

## Function Definitions:

Equivalent resistance , two parallel resistances:  $R_{par}(r1, r2) := \frac{r1 \cdot r2}{r1 + r2}$

Line current:  $I_L(P) := \frac{P}{\sqrt{3} \cdot V_{LL}}$

Balanced delta to wye conversion:  $R_{\Delta Y}(r_{\Delta}) := \frac{r_{\Delta}}{3}$

Balanced wye to delta conversion:  $R_{Y\Delta}(r_Y) := 3 \cdot r_Y$

## Variable Definitions:

Heating element resistance  $R := 5 \Omega$

Nominal system voltage  $V_{LL} := 208 \text{ V}$

## Calculations:

Nominal line-to-neutral voltage  $V_{LN} := \frac{V_{LL}}{\sqrt{3}}$   $V_{LN} = 120 \text{ V}$

Line current, each phase:

Delta, parallel heating elements  $P_{\Delta p} := 3 \cdot \frac{V_{LL}^2}{\left(\frac{R}{2}\right)}$   $P_{\Delta p} = 51.92 \text{ kW}$   $I_L(P_{\Delta p}) = 144.11 \text{ A}$   
 Define this as the base power.

Percentage of base power:

Delta, single heating element  $P_{\Delta} := 3 \cdot \frac{V_{LL}^2}{R}$   $P_{\Delta} = 25.96 \text{ kW}$   $\frac{P_{\Delta}}{P_{\Delta p}} = 50 \%$   $I_L(P_{\Delta}) = 72.05 \text{ A}$

Delta, series heating elements  $P_{\Delta s} := 3 \cdot \frac{V_{LL}^2}{2 \cdot R}$   $P_{\Delta s} = 12.98 \text{ kW}$   $\frac{P_{\Delta s}}{P_{\Delta p}} = 25 \%$   $I_L(P_{\Delta s}) = 36.03 \text{ A}$

Wye, parallel heating elements  $P_{Yp} := 3 \cdot \frac{V_{LN}^2}{\left(\frac{R}{2}\right)}$   $P_{Yp} = 17.31 \text{ kW}$   $\frac{P_{Yp}}{P_{\Delta p}} = 33.33 \%$   $I_L(P_{Yp}) = 48.04 \text{ A}$

Wye, single heating element  $P_Y := 3 \cdot \frac{V_{LN}^2}{R}$   $P_Y = 8.65 \text{ kW}$   $\frac{P_Y}{P_{\Delta p}} = 16.67 \%$   $I_L(P_Y) = 24.02 \text{ A}$

Wye, series heating elements  $P_{Ys} := 3 \cdot \frac{V_{LN}^2}{2 \cdot R}$   $P_{Ys} = 4.33 \text{ kW}$   $\frac{P_{Ys}}{P_{\Delta p}} = 8.33 \%$   $I_L(P_{Ys}) = 12.01 \text{ A}$

Delta with internal wye (convert internal wye to delta equivalent; eq. is in parallel with original delta)  $P_{\Delta Y} := 3 \cdot \frac{V_{LL}^2}{R_{par}(R, R_{Y\Delta}(R))}$   $P_{\Delta Y} = 34.61 \text{ kW}$   $\frac{P_{\Delta Y}}{P_{\Delta p}} = 66.67 \%$   $I_L(P_{\Delta Y}) = 96.07 \text{ A}$

Wye with internal delta (convert internal delta to wye equivalent; eq. is in series with original wye)  $P_{Y\Delta} := 3 \cdot \frac{V_{LN}^2}{R + R_{\Delta Y}(R)}$   $P_{Y\Delta} = 6.49 \text{ kW}$   $\frac{P_{Y\Delta}}{P_{\Delta p}} = 12.5 \%$   $I_L(P_{Y\Delta}) = 18.01 \text{ A}$