon})$$

$$J_{BHP} := \frac{W_{pon} \cdot (t_d - CA_d)^3}{3} + \frac{H_{or} \cdot (t_{or} - CA_{or})^3}{3} + \frac{H_{ir} \cdot (t_{ir} - CA_{ir})^3}{3} \dots$$

$$+ \frac{W_{oExt} \cdot (t_{or} - CA_{or})^3}{3} + \frac{W_{iExt} \cdot (t_{ir} - CA_{ir})^3}{3}$$

$$J_{BHP} = 8.75 \cdot \text{in}^4$$

$$J_{RSF} := \frac{4 \cdot A_{pJ}^2}{\frac{H_{or} - H_{oExt}}{t_{or} - CA_{or}} + \frac{H_{ir}}{t_{ir} - CA_{ir}} + \frac{b_c}{t_c - CA_c} + \frac{b_{BS}}{t_d - CA_d}}$$

$$J := \begin{cases} J_{RSF} & \text{if RoofType} = 1 \\ J_{BHP} & \text{otherwise} \end{cases}$$

$$J = 41789.27 \cdot \text{in}^4$$

Torsional constant

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$t_{fCw} := \begin{cases} t_{ir} - CA_{ir} & \text{if } H_{or} > H_{ir} \\ t_{or} - CA_{or} & \text{if } H_{ir} > H_{or} \\ \min(t_{ir} - CA_{ir}, t_{or} - CA_{or}) & \text{otherwise} \end{cases}$$

$$t_{f2Cw} := \begin{cases} t_{or} - CA_{or} & \text{if } H_{or} > H_{ir} \\ t_{ir} - CA_{ir} & \text{if } H_{ir} > H_{or} \\ \max(t_{ir} - CA_{ir}, t_{or} - CA_{or}) & \text{otherwise} \end{cases}$$

$$\alpha_w := \frac{1}{1 + \left(\frac{\min(H_{or}, H_{ir})}{\max(H_{or}, H_{ir})} \right)^3 \cdot \frac{t_{fCw}}{t_{f2Cw}}}$$

$$\alpha_w = 0.50$$

$$R_{eff} := \frac{D}{2} - S_{rim} - c_{px} \quad R_{eff} = 103.33 \text{ ft} \quad \text{Effective radius of roof}$$

$$C_w := \begin{cases} 0 \cdot \text{in}^6 & \text{if } \text{RoofType} = 1 \\ C_{wCH}(W_{pon}, \min(H_{or}, H_{ir}), t_{fCw}, t_d - CA_d) \cdot \alpha_w & \text{otherwise} \end{cases} \quad \text{Warping constant}$$

$$C_w = 0.00 \cdot \text{in}^6$$

$$C_T := \frac{\pi^2 \cdot E_s \cdot C_w}{(1.7725 \cdot R_{eff})^2} + G \cdot J \quad \text{Torsional rigidity}$$

$$C_T = 4.66 \times 10^{11} \cdot \text{lbs} \cdot \text{in}^2$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$F_{\text{crd}} := \frac{4 \cdot \pi^2 \cdot E_S}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_d - CA_d}{b_{BS}} \right)^2 = 177.75 \text{ psi}$$

$$F_{\text{crc}} := \frac{4 \cdot \pi^2 \cdot E_S}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_c - CA_c}{b_c} \right)^2 = 177.67 \text{ psi}$$

$$F_{\text{cror}} := \frac{4 \cdot \pi^2 \cdot E_S}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_{or} - CA_{or}}{H_{or} - H_{oExt}} \right)^2$$

$$F_{\text{cror}} = 80896.57 \text{ psi}$$

$$F_{\text{crir}} := \frac{4 \cdot \pi^2 \cdot E_S}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_{ir} - CA_{ir}}{H_{ir}} \right)^2$$

$$F_{\text{crir}} = 65526.22 \text{ psi}$$

$$\lambda_{\text{crd}}(f) := \sqrt{\frac{f}{F_{\text{crd}}}}$$

$$\lambda_{\text{crc}}(f) := \sqrt{\frac{f}{F_{\text{crc}}}}$$

$$\lambda_{\text{cror}}(f) := \sqrt{\frac{f}{F_{\text{cror}}}}$$

$$\lambda_{\text{crir}}(f) := \sqrt{\frac{f}{F_{\text{crir}}}}$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$\rho_{\text{crd}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{crd}}(f)}}{\lambda_{\text{crd}}(f)}$$

$$\rho_{\text{crc}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{crc}}(f)}}{\lambda_{\text{crc}}(f)}$$

$$\rho_{\text{cror}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{cror}}(f)}}{\lambda_{\text{cror}}(f)}$$

$$\rho_{\text{cir}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{cir}}(f)}}{\lambda_{\text{cir}}(f)}$$

$$b_{\text{effd}}(f) := \begin{cases} b_{\text{BS}} & \text{if } \lambda_{\text{crd}}(f) \leq .673 \\ \rho_{\text{crd}}(f) \cdot b_{\text{BS}} & \text{otherwise} \end{cases}$$

$$b_{\text{effc}}(f) := \begin{cases} W_{\text{pon}} & \text{if } \lambda_{\text{crc}}(f) \leq .673 \\ \rho_{\text{crc}}(f) \cdot b_{\text{c}} & \text{otherwise} \end{cases}$$

$$b_{\text{effor}}(f) := \begin{cases} H_{\text{or}} & \text{if } \lambda_{\text{cror}}(f) \leq .673 \\ \rho_{\text{cror}}(f) \cdot (H_{\text{or}} - H_{\text{oExt}}) + H_{\text{oExt}} & \text{otherwise} \end{cases}$$

$$b_{\text{effir}}(f) := \begin{cases} H_{\text{ir}} & \text{if } \lambda_{\text{cir}}(f) \leq .673 \\ \rho_{\text{cir}}(f) \cdot (H_{\text{ir}}) & \text{otherwise} \end{cases}$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$A_{\text{effC}}(f) := b_{\text{effor}}(f) \cdot (t_{\text{or}} - CA_{\text{or}}) + b_{\text{effir}}(f) \cdot (t_{\text{ir}} - CA_{\text{ir}}) + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) + b_{\text{effd}}(f) \cdot (t_{\text{d}} - CA_{\text{d}}) \dots \\ + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) + H_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}})$$

$$c_{\text{effC}}(f) := \frac{1}{A_{\text{effC}}(f)} \left[b_{\text{effor}}(f) \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \frac{(H_{\text{or}} - H_{\text{oExt}})}{2} + b_{\text{effir}}(f) \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(BS + \frac{H_{\text{ir}}}{2} \right) \dots \right. \\ \left. + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) \cdot \left(\frac{H_{\text{or}} - H_{\text{oExt}} + BS + H_{\text{ir}}}{2} \right) \dots \right. \\ \left. + b_{\text{effd}}(f) \cdot (t_{\text{d}} - CA_{\text{d}}) \cdot \left(\frac{BS}{2} \right) + H_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left(H_{\text{or}} - \frac{H_{\text{oExt}}}{2} \right) \dots \right. \\ \left. + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot H_{\text{or}} + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot (BS + H_{\text{ir}}) \right]$$

$$K_{\text{rad}} := \frac{R_{\text{ir}} \cdot R_{\text{eff}}}{A_{\text{p}} \cdot E_{\text{s}}}$$

$$K_{\text{rad}} = 5.04 \times 10^{-4} \cdot \frac{\text{in}^2}{\text{lbs}}$$

Radial flexibility of pontoon ring

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$\begin{aligned}
 I_{\text{effC}}(f) := & \frac{(t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{effor}}(f)}{2} + H_{\text{oExt}} \right)^3}{12} + \frac{(t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{effor}}(f)}{2} \right)^3}{12} \dots \\
 & + \frac{b_{\text{effor}}(f)}{2} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{effor}}(f)}{4} - c_{\text{effC}}(f) \right)^2 + \frac{2 \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(\frac{b_{\text{effir}}(f)}{2} \right)^3}{12} \dots \\
 & + \left(\frac{b_{\text{effor}}(f)}{2} + H_{\text{oExt}} \right) \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left[\left(H_{\text{or}} - \frac{\frac{b_{\text{effor}}(f)}{2} + H_{\text{oExt}}}{2} \right) - c_{\text{effC}}(f) \right]^2 \dots \\
 & + \frac{b_{\text{effir}}(f)}{2} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(\frac{b_{\text{effir}}(f)}{4} + BS - c_{\text{effC}}(f) \right)^2 \dots \\
 & + \frac{b_{\text{effir}}(f)}{2} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left[\left(H_{\text{ir}} + BS - \frac{b_{\text{effir}}(f)}{4} \right) - c_{\text{effC}}(f) \right]^2 \dots \\
 & + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) \cdot \left(\frac{H_{\text{or}} - H_{\text{oExt}} + H_{\text{ir}}}{2} - c_{\text{effC}}(f) \right)^2 \dots \\
 & + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot (BS + H_{\text{ir}} - c_{\text{effC}}(f))^2 + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot (H_{\text{or}} - c_{\text{effC}}(f))^2 \dots \\
 & + \frac{b_{\text{effd}}(f)}{2} \cdot (t_{\text{d}} - CA_{\text{d}}) \cdot \left(c_{\text{effC}}(f) - \frac{b_{\text{effd}}(f)}{4} \cdot \frac{BS}{W_{\text{pon}}} \right)^2 \dots \\
 & + \frac{b_{\text{effd}}(f)}{2} \cdot (t_{\text{d}} - CA_{\text{d}}) \cdot \left[c_{\text{effC}}(f) - \left(BS - \frac{b_{\text{effd}}(f)}{4} \cdot \frac{BS}{W_{\text{pon}}} \right) \right]^2
 \end{aligned}$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$F_{\text{crorB}} := \frac{24 \cdot \pi^2 \cdot E_s}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_{\text{or}}}{H_{\text{or}} - H_{\text{oExt}}} \right)^2$$

$$F_{\text{crorB}} = 485379.41 \text{ psi}$$

$$F_{\text{cricrB}} := \frac{24 \cdot \pi^2 \cdot E_s}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t_{\text{ir}}}{H_{\text{ir}}} \right)^2$$

$$F_{\text{cricrB}} = 393157.32 \text{ psi}$$

$$\lambda_{\text{crorB}}(f) := \sqrt{\frac{f}{F_{\text{cror}}}}$$

$$\lambda_{\text{cricrB}}(f) := \sqrt{\frac{f}{F_{\text{cricr}}}}$$

$$\rho_{\text{crorB}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{cror}}(f)}}{\lambda_{\text{cror}}(f)}$$

$$\rho_{\text{cricrB}}(f) := \frac{1 - \frac{.22}{\lambda_{\text{cricr}}(f)}}{\lambda_{\text{cricr}}(f)}$$

$$b_{\text{efforB}}(f) := \begin{cases} H_{\text{or}} - H_{\text{oExt}} & \text{if } \lambda_{\text{crorB}}(f) \leq .673 \\ \rho_{\text{crorB}}(f) \cdot (H_{\text{or}} - H_{\text{oExt}}) & \text{otherwise} \end{cases}$$

$$b_{\text{effirB}}(f) := \begin{cases} H_{\text{ir}} & \text{if } \lambda_{\text{cricrB}}(f) \leq .673 \\ \rho_{\text{cricrB}}(f) \cdot (H_{\text{ir}}) & \text{otherwise} \end{cases}$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$A_{\text{effB}}(f) := b_{\text{efforB}}(f) \cdot (t_{\text{or}} - CA_{\text{or}}) + b_{\text{effirB}}(f) \cdot (t_{\text{ir}} - CA_{\text{ir}}) + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) + b_{\text{BS}} \cdot (t_{\text{d}} - CA_{\text{d}}) \dots \\ + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) + H_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}})$$

$$c_{\text{effB}}(f) := \frac{1}{A_{\text{effB}}(f)} \left[b_{\text{efforB}}(f) \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \frac{(H_{\text{or}} - H_{\text{oExt}})}{2} + b_{\text{effirB}}(f) \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(BS + \frac{H_{\text{ir}}}{2} \right) \dots \right. \\ \left. + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) \cdot \left(\frac{H_{\text{or}} - H_{\text{oExt}} + BS + H_{\text{ir}}}{2} \right) \dots \right. \\ \left. + b_{\text{BS}} \cdot (t_{\text{d}} - CA_{\text{d}}) \cdot \left(\frac{BS}{2} \right) + H_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left(H_{\text{or}} - \frac{H_{\text{oExt}}}{2} \right) \dots \right. \\ \left. + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot H_{\text{or}} + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot (BS + H_{\text{ir}}) \right]$$

Internal Pontoon Floating Roof Design

L. Pontoon Ring Section Properties

$$\begin{aligned}
 I_{\text{effB}}(f) := & \frac{(t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{efforB}}(f)}{2} + H_{\text{oExt}} \right)^3}{12} + \frac{(t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{efforB}}(f)}{2} \right)^3}{12} \dots \\
 & + \frac{b_{\text{efforB}}(f)}{2} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left(\frac{b_{\text{efforB}}(f)}{4} - c_{\text{effB}}(f) \right)^2 + \frac{2 \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(\frac{b_{\text{effirB}}(f)}{2} \right)^3}{12} \dots \\
 & + \left(\frac{b_{\text{efforB}}(f)}{2} + H_{\text{oExt}} \right) \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot \left[\left(H_{\text{or}} - \frac{\frac{b_{\text{efforB}}(f)}{2} + H_{\text{oExt}}}{2} \right) - c_{\text{effB}}(f) \right]^2 \dots \\
 & + \frac{b_{\text{effirB}}(f)}{2} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left(\frac{b_{\text{effirB}}(f)}{4} + BS - c_{\text{effB}}(f) \right)^2 \dots \\
 & + \frac{b_{\text{effirB}}(f)}{2} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot \left[\left(H_{\text{ir}} + BS - \frac{b_{\text{effirB}}(f)}{4} \right) - c_{\text{effB}}(f) \right]^2 \dots \\
 & + b_{\text{effc}}(f) \cdot (t_{\text{c}} - CA_{\text{c}}) \cdot \left(\frac{H_{\text{or}} - H_{\text{oExt}} + H_{\text{ir}}}{2} - c_{\text{effB}}(f) \right)^2 \dots \\
 & + W_{\text{iExt}} \cdot (t_{\text{ir}} - CA_{\text{ir}}) \cdot (BS + H_{\text{ir}} - c_{\text{effB}}(f))^2 + W_{\text{oExt}} \cdot (t_{\text{or}} - CA_{\text{or}}) \cdot (H_{\text{or}} - c_{\text{effB}}(f))^2 \dots \\
 & + \int_{0 \cdot \text{ft}}^{W_{\text{pon}}} \frac{(t_{\text{d}} - CA_{\text{d}}) \cdot \left(\frac{x}{W_{\text{pon}}} \cdot BS - c_{\text{effB}}(f) \right)^2}{\cos(\theta_{\text{BS}})} dx
 \end{aligned}$$

$$S_{\text{effB}}(f) := \frac{I_{\text{effB}}(f)}{\max(c_{\text{effB}}(f), H_{\text{or}} - c_{\text{effB}}(f))}$$

$$S_{\text{effB}}(10 \cdot \text{psi}) = 6.47 \text{ft}^{2.00} \cdot \text{in}$$

Internal Pontoon Floating Roof Design

M. Check Pontoon Ring Strength

$$n_{rpE} = 527.73 \cdot \frac{\text{lbs}}{\text{in}}$$

$$\Omega_C := 1.8$$

$$\Omega_b := 1.67$$

$$P_p := n_{rpE} \cdot R_{ir}$$

$$P_p = 616.39 \cdot \text{kip}$$

$$F'_{cr}(n) := \frac{E \cdot I_{effC}(36 \cdot \text{ksi}) \cdot (n^2 - 4)}{4 \cdot R_{ir} \cdot R_{eff}^2 \cdot \left(1 + \frac{4 \cdot E \cdot I_{effC}(36 \cdot \text{ksi})}{n^2 \cdot C_T} \right)}$$

$$K_f := \gamma_w \cdot SG_{min} \cdot W_{pon}$$

$$F''_{cr}(n) := 4 \cdot \frac{K_f \cdot R_{eff}^2}{R_{ir} \cdot n^2}$$

$$F''_{cr}(4) = 14378.14 \cdot \frac{\text{lbs}}{\text{ft}}$$

$$F_{crp} := \min(F'_{cr}(4) + F''_{cr}(4), F'_{cr}(8) + F''_{cr}(8))$$

$$F_{crp} = 15442.92 \cdot \frac{\text{lbs}}{\text{ft}}$$

$$P_{crp} := \frac{1}{\Omega_C} \cdot F_{crp} \cdot R_{ir}$$

$$P_{crp} = 835.06 \cdot \text{kip}$$

$$P_{yp} := \frac{1}{\Omega_C} \cdot A_{effC}(F_{yp}) \cdot F_{yp}$$

$$P_{yp} = 996.63 \cdot \text{kip}$$

Internal Pontoon Floating Roof Design

M. Check Pontoon Ring Strength

$$P_n := \min(P_{crp}, P_{yp})$$

$$\frac{P_p}{P_n} = 73.81\%$$

$$M_p = 401.74 \cdot \text{ft} \cdot \text{kip}$$

$$M_n := \frac{1}{\Omega_b} \cdot S_{effB}(F_{yp}) \cdot F_{yp}$$

$$M_n = 693.46 \cdot \text{ft} \cdot \text{kip}$$

$$\frac{M_p}{M_n} = 57.93\%$$

$$INT_{PM} := \begin{cases} \frac{P_p}{P_n} + \frac{M_p}{M_n} & \text{if } \frac{P_p}{P_n} \leq 0.15 \\ \max \left(\left(\frac{P_p}{P_n} + \frac{M_p}{M_n} \right), \left(\frac{P_p}{P_{yp}} + \frac{M_p}{M_n} \right) \right) & \text{otherwise} \end{cases}$$

$$INT_{PM} = 131.75\%$$

$$\frac{t_{or}}{t_{ir}} = 100.00\%$$

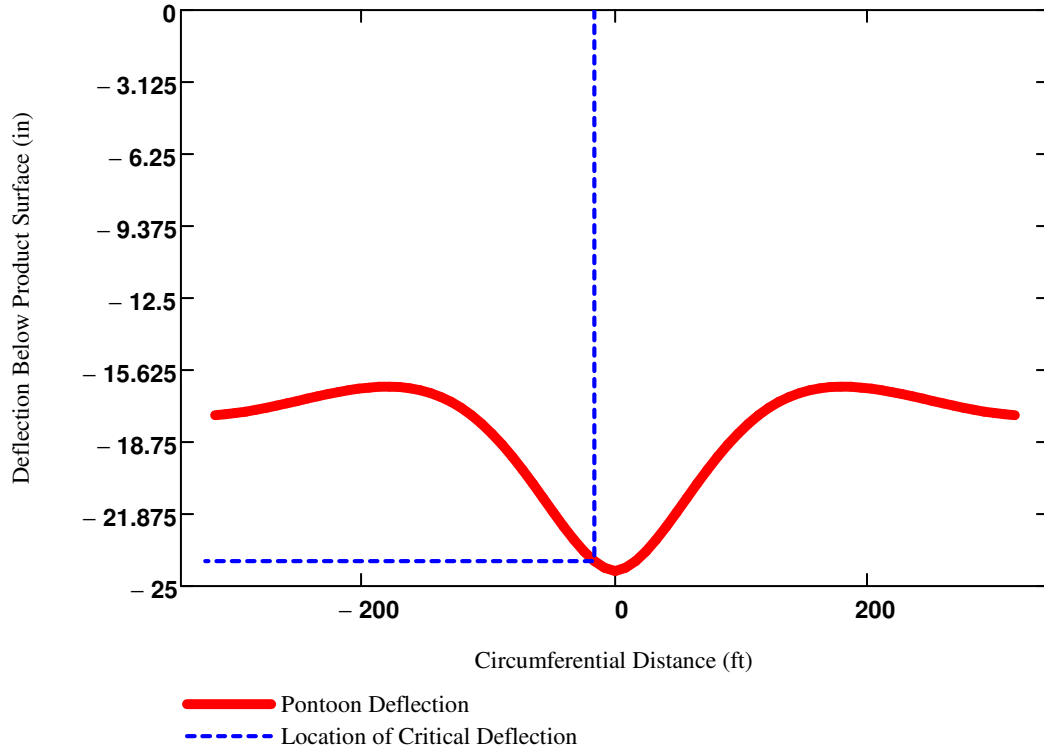
Internal Pontoon Floating Roof Design

N. Check Pontoon Ring Floating Stability

$$\frac{2 \cdot |\Delta_{TOT}|}{H_{ir} + (H_{or} - H_{oExt} - BS)} = 83.93\%$$

$$\Delta_{TOT} = -23.92 \text{ in}$$

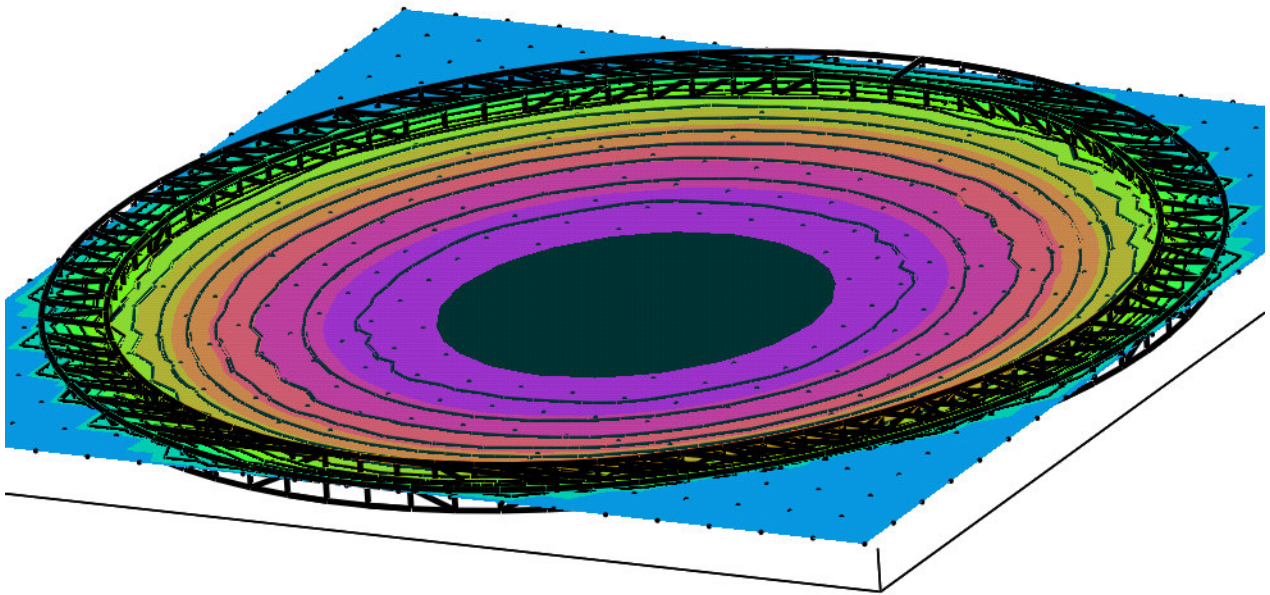
Check pontoon floating stability



Internal Pontoon Floating Roof Design

O. Plot of Results

3D Plot of Deflected Pontoon



Internal Pontoon Floating Roof Design

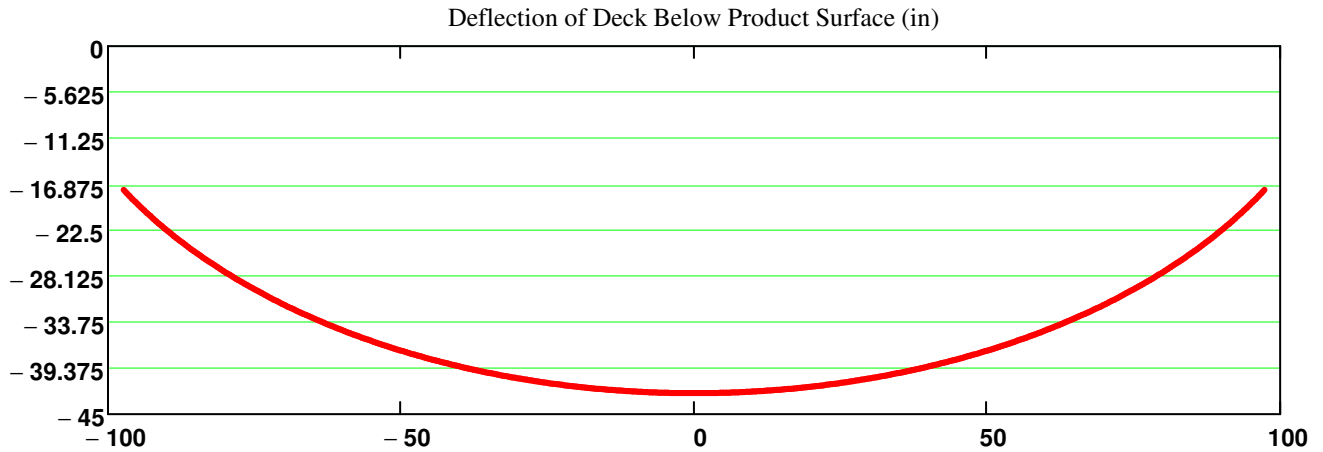
O. Plot of Results

Deflection of deck relative to pontoon attachment

$$\delta_{deck_{rows}}(\delta_{deck}) = -24.85 \text{ in}$$

Deflection of deck relative to product surface

$$\delta_{deck_{rows}}(\delta_{deck}) + \frac{\delta_{pon_{rows}}(\delta_{pon}) + \delta_{pon_1}}{2} = -42.44 \text{ in}$$



Internal Pontoon Floating Roof Design

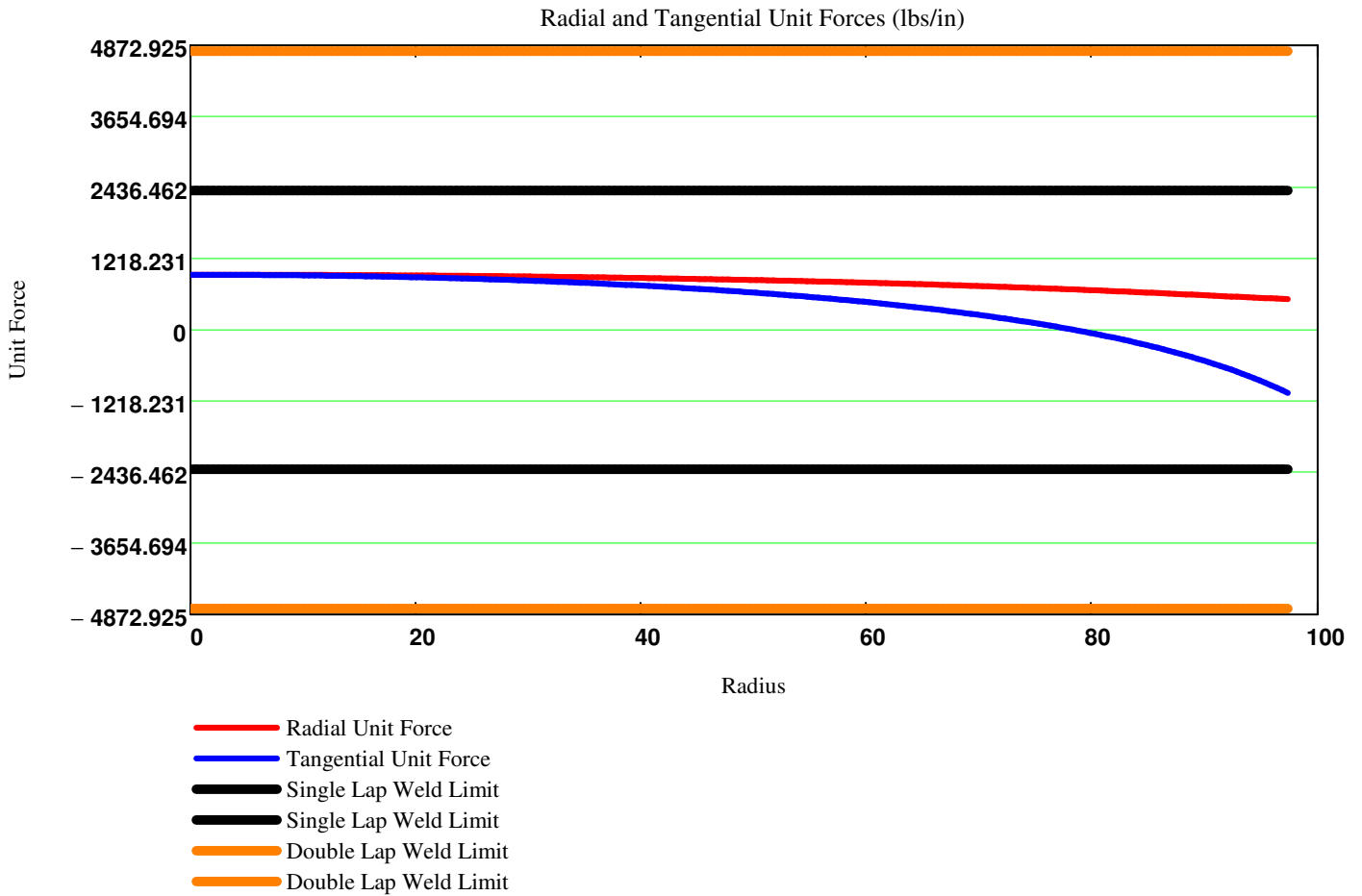
O. Plot of Results

$$i := 1 \dots \text{rows}(r_{\text{deck}})$$

Safety factor for
 weld strength

Maximum unit for in weld per AISC 360

$$\Omega_w := 2 \quad n_{d\text{Max}_i} := \frac{(t_d - CA_d) \cdot 0.7071 \cdot 0.6 \cdot F_{uw}}{\Omega_w} \quad n_{d\text{Max}_1} = 2386.46 \frac{\text{lbs}}{\text{in}}$$



Unit force curves must be within single lap weld limit, otherwise double lap weld is required. If double lap weld is limit is exceeded, geometry must be changed. Deck shall have a 2" in 12" underside weld at all supports, bulkheads, and appurtenances as a minimum.