EXAMPLE 6.8.1Structural Steel Corbel

Given:

The structural steel corbel shown.

$$f_c' = 5000 \text{ psi, normalweight}$$

Problem:

Find the design strength.

Solution:

Effective width b = confined width (8 in.) or

$$b = 2.5w = 2.5(4) = 10$$
 in.

Use
$$b = 8$$
 in.

$$e = 4 + 10/2 = 9 \text{ in.}$$

$$V_c = \frac{0.85 f_c' b \ell_e}{1 + 3.6 e' \ell_e'} = \frac{0.85(5)(8)(10)}{1 + 3.6(9)/(10)} = 80.2 \text{ kip}$$

Since the A_s bars are anchored above and below, they can be counted twice.

$$A_s = (2) \#4 = 2(2)(0.2) = 0.80 \text{ in.}^2$$

$$V_r = \frac{2A_s f_y}{1 + \frac{6e / \ell_e}{(4.8s / \ell_e) - 1}} = \frac{2(0.80)(60)}{1 + \frac{6(9) / (10)}{[4.8(7) / (10)] - 1}} = 29.2 \text{ kip}$$

$$\phi V_n = 0.75(80.2 + 29.2) = 82.0 \text{ kip}$$

Alternatively, using Design Aids 6.15.10 and 6.15.11:

For
$$b = 8$$
 in.; $a = 4$ in.; $\ell_e = 10$ in.

Read
$$\phi V_c = 60 \text{ kip}$$

For
$$A_s = (2)$$
 #4, anchored above and below: $V_r = 4(7) = 28$ kip $\phi V_n = 60 + 0.75(28) = 81$ kip

Steel section flexural capacity:

From AISC Steel Construction Manual:

$$Z_p = 14.6$$

Assume $V_u = 85$ kip.

$$\phi V_n = \frac{\phi Z_p F_y}{a + 0.5 V_n / (0.85 f_c' b)} = \frac{0.9 (14.6) (46)}{4 + 0.5 (85) / (0.85) (5) (8)} = 115.1 \text{ kip} > 82.0 \text{ kip}$$

Since the bar must be anchored for forces above and below, twice the minimum length of weld from Design Aid 6.14.3 is required: 2(1.75) = 3.5 in. each bar.